

Combined H1 & ZEUS data and HERAPDF0.1

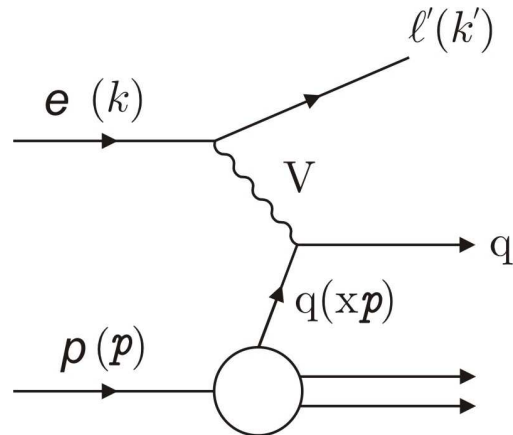
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On behalf of the HERA Structure Function
Working Group

- ❖ Combined deep inelastic data
- ❖ NLO QCD fit to the combined data
- ❖ Outlook



Deep Inelastic Scattering at HERA



Neutral Current $ep \rightarrow eX$, $V = \gamma$ or Z^0

Charged Current $ep \rightarrow \nu X$, $V = W^\pm$

Kinematics

$$Q^2 = -(k - k')^2 \quad x = \frac{Q^2}{2p \cdot q} \quad y = \frac{p \cdot q}{p \cdot k} \quad q = k - k'$$

$$s = (k + p)^2 \quad Q^2 = sxy \quad Y_\pm = 1 \pm (1 - y)^2$$

$$\frac{d^2 \sigma^{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ F_2^{NC}(x, Q^2) \mp Y_- x F_3^{NC}(x, Q^2) \right]^\dagger$$

$$\frac{d^2 \sigma^{CC}(e^\pm p)}{dx dQ^2} = \frac{G_F^2}{4\pi x} \frac{M_W^4}{(Q^2 + M_W^2)^2} \left[Y_+ F_2^{CC}(x, Q^2) \mp Y_- x F_3^{CC}(x, Q^2) \right]^\dagger$$

$$F_2^{NC} \simeq \sum_i e_i^2 x(q_i + \bar{q}_i) \quad (\gamma \text{ only}); \quad F_2^{CC} = \sum_i x(q_i + \bar{q}_i); \quad xF_3^{CC} = \sum_i x(q_i - \bar{q}_i)$$

$q_i(x, Q^2)$ - momentum density of quark flavour i in proton

\dagger F_L has been ignored

Combined deep inelastic data

- ❖ Scope of the project
- ❖ Data
- ❖ Method
- ❖ Results

Scope of the project

- ❖ Combination of HERA-I (1994-2000) inclusive DIS cross-sections
 - more precisely reduced cross-sections (the terms in [] on slide 2)
- ❖ Exploit the different technology of the H1 and ZEUS detectors to ‘cross-calibrate’, and hence reduce the systematic uncertainties
- ❖ The basic assumption is that the two experiments are measuring the same cross-sections at the same (x, Q^2) point.
- ❖ The method (developed by A. Glazov) uses an iterative χ^2 minimisation which takes full account of error correlations
 - first discussed at DIS2005 and then at the HERA-LHC Workshop
- ❖ Preliminary results for the combined data as submitted to LP2007 and presented at DIS2008 (Feltesse)

Input NC & CC data sets: $1.5 < Q^2 < 30000 \text{ GeV}^2$, 240 pb^{-1}

data set		x range		Q^2 range (GeV^2)		\mathcal{L} pb^{-1}	comment
H1 NC min. bias	97	0.00008	0.02	1.5	12	1.8	$e^+p \sqrt{s} = 301 \text{ GeV}$
H1 NC low Q^2	96 – 97	0.000161	0.20	12	150	17.9	$e^+p \sqrt{s} = 301 \text{ GeV}$
H1 NC	94 – 97	0.0032	0.65	150	30 000	35.6	$e^+p \sqrt{s} = 301 \text{ GeV}$
H1 CC	94 – 97	0.013	0.40	300	15 000	35.6	$e^+p \sqrt{s} = 301 \text{ GeV}$
H1 NC	98 – 99	0.0032	0.65	150	30 000	16.4	$e^-p \sqrt{s} = 319 \text{ GeV}$
H1 CC	98 – 99	0.013	0.40	300	15 000	16.4	$e^-p \sqrt{s} = 319 \text{ GeV}$
H1 NC	99 – 00	0.00131	0.65	100	30 000	65.2	$e^+p \sqrt{s} = 319 \text{ GeV}$
H1 CC	99 – 00	0.013	0.40	300	15 000	65.2	$e^+p \sqrt{s} = 319 \text{ GeV}$
ZEUS NC	96 – 97	0.00006	0.65	2.7	30 000	30.0	$e^+p \sqrt{s} = 301 \text{ GeV}$
ZEUS CC	94 – 97	0.015	0.42	280	17 000	47.7	$e^+p \sqrt{s} = 301 \text{ GeV}$
ZEUS NC	98 – 99	0.005	0.65	200	30 000	15.9	$e^-p \sqrt{s} = 319 \text{ GeV}$
ZEUS CC	98 – 99	0.015	0.42	280	30 000	16.4	$e^-p \sqrt{s} = 319 \text{ GeV}$
ZEUS NC	99 – 00	0.005	0.65	200	30 000	63.2	$e^+p \sqrt{s} = 319 \text{ GeV}$
ZEUS CC	99 – 00	0.008	0.42	280	17 000	60.9	$e^+p \sqrt{s} = 319 \text{ GeV}$

NB: H1 NC min. bias ($Q^2 < 12 \text{ GeV}^2$) moved up by 3.4 % after re-analysis of luminosity

Some details

- ❖ Common (x, Q^2) bins: H1 x ; ZEUS Q^2
- ❖ Shift measured data by simple interpolation using H1PDF2k
 - checked using ZEUS-Jets, NC shift factors agree within a few permille, some $CC < 2\%$. - differences much less than statistical errors.
- ❖ Move data to 920 GeV E_p beam energy
 - simple interpolation for CC
 - additive for NC
 - systematic uncertainty from F_L : compare $F_L = 0$ and $F_L = F_L(\text{H1PDF2k})$, up to 5% at high y .
 - treat as a correlated ‘procedural’ systematic uncertainty

χ^2 for a single data set

$$\chi_{\text{exp}}^2(M^{i,\text{true}}, \Delta\alpha_j) = \sum_i \frac{\left[M^{i,\text{true}} - \left(M^i + \sum_j \frac{\partial M^i}{\partial \alpha_j} \Delta\alpha_j \right) \right]^2}{\sigma_i^2} + \sum_j \frac{(\Delta\alpha_j)^2}{\sigma_{\alpha_j}^2}$$

M^i measured central values

σ_i statistical and uncorrelated systematic uncertainties

σ_{α_j} correlated systematic uncertainties

$\frac{\partial M^i}{\partial \alpha_j}$ sensitivity of datum i to systematic j

$M^{i,\text{true}}$ fitted combined H1 - ZEUS data

$\Delta\alpha_j$ fitted shifts of correlated uncertainties

By definition $\chi^2 = 0$ for $M^{i,\text{true}}$ and $\Delta\alpha_j = 0$;

$\text{Cov}(M^{i,\text{true}}, M^{j,\text{true}})$ gives the error matrix for the combined data

Caveat

- ❖ In principle a nice simple χ^2 which allows minimisation by linear equations
- ❖ Unbiased for uncertainties independent of the central value (additive)
- ❖ However, for cross-sections, many uncertainties are proportional to the central value (multiplicative)
- ❖ This introduces a bias, as a smaller M^i will have a smaller relative error and hence give a smaller overall χ^2
- ❖ Modify χ^2 - translate multiplicative to additive uncertainty using $M^{i,true}$, common to all measurements

Revised χ^2 for a single data set

$$\chi_{\text{exp}}^2(M^{i,\text{true}}, \Delta\alpha_j) = \sum_i \frac{\left[M^{i,\text{true}} - \left(M^i + \sum_j \frac{\partial M^i}{\partial \alpha_j} \frac{M^{i,\text{true}}}{M^i} \Delta\alpha_j \right) \right]^2}{\left(\sigma_i \frac{M^{i,\text{true}}}{M^i} \right)^2} + \sum_j \frac{(\Delta\alpha_j)^2}{\sigma_{\alpha_j}^2}$$

Minimisation is now non - linear, use an iterative procedure

1. Minimise original χ^2 to find an initial approximation to $\{M^{i,\text{true}}\}$
2. Scale errors $\sigma_i \rightarrow \sigma_i \frac{M^{i,\text{true}}}{M^i}$
3. Repeat step 1

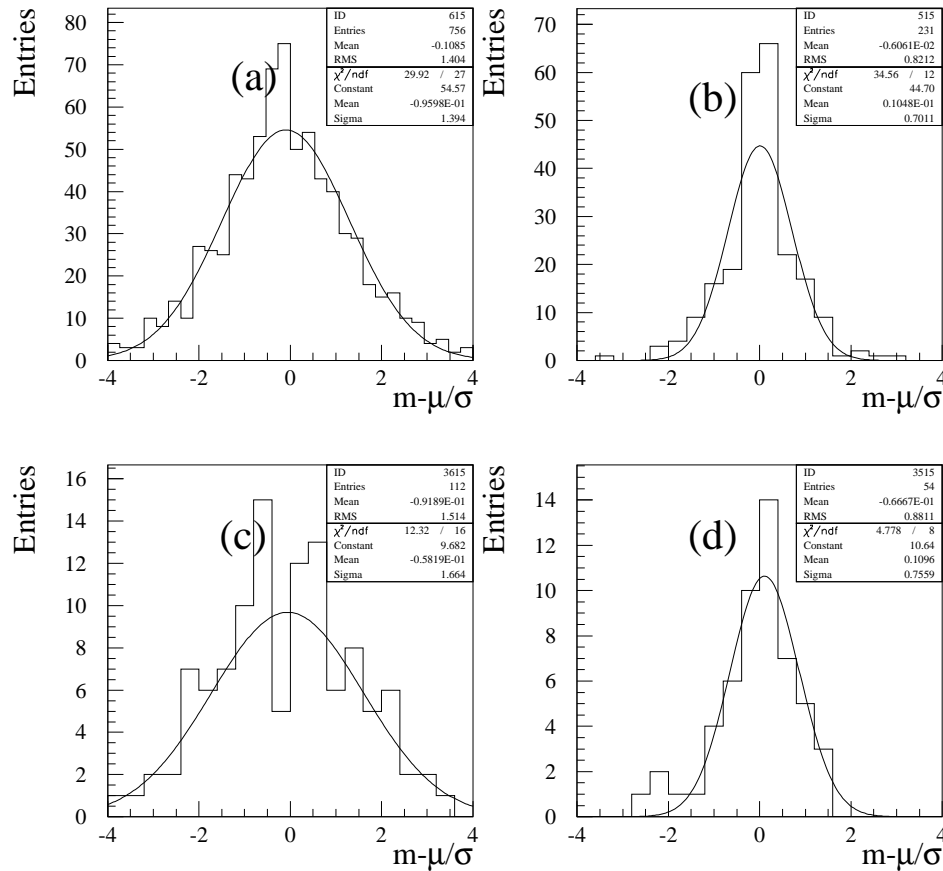
Convergence is usually after two iterations

Full χ^2 is the sum over all χ_{exp}^2 .

Uncertainties

- ❖ Statistical uncertainties are uncorrelated
- ❖ Systematic uncertainties:
 - point-to-point uncorrelated, added in quadrature to statistical giving a total point-to-point uncorrelated uncertainty
 - point-to-point correlated errors, (e.g. energy scales), often common for CC and NC measurements for a given experiment and run period
 - multiplicative or additive? Try both – gives additional uncertainty $< 1\%$ for low Q^2 rising to 1.5% at large Q^2
 - overall normalisation uncertainty, similarly common for a given experiment and run period (clearly multiplicative)
- ❖ Correlations between H1 and ZEUS, (e.g. MC simulations, calibration methods..), 12 possible sources identified
 - compare $2^{12}-1$ averages taking all pairs as correlated or uncorrelated in turn to give deviation from central values
 - largest ($\sim 1\%$) from photoproduction MC and hadronic energy scales
 - treat these as procedural uncertainties

Quality of the fit



1153 individual NC, CC data
averaged to 573 points

$$\chi^2 = 510$$

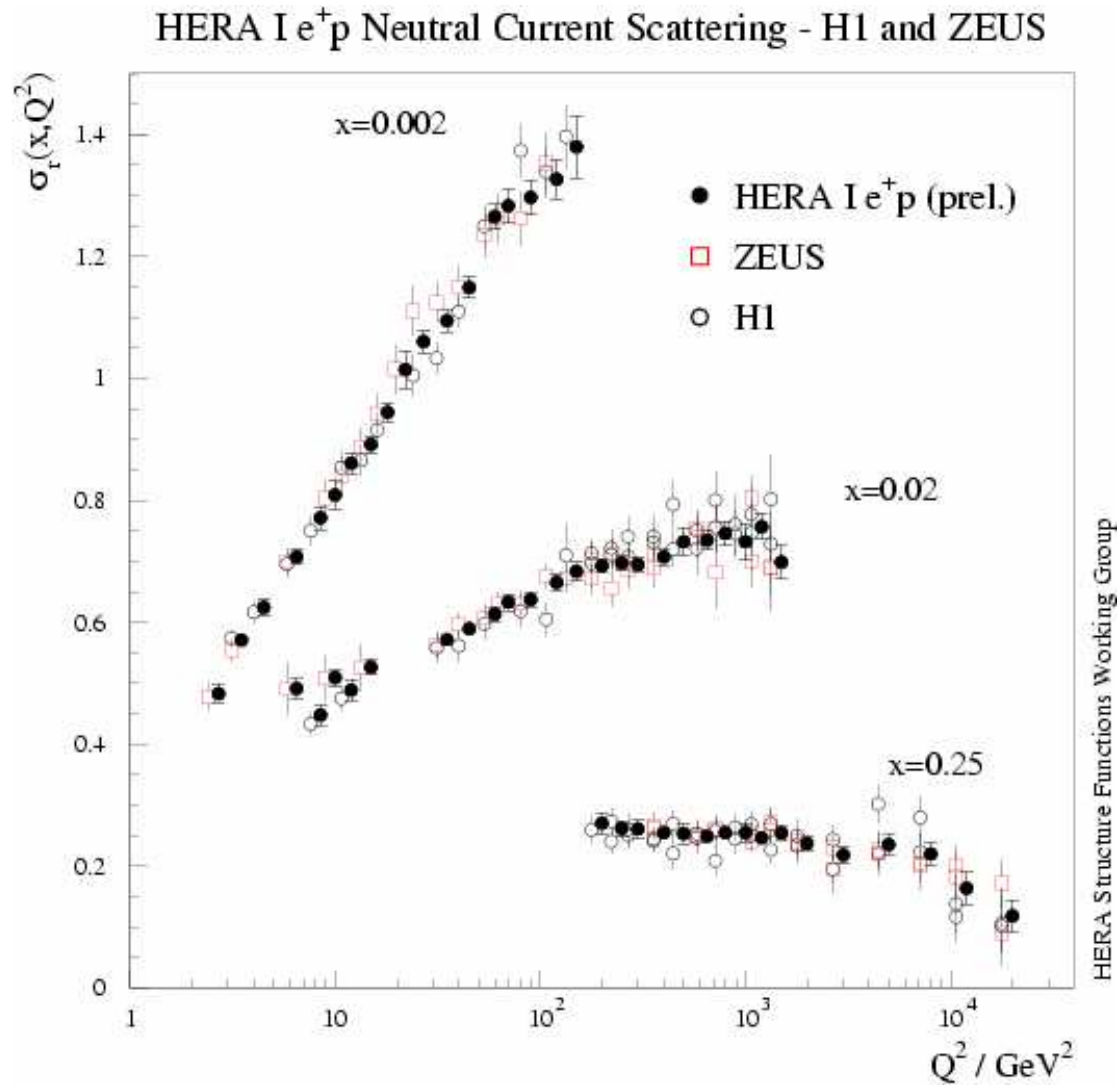
	Pulls	
	Mean	Sigma
(a) NC e+p	-0.09	1.4
(b) NC e-p	0.01	0.7
(c) CC e+p	-0.05	1.7
(c) CC e-p	0.1	0.8

A total of 43 systematic uncertainties from the data and 4 from the averaging procedure

Comments on the results

- ❖ All uncertainties lie within 1σ of the central value of published data
 - except the normalisation of H1 NC low Q^2 (1996-7), up by 1.6σ
- ❖ Almost all systematic uncertainties reduced, eg
 - H1 rear calorimeter energy scale by a factor of 3
 - ZEUS forward energy flow modelling by a factor of 4
- ❖ Overall precision improved
 - $Q^2 < 12 \text{ GeV}^2$, separately 2-3%, combined better than 2%
 - medium Q^2 , 1.5% achieved
 - highest Q^2 , 10% achieved, increased statistics now important
- ❖ Both H1PDF2k and ZEUS-Jets PDFs describe the combined data well

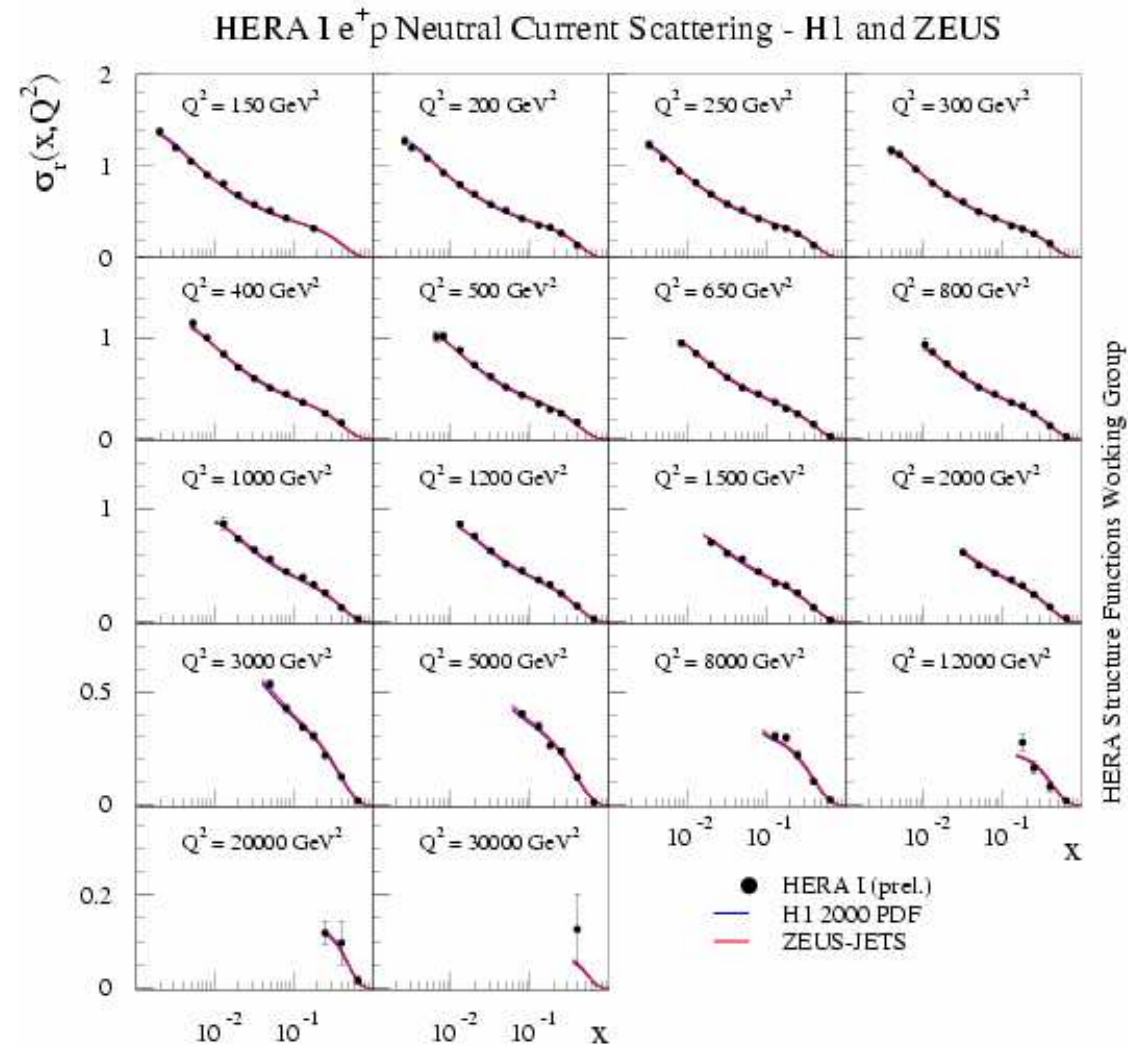
Examples (I): NC e^+p , at fixed x



Combined data is smoother than that of either H1 or ZEUS – with significantly smaller uncertainties

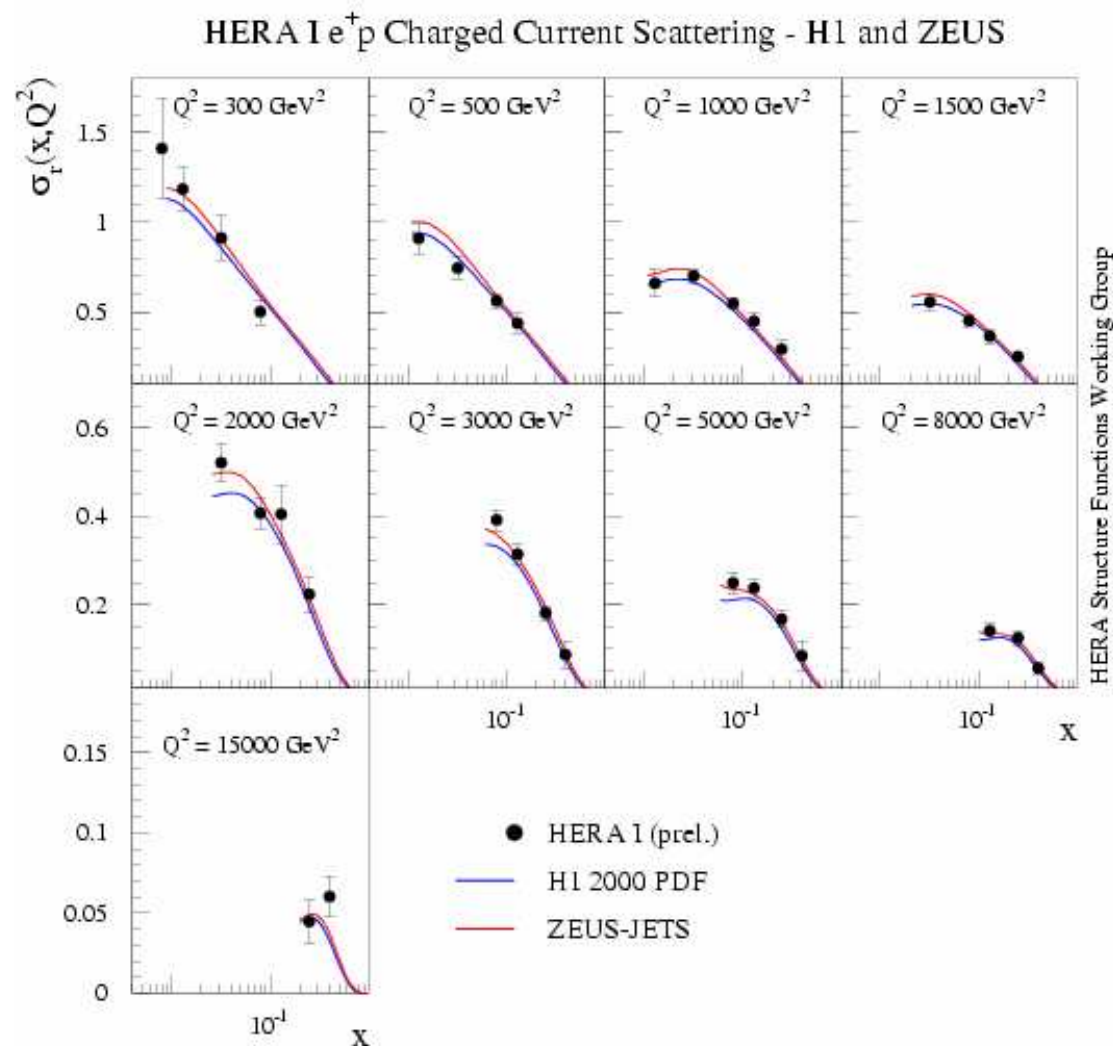
Examples (II): NC e^+p , high Q^2

Combined data
compared to
H1PDF2k &
ZEUS-Jets
calculations



Examples (III): CC e^+p

Combined data
compared to
H1PDF2k &
ZEUS-Jets
calculations



Combined data – summary & outlook

- ❖ A robust procedure has been developed for combining the H1 and ZEUS NC and CC reduced cross-section data
- ❖ The experiments cross calibrate each other, leading to a significant reduction in systematic uncertainties across the kinematic plane, in addition at large Q^2 there is a reduction in statistical error
- ❖ It is hoped to publish the combined data later this year (H1 has a couple of HERA-I NC data sets still to be published)
- ❖ HERA-II data on NC and CC cross-sections with polarised e^+ and e^- beams are being extracted by H1 and ZEUS
- ❖ Once the individual results are published, the combined HERA-II data will be produced

NLO QCD fit to the combined HERA data

- ❖ Context & Scope
- ❖ Form of the PDF parameterisation
- ❖ Error/uncertainty treatment
- ❖ Model assumptions
- ❖ HERAPDF0.1
- ❖ Comparisons
- ❖ LHAPDF
- ❖ Summary

Context & Scope

- ❖ H1PDF2k and ZEUS-Jets, most recent PDF sets from H1 and ZEUS
 - differ in many details (parameterisation and choice of partons, uncertainty treatment, input data)
 - results broadly compatible, but the gluon PDFs in particular are different
- ❖ Goal is an NLO PDF fit to the combined HERA-I data alone
- ❖ A lot of preliminary and ongoing work undertaken by the H1-ZEUS team, e.g.
 - try each other's approaches on own data and combined data
 - try both hessian and offset methods for uncertainty estimates
 - try different flavour break-ups and heavy flavour schemes
 - etc
- ❖ The outcome (HERAPDF0.1) should be viewed as work in progress

HERA PDF parameterisation at Q_0^2

$$xf(x, Q_0^2) = Ax^B(1-x)^C(1+Dx+Ex^2+Fx^3+\dots)$$

	A	B	C	D	E
gluon	sum rule				
u_v	sum rule				
d_v	sum rule	$= B(u_v)$			
U_{bar}	$\lim_{x \rightarrow 0} U/D \rightarrow 1$				
D_{bar}		$= B(U)$			

Optimisation and
constraints on
parameters

Partons fitted : $xg, xu_v, xd_v, x\bar{U} = x\bar{u} + x\bar{c}, x\bar{D} = x\bar{d} + x\bar{s} + x\bar{b}$

Sea flavour break - up at Q_0 : $s = f_s D, c = f_c U, A_{\bar{U}} = (1 - f_s)A_{\bar{D}} / (1 - f_c)$

with $f_s = 0.33, f_c = 0.15$

Parameter optimisation: start with A, B, C (BLUE) add D, E ,F... until no χ^2 advantage – find only D & E (red) non zero for xu_v

This form is derived from the H1 and ZEUS parameterisations

less model dependence for B parameters than H1 form

no additional x(ubar-dbar) input as used in the ZEUS form

More details

- ❖ NLO DGLAP framework for evolving PDFs to arbitrary Q^2
- ❖ Zero-mass variable-number heavy flavour scheme
- ❖ Renormalisation and factorisation scales: Q^2
- ❖ Fit 573 combined HERA-I NC & CC data
- ❖ A total of 11 free parameters

Further fixed parameters :

$$Q_0^2 = 4 \text{ GeV}^2 \text{ (input scale)}$$

$$Q_{\min}^2 = 3.5 \text{ GeV}^2 \text{ (minimum for data)}$$

$$m_c = 1.4 \text{ GeV (charm mass)}, m_b = 4.75 \text{ GeV (beauty mass)}$$

$$\alpha_s(M_Z) = 0.1176 \text{ (PDG 2006 value)}$$

Error/uncertainty treatment

- ❖ Combined data have much reduced errors, systematic uncertainties smaller than statistical across most of (x, Q^2) plane
- ❖ Combine 43 systematic uncertainties of the data with their statistical uncertainties in quadrature, then offset the 4 combination systematic uncertainties. Gives $\chi^2/dof = 476.7/562$
- ❖ Checks:
 - taking 47 systematics in quadrature gives $\chi^2/dof = 428/562$
 - taking all systematics as correlated gives $\chi^2/dof = 553.1/562$
 - all three methods give very similar PDF central values and uncertainties
- ❖ The self consistency and small systematics of the combined data allows the use of $\Delta\chi^2 = 1$ to calculate PDF parameter uncertainties

Model uncertainties

❖ To be added to total PDF uncertainty

$$m_c (1.45): 1.3 \rightarrow 1.55 \text{ GeV}$$

$$m_b (4.75): 4.3 \rightarrow 5.0 \text{ GeV}$$

$$f_s (0.33): 0.25 \rightarrow 0.40$$

$$f_c (0.15): 0.10 \rightarrow 0.20$$

$$Q_0^2 (4.0): 2.0 \rightarrow 6.0 \text{ GeV}^2$$

$$Q_{\min}^2 (3.5): 2.5 \rightarrow 5.0 \text{ GeV}^2$$

❖ To be compared with the results

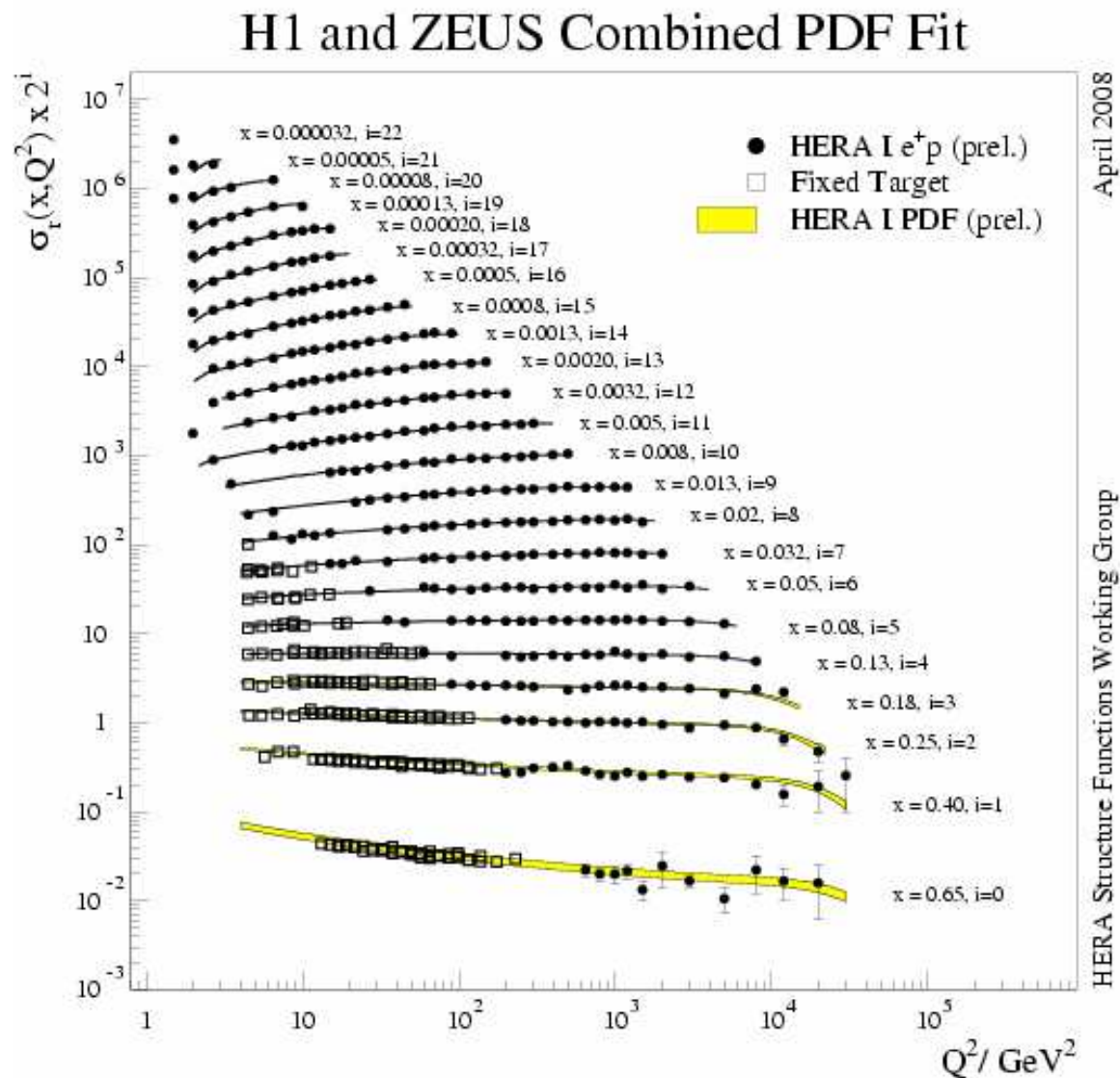
$$\text{Vary } \alpha_s(M_Z) (0.1176): 0.1156 \rightarrow 0.1196$$

$$\text{Vary PDF parameterisation (HERA): H1} \rightarrow \text{ZEUS}$$

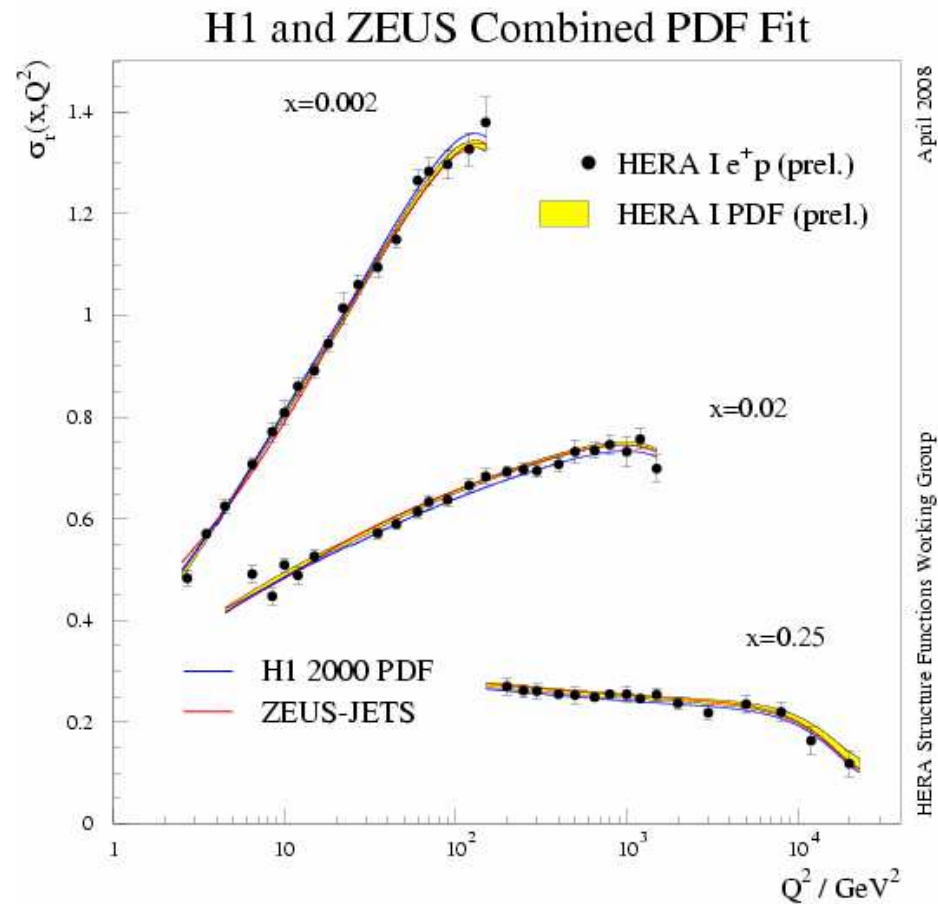
PDF fit results I

HERAPDF0.1
fit quality to
the combined
HERA-I data
for NC e+p

uncertainties on
both data and fit
are included



PDF fit results II



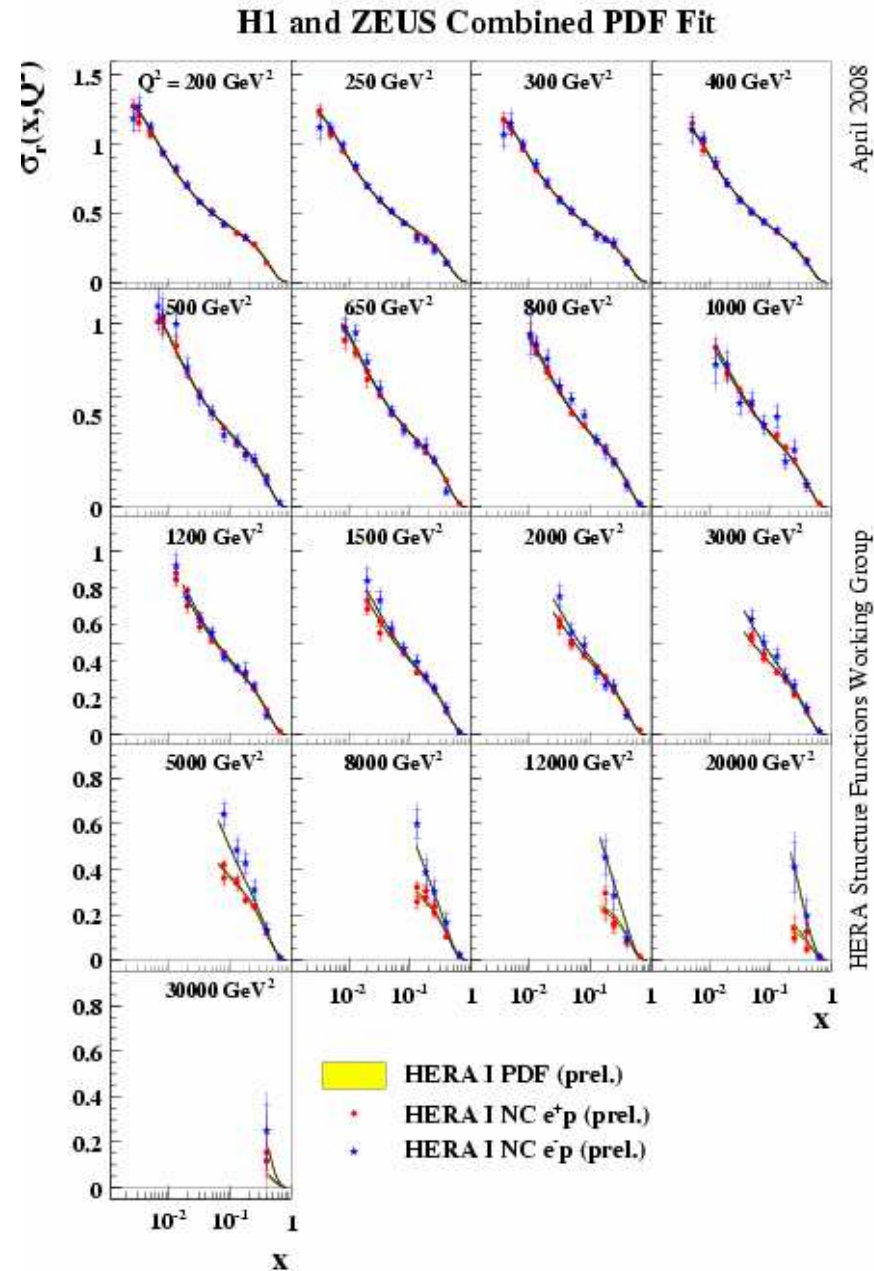
In more detail, for
the three x values
shown on p 13

scaling violation
thru' DGLAP eqns
gives tight constraint
on gluon

PDF fit results III

High Q^2 NC

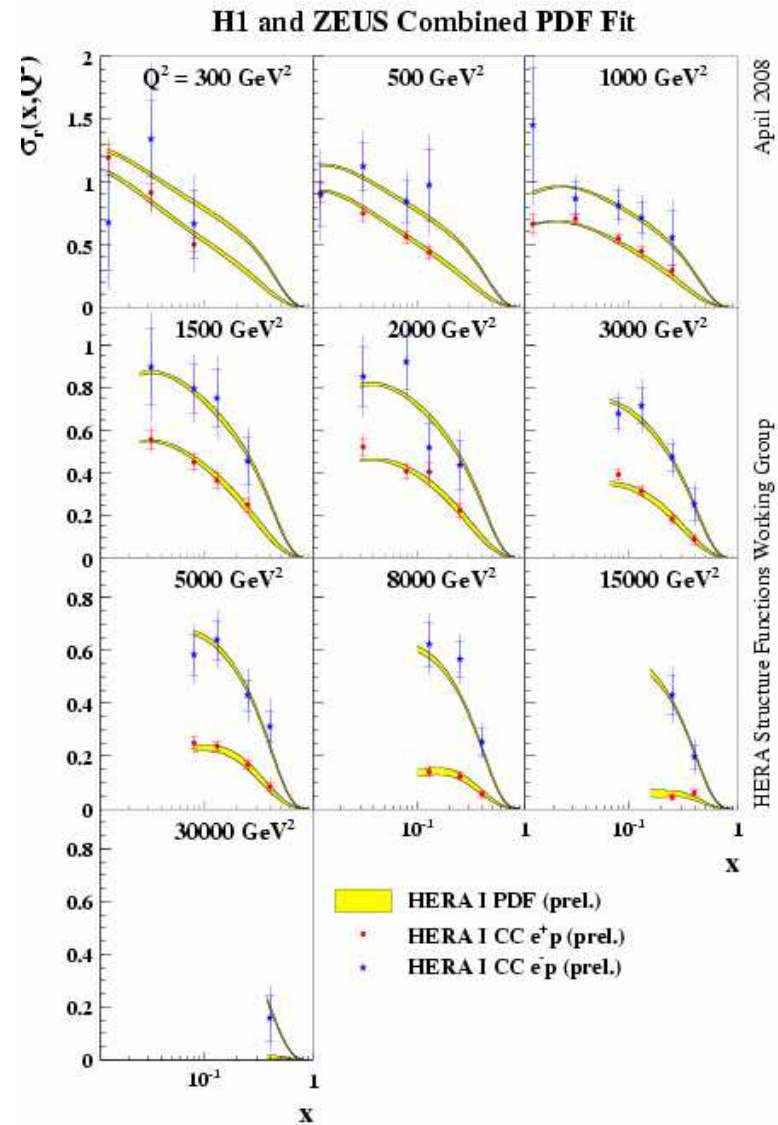
Precision is crucial for the extraction and exploitation of xF_3 and its valence quark dependence



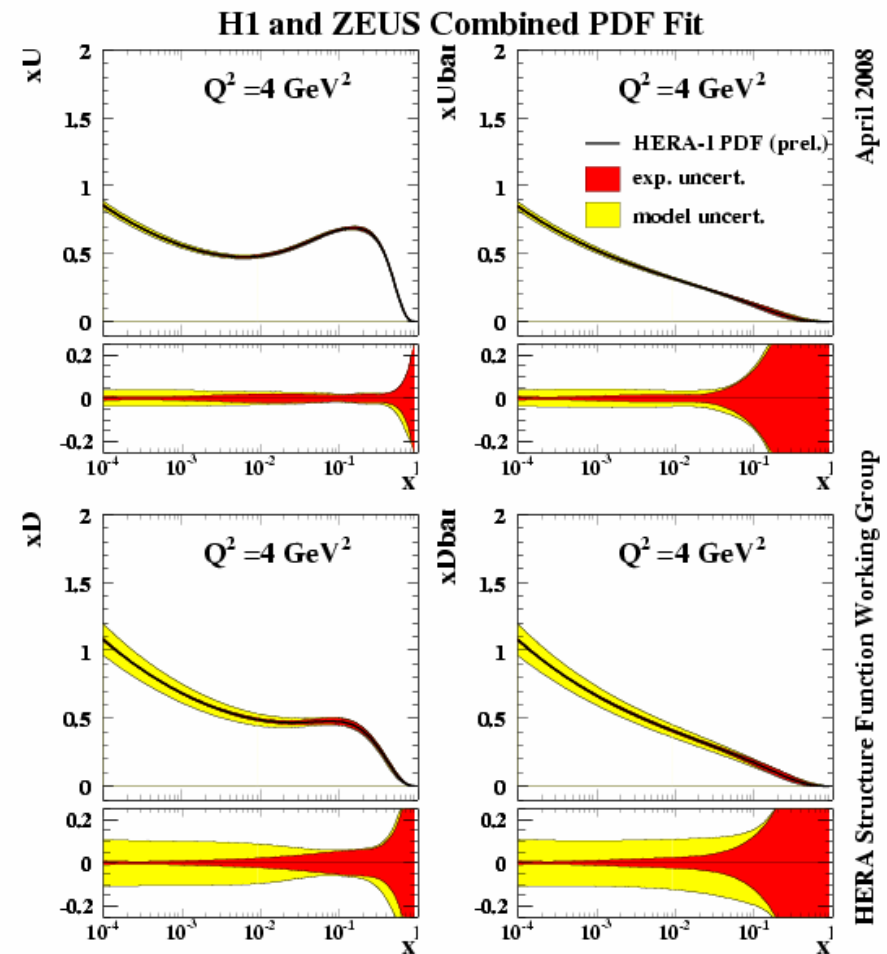
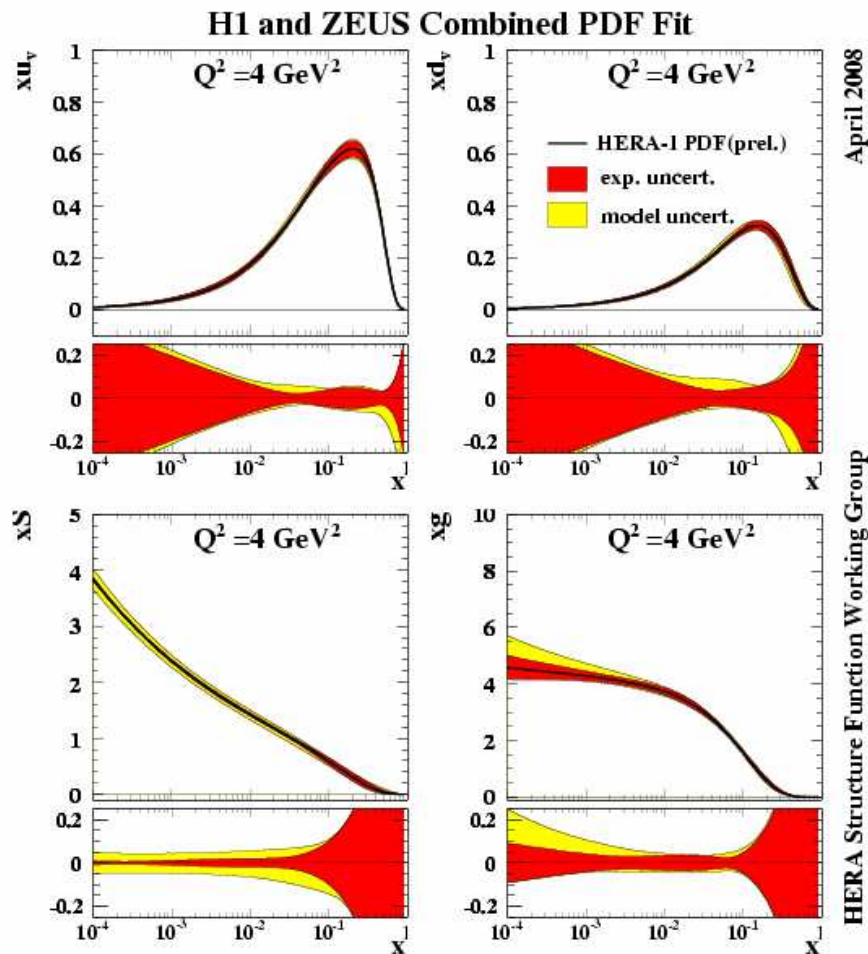
PDF fit results IV

High Q^2 CC

Precision needed to exploit the different flavour dependence of the e^+ and e^- cross-sections

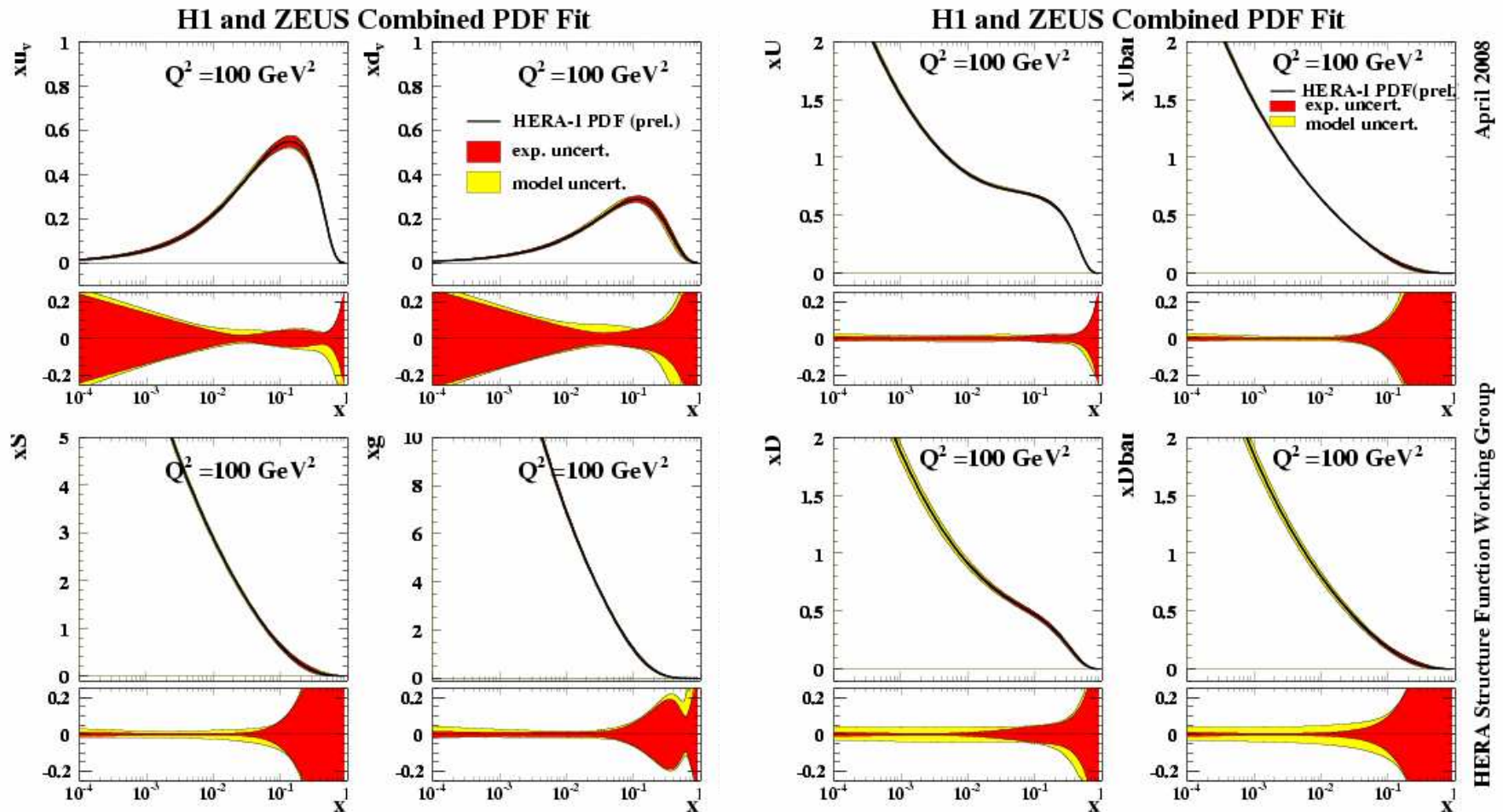


PDFs at the starting scale $Q_0^2 = 4 \text{ GeV}^2$



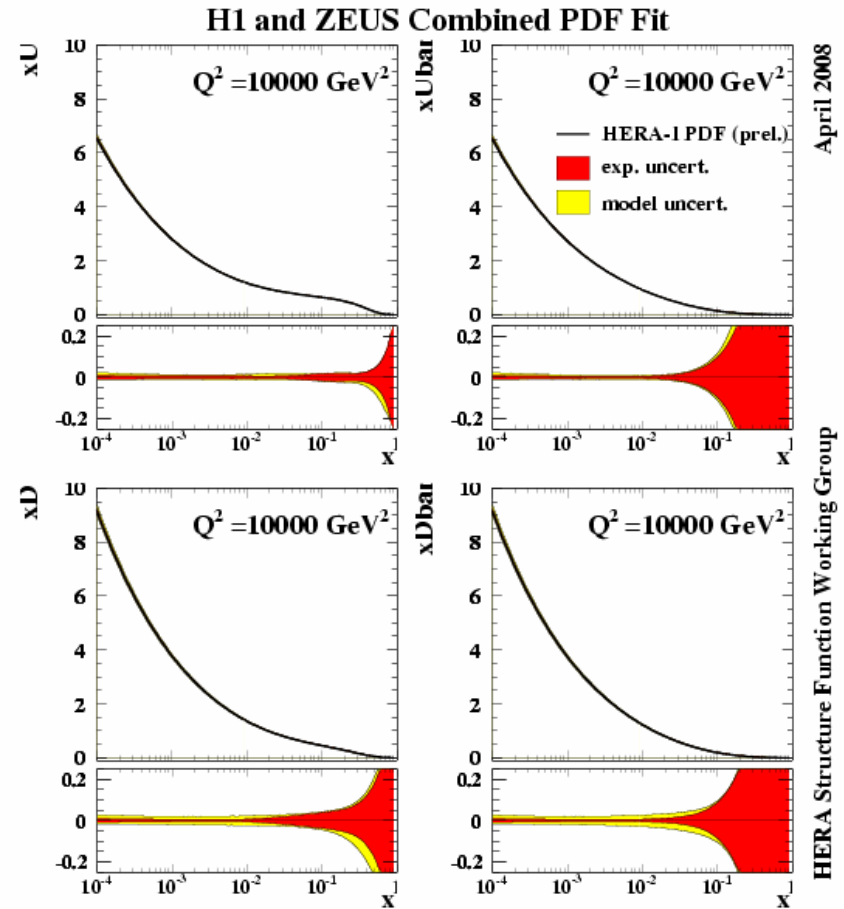
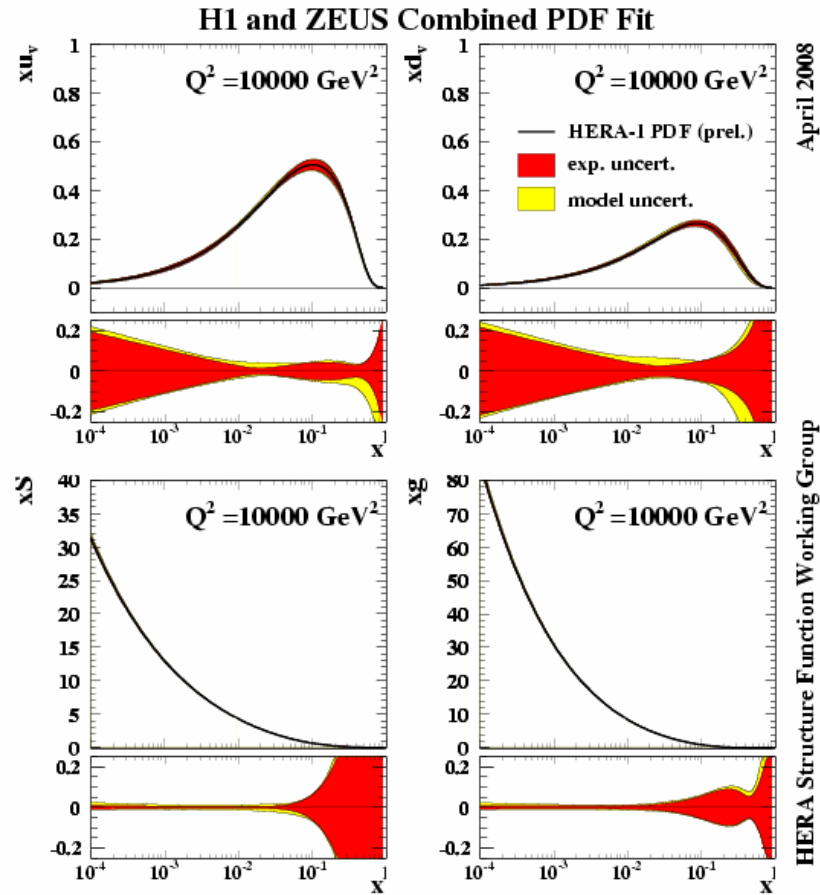
Total exp. uncertainty band (red); model uncertainties (yellow)
 $-f_s$ dominates model uncert. on sea; Q_0^2 & Q_{min}^2 dominate xg & xq_v

PDFs at $Q^2 = 100 \text{ GeV}^2$



Uncertainties decrease as Q^2 increases

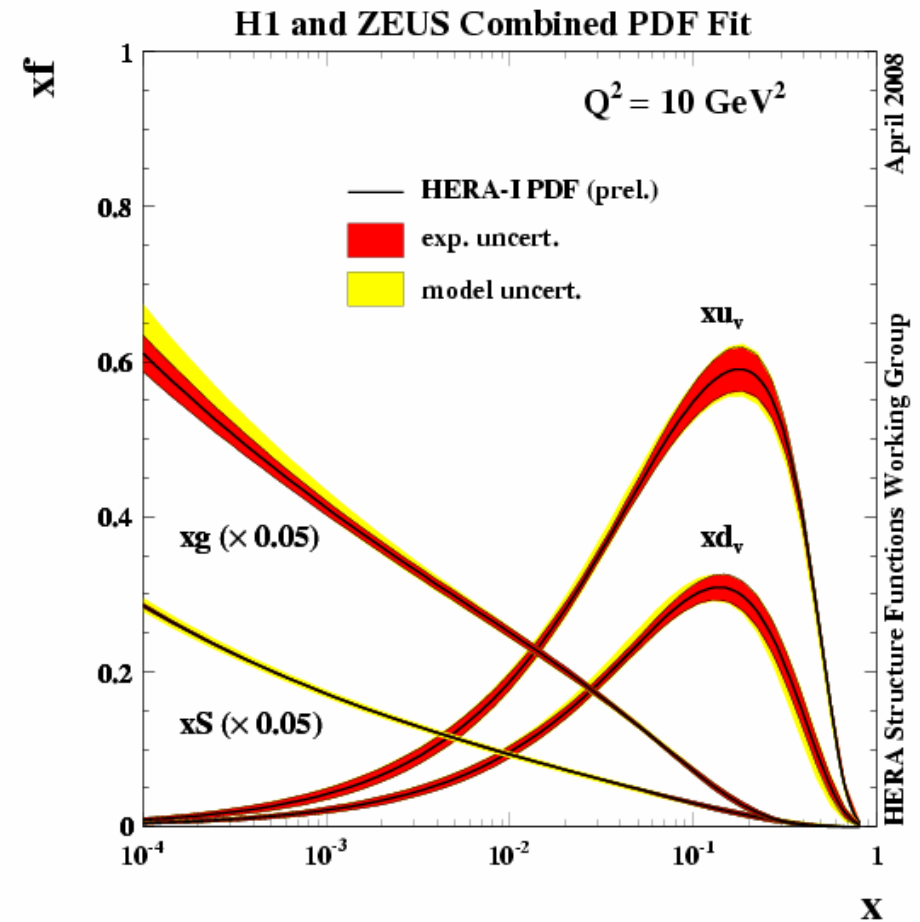
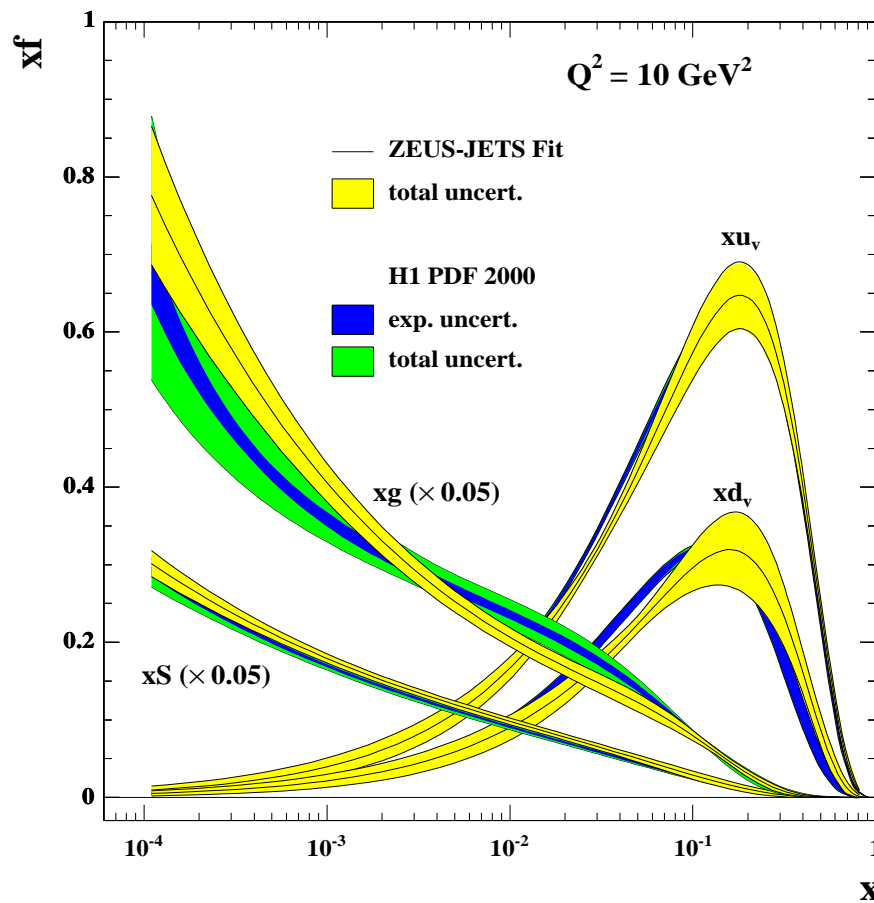
PDFs at $Q^2 = 10000 \text{ GeV}^2$



Scale relevant for the LHC – impressively small uncertainties
 see Cooper-Sarkar & Perez (talk at HERA-LHC May 08 w/shop, Indico confId = 27458)

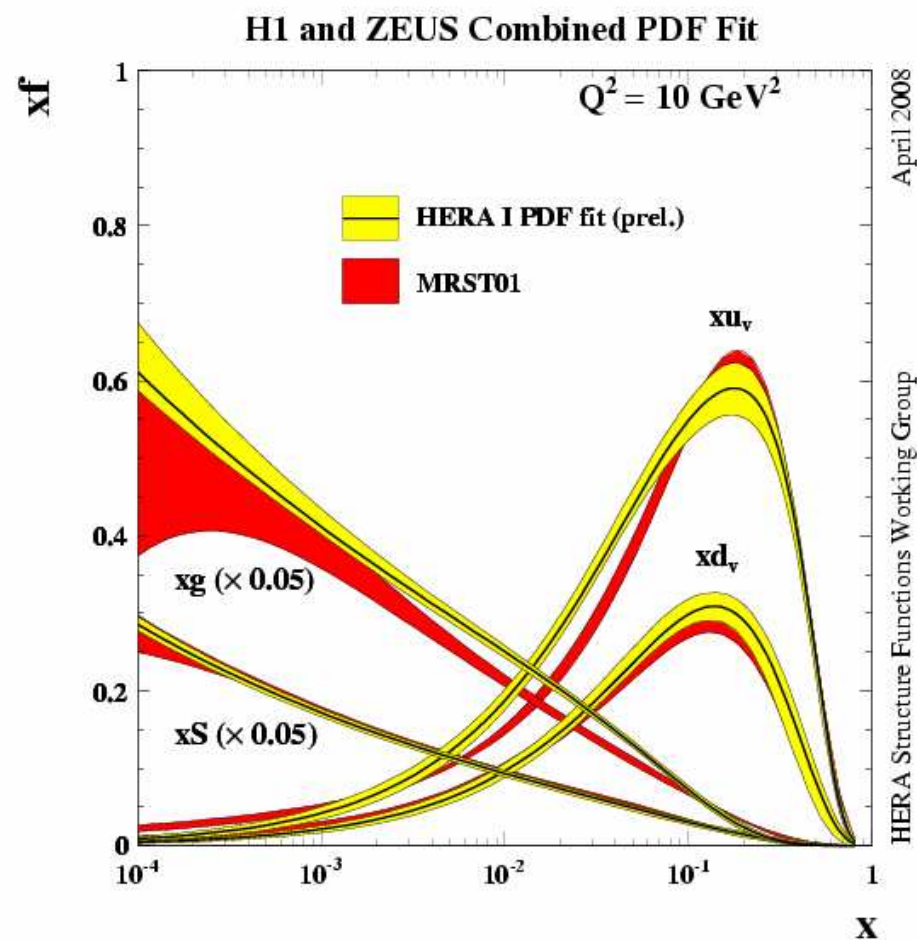
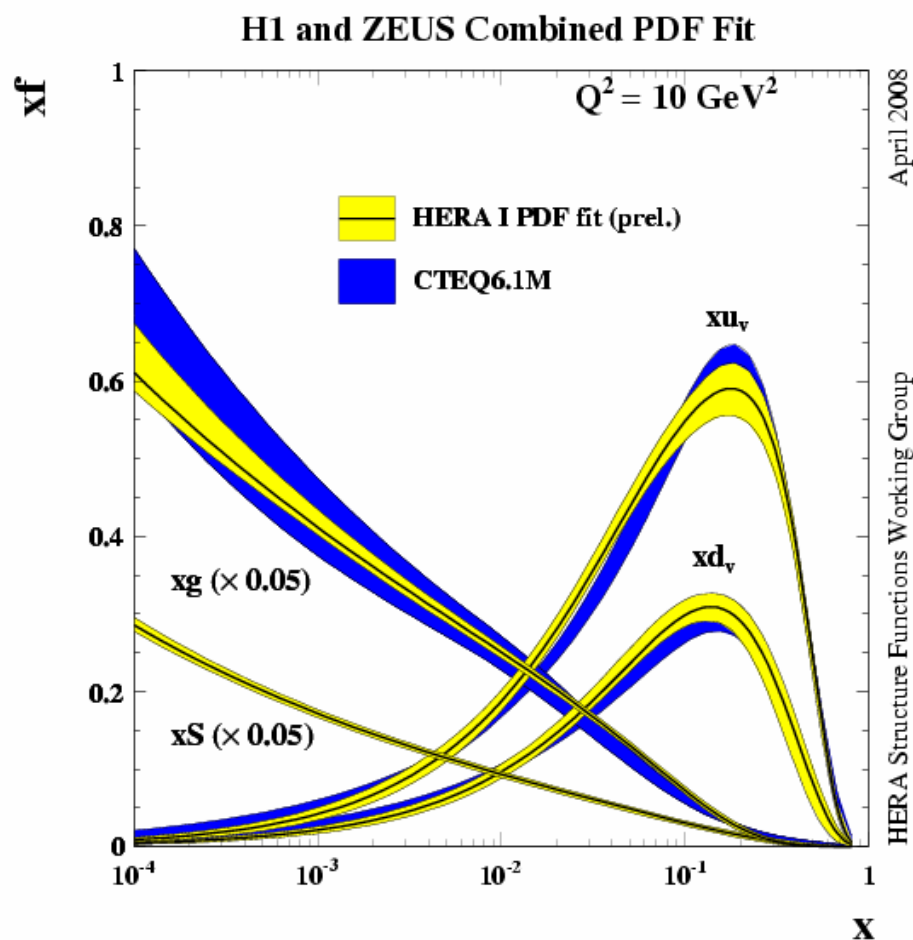
Comparisons I: with H1 & ZEUS fits

NB: H1PDF2k has α_s variation included in model error, ZEUS-Jets does not.



Improved precision and resolution of a discrepancy

Comparisons II: with CTEQ & MRST



Difference between HERAPDF0.1 and MRST01 xg at low x is due in part to parameterisation

LHAPDF

- ❖ Results shown here are those released at DIS08
- ❖ The intention is to release HERAPDF0.1 to LHAPDF ‘soon’
- ❖ Quite a few details are being checked and refined, e.g.
 - more work on flavour break-up of the sea
 - ditto on varying Q_0^2 and m_c
 - studies of xg at low and high x wrt other PDFs and other data
- ❖ None of the above have produced any significant differences from the results shown here
- ❖ There are also technical choices to be made, e.g.
 - input parameters plus evolution code?
 - or PDF values on (x, Q^2) grid?

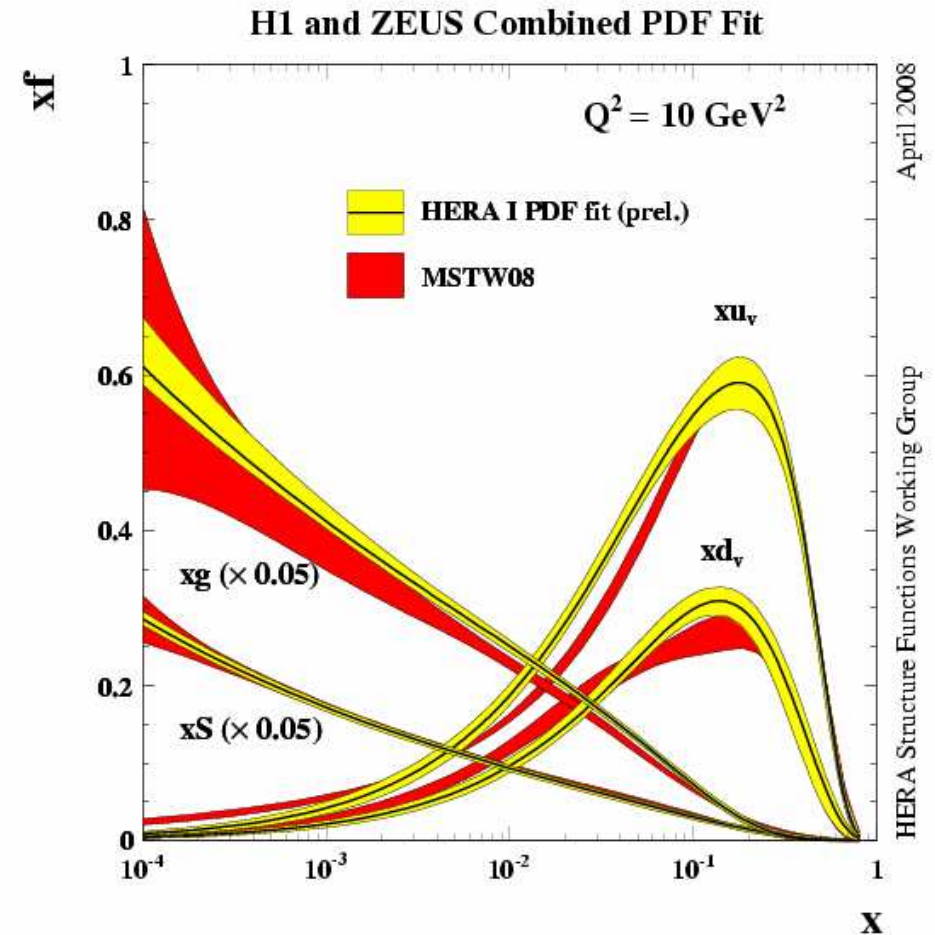
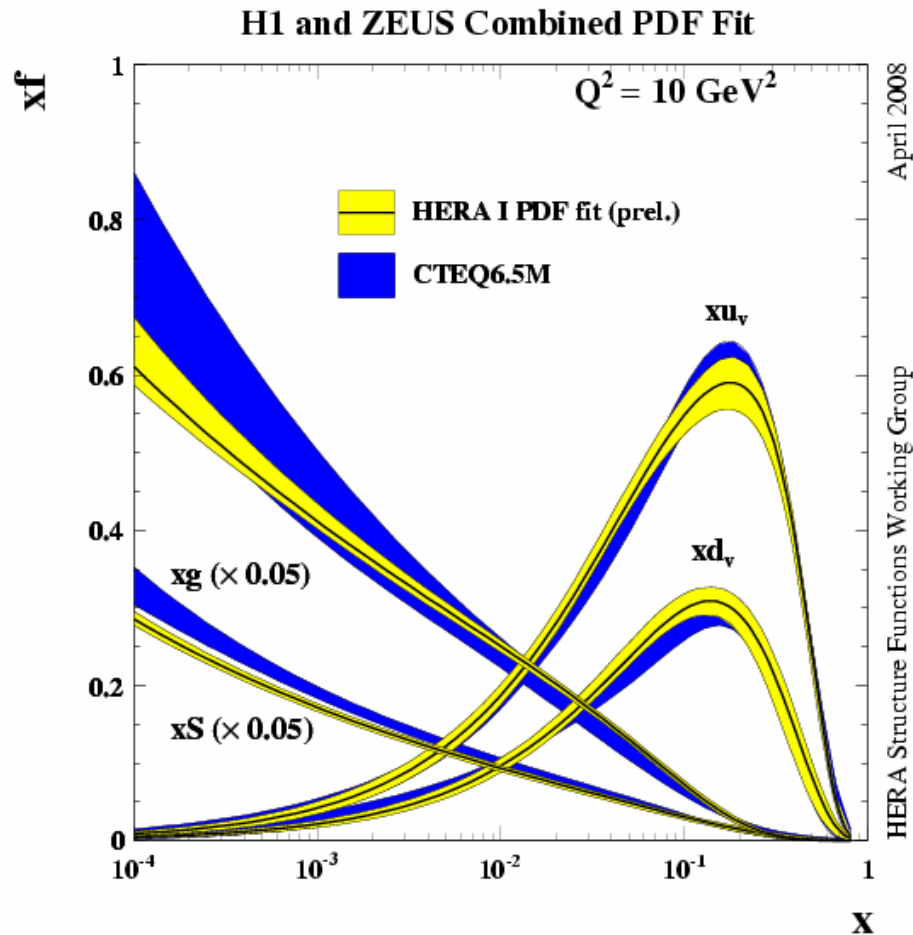
Summary (PDF fit)

- ❖ The improved precision of the combined HERA-I is reflected in the improved precision of the HERAPDF0.1 fit
- ❖ Experimental and fit-model uncertainties have been studied and allowed for
- ❖ Differences between H1PDF2k and ZEUS-Jets understood and resolved
- ❖ Note that the HERA fit parameterisation is ‘minimal and optimised’ in form and number of parameters
 - does not require target mass corrections
 - does not require heavy target or deuteron corrections

This is the just the start of the ‘combined HERA data’ programme

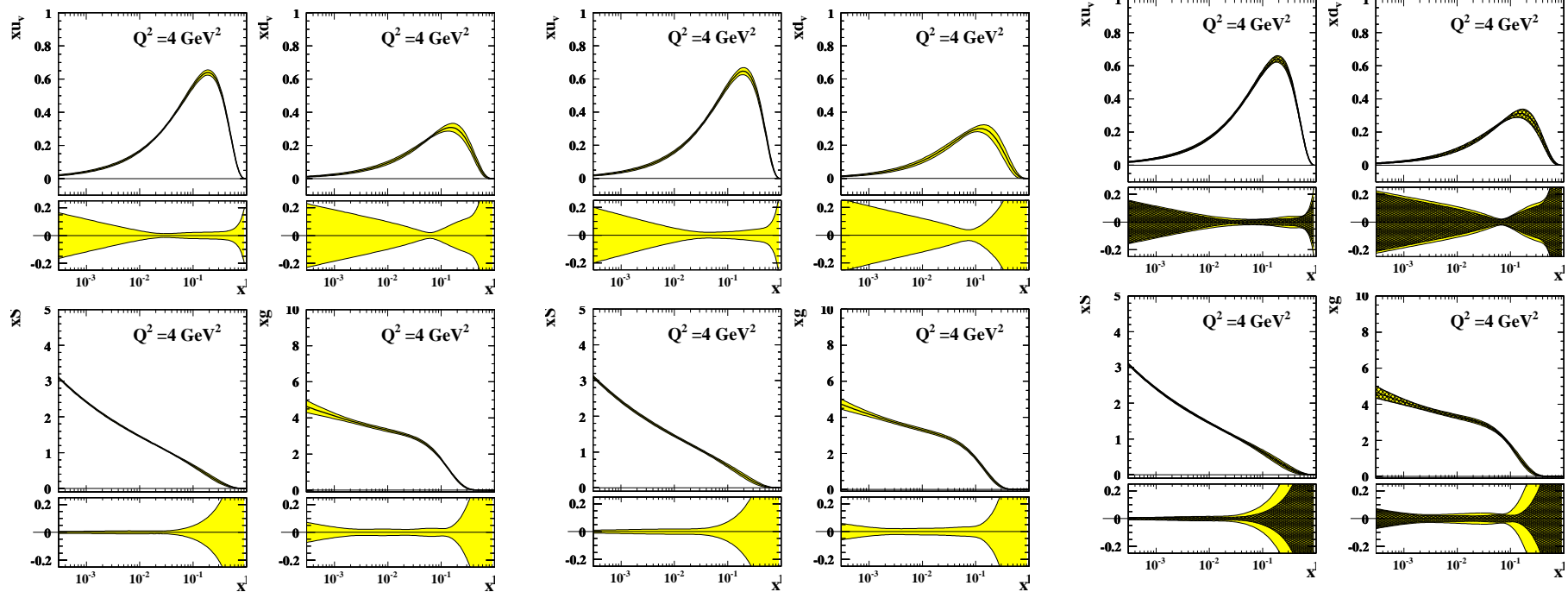
EXTRAS

Compare to CTEQ and MRST analyses: newer



Note MSTW08 is as yet unpublished
– this is a pre-release

Different error treatments

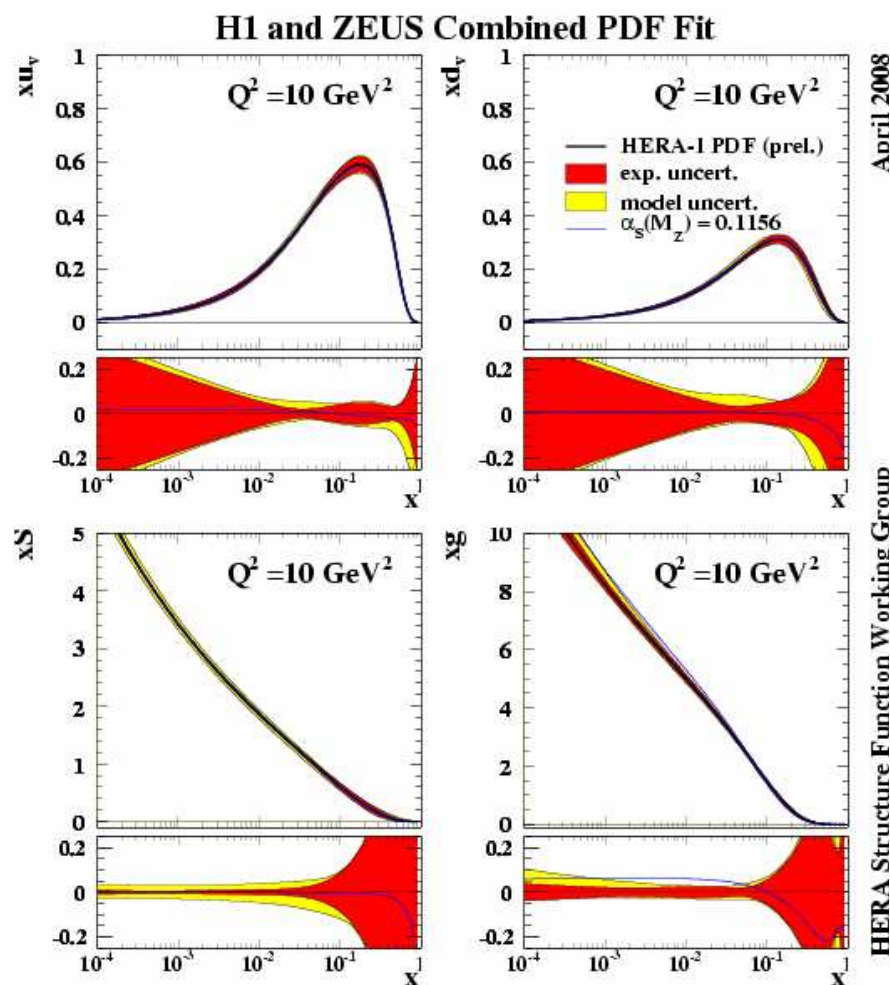


47 systematic errors
added to statistical
quadratically $\chi^2=428.0$

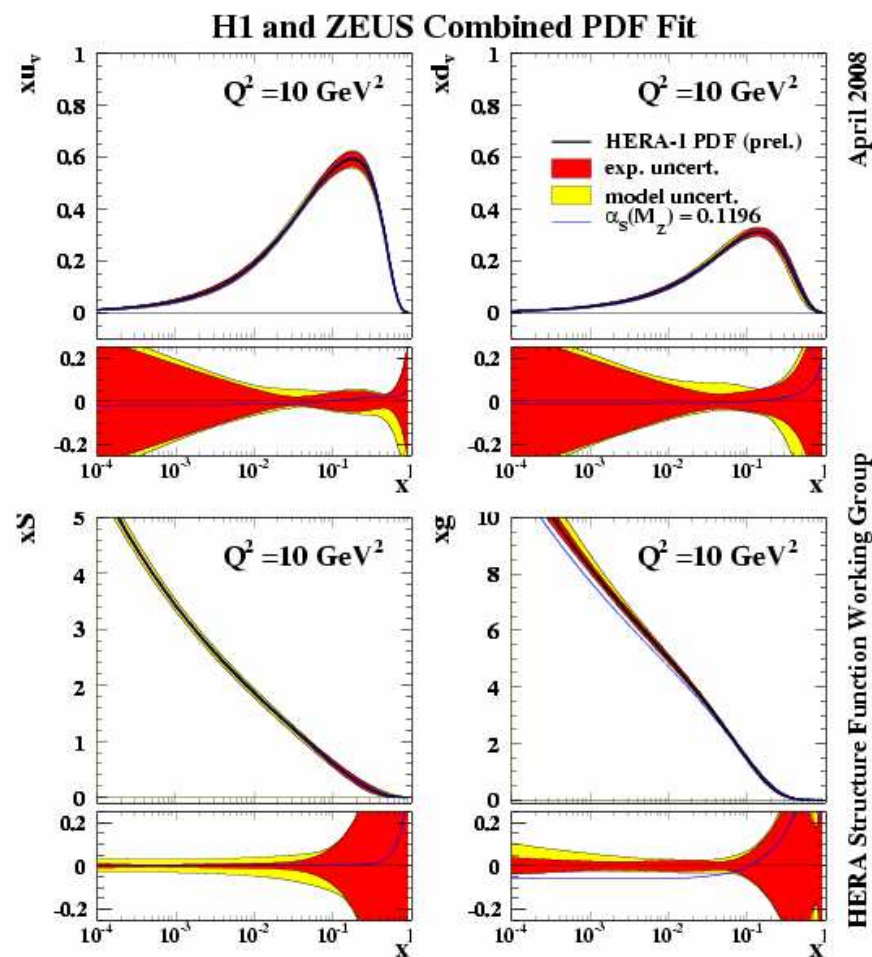
47 systematic errors
treated by Hessian
method $\chi^2=553.1$

43 original sources of
systematic errors added
to statistical quadratically
and 4 procedural errors
Offset $\chi^2=476.7$

Varying α_s



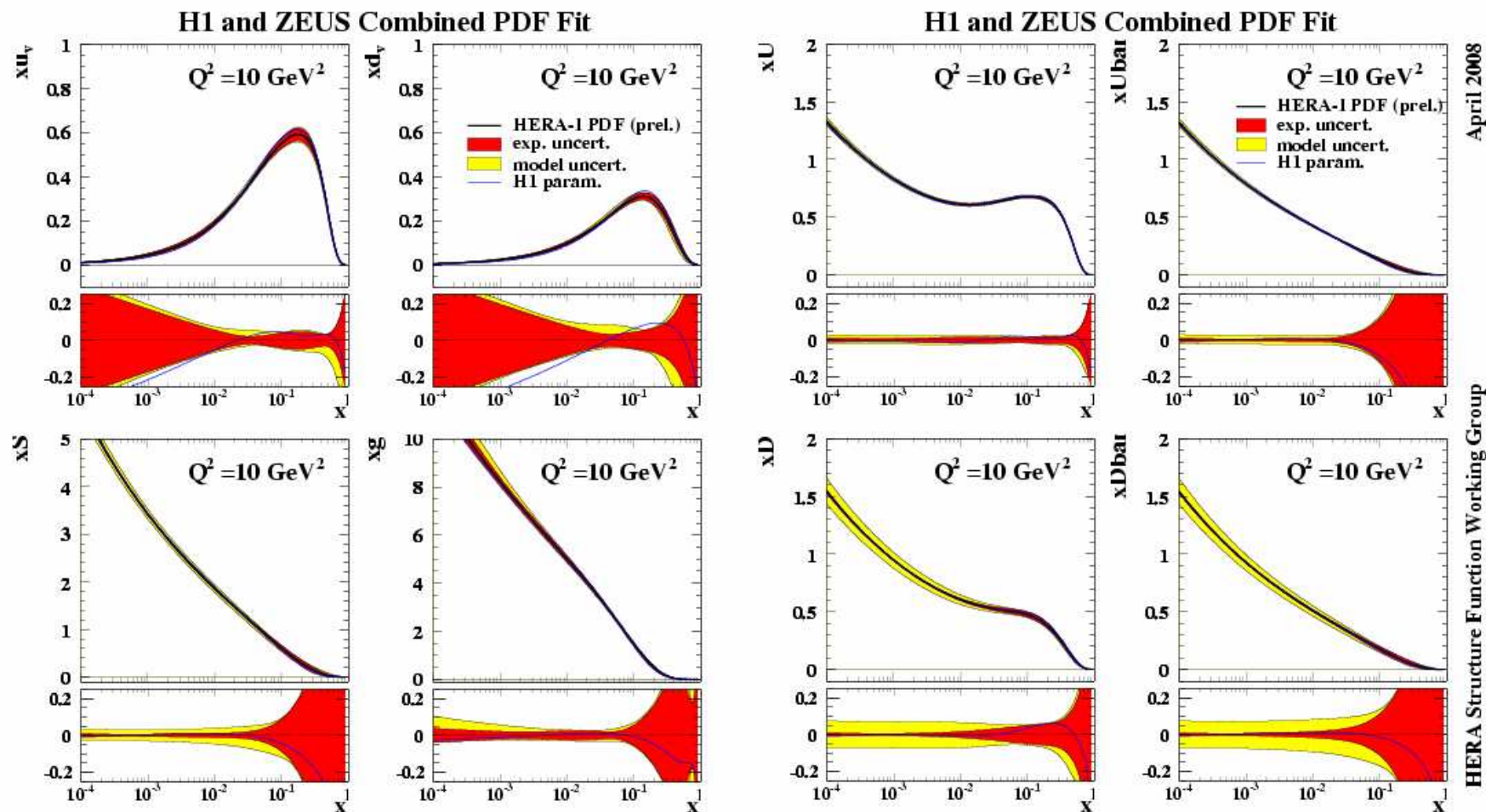
$\alpha_s = 0.1156$



$\alpha_s = 0.1196$

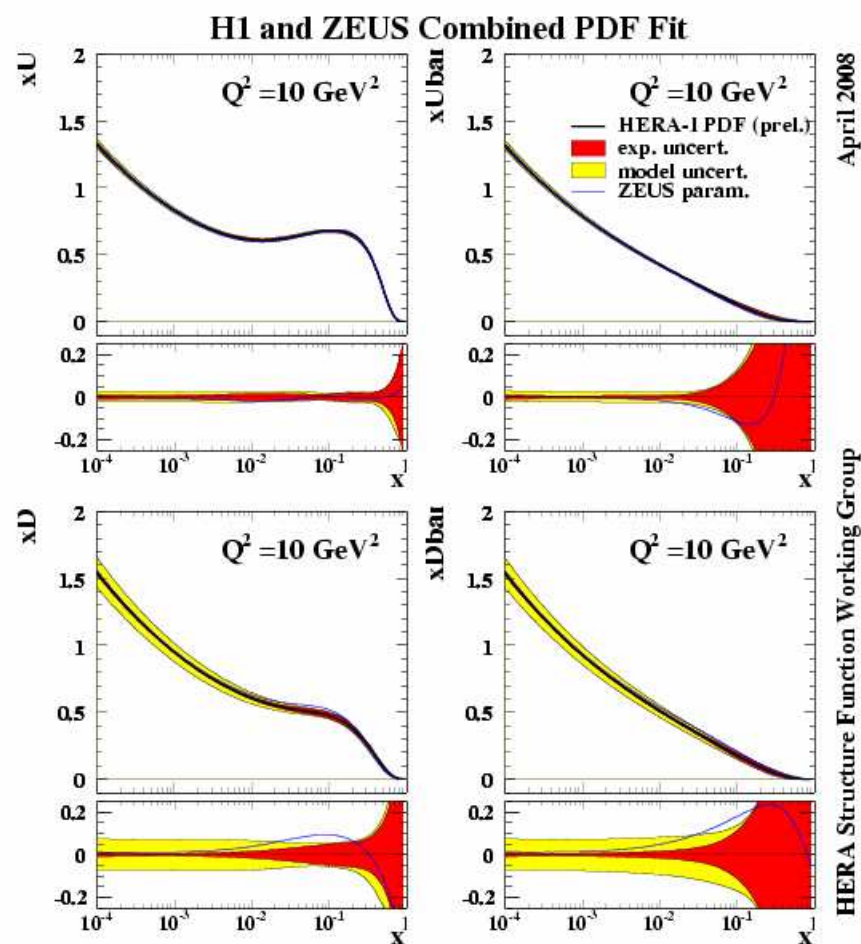
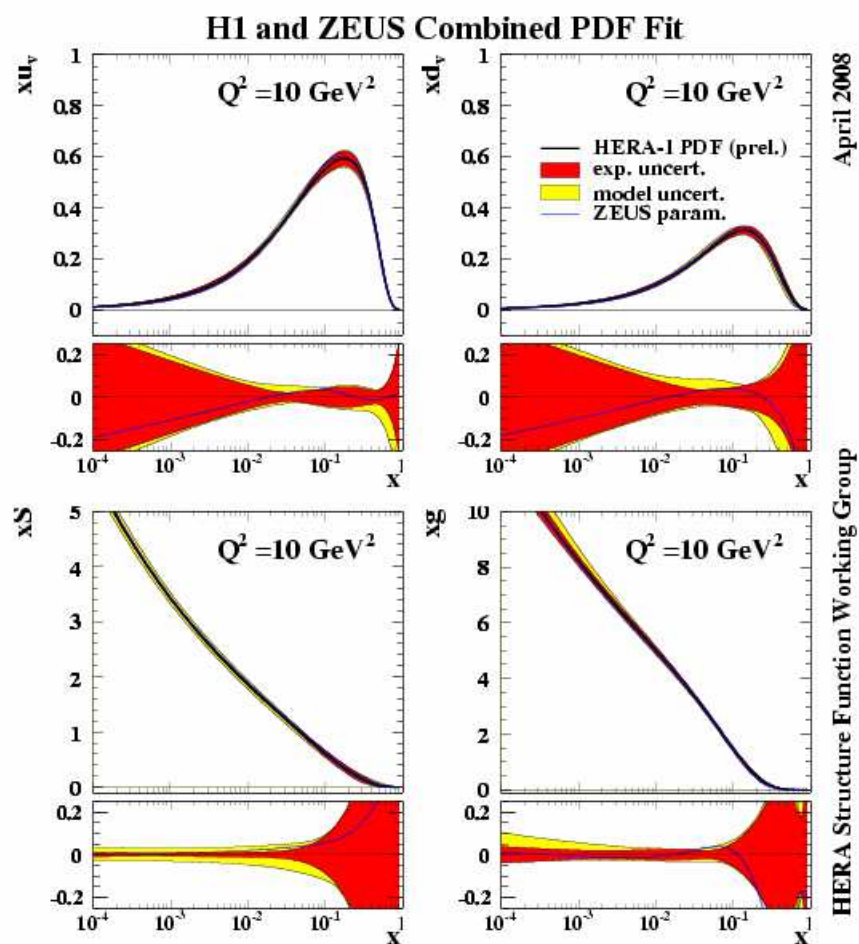
Variation is (just) outside the gluon error band

Variation: H1 style parameterisation



Central HERAPDF0.1 fit compared to H1 style parameterisation (optimised)
Marginally outside error bands for valence quarks at low x

Variation: ZEUS style parameterisation



Central HERAPDF0.1 fit compared to ZEUS style parameterisation (optimised)
 just inside error bands if model uncertainty included