

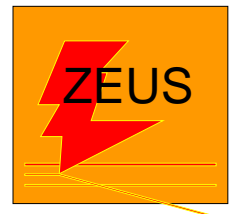
# Heavy Quark production at HERA and Heavy Quark contributions to the Proton Structure Function

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on behalf of the ZEUS and H1 Collaborations

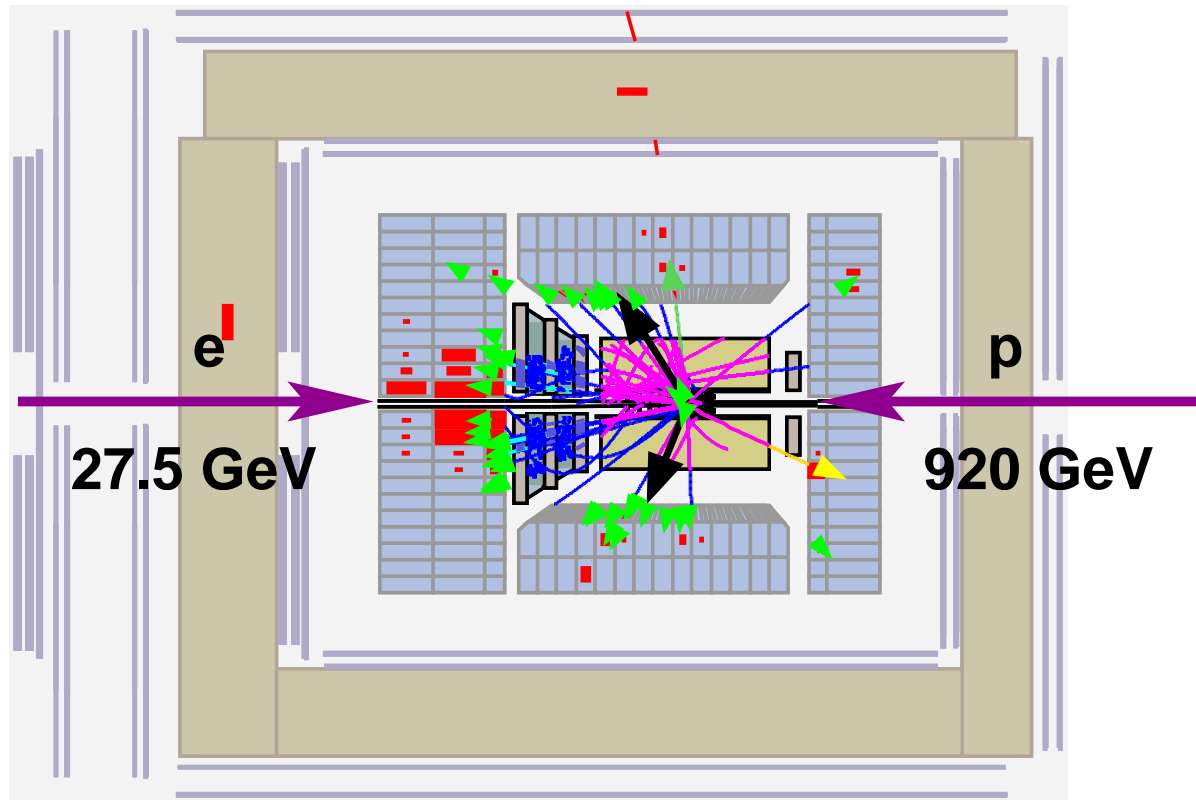
- Introduction
- Heavy quark measurement methods
- Structure functions  $F_2^{cc}$  and  $F_2^{bb}$



Lake Louise Winter Institute 2008  
Lake Louise, 02/23/2008



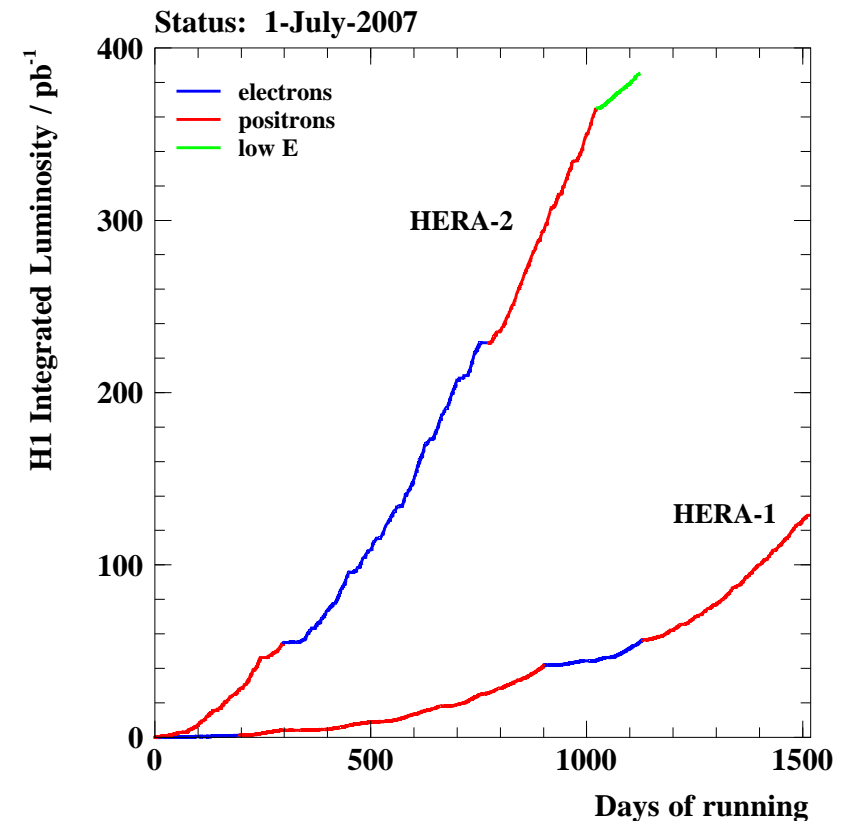
# *ep*-collisions at HERA



|                                  |                |
|----------------------------------|----------------|
| <i>ep</i> center of mass energy: |                |
| <b>1992 - 1997</b>               | <b>300 GeV</b> |
| <b>1998 - 2007</b>               | <b>320 GeV</b> |
| 05/2007                          | 225 GeV        |
| 06/2007                          | 252 GeV        |

Integrated Luminosity (e.g. H1 on tape)

| Year                     | $e^+p$               | $e^-p$               |
|--------------------------|----------------------|----------------------|
| 96-00 ( <b>HERA I</b> )  | 124 pb <sup>-1</sup> | 22 pb <sup>-1</sup>  |
| 03-07 ( <b>HERA II</b> ) | 242 pb <sup>-1</sup> | 255 pb <sup>-1</sup> |
| 05/2007 (LER)            | 15 pb <sup>-1</sup>  |                      |
| 06/2007 (MER)            | 8 pb <sup>-1</sup>   |                      |



# Heavy Flavour production

Dominant process in  $ep$ -collisions: **Boson-Gluon-Fusion**

## Kinematic variables:

$Q^2 = -q^2$  photon virtuality, squared momentum transfer

$x = \frac{Q^2}{2Pq}$  Bjorken scaling variable

$y = \frac{Pq}{Pk}$  Inelasticity

## Two kinematic regimes:

- **Photoproduction ( $\gamma p$ ):**  
 $Q^2 < 1 \text{ GeV}^2$
- **Deep inelastic scattering (DIS):**  
 $Q^2 > 1 \text{ GeV}^2$

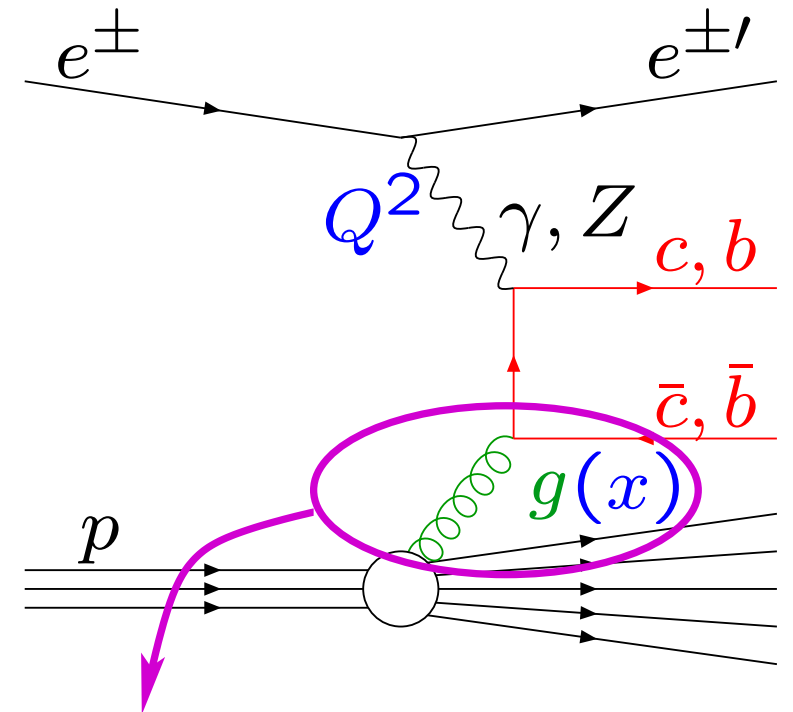
## Multiple scales:

$M_{c,b} \sim 1.5(4.75) \text{ GeV}$

$p_t^{c,b} \sim \text{typically few GeV}$

$Q^2 > 1 \text{ GeV}^2$  in DIS

$\Rightarrow$  different pQCD approaches



sensitive to gluon contents  
of the proton

# pQCD approximations

## Massive scheme:

- $c, b$  massive
- neglects  $\left[\alpha_s \ln \left(Q^2/m_{c,b}^2\right)\right]^n$
- scale  $m_{c,b}$

→  $c, b$  produced perturbatively  
(not part of the proton or photon)

( $\gamma p$ : Frixione et al, FMNR

DIS: Harris & Smith, HVQDIS)

## Massless scheme:

- $c, b$  massless
- resums  $\left[\alpha_s \ln \left(Q^2/m_{c,b}^2\right)\right]^n$
- scale  $Q^2, p_t$

→  $c, b$  also in proton and photon

( $\gamma p$ : Kniehl et al )

## Variable Flavour Number Scheme (VFNS):

- massive at small  $Q^2$
- massless at high  $Q^2$

(Cacciari et al)

# Charm tagging: $D^* \rightarrow K\pi\pi$ in DIS

## Golden decay mode

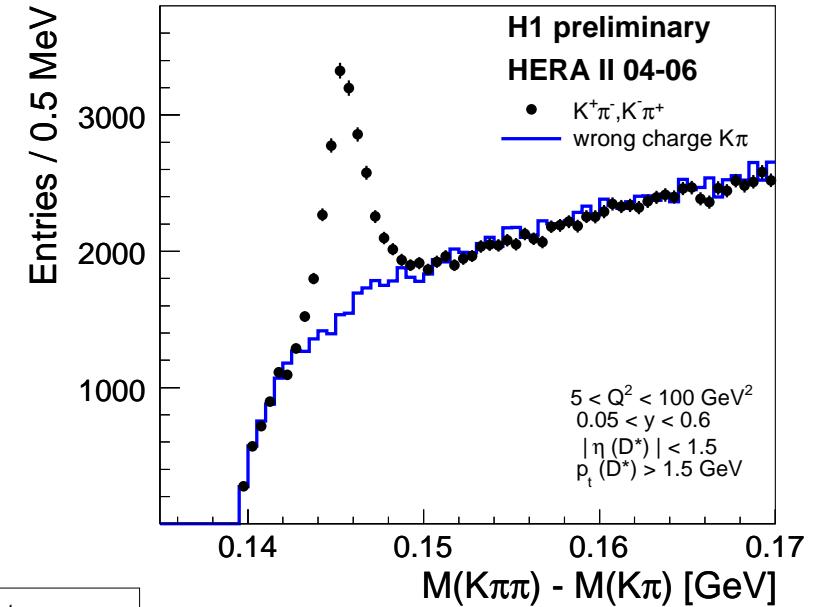
tagged by invariant mass  $M(K\pi)$

and  $\Delta M = M(K\pi\pi) - M(K\pi)$

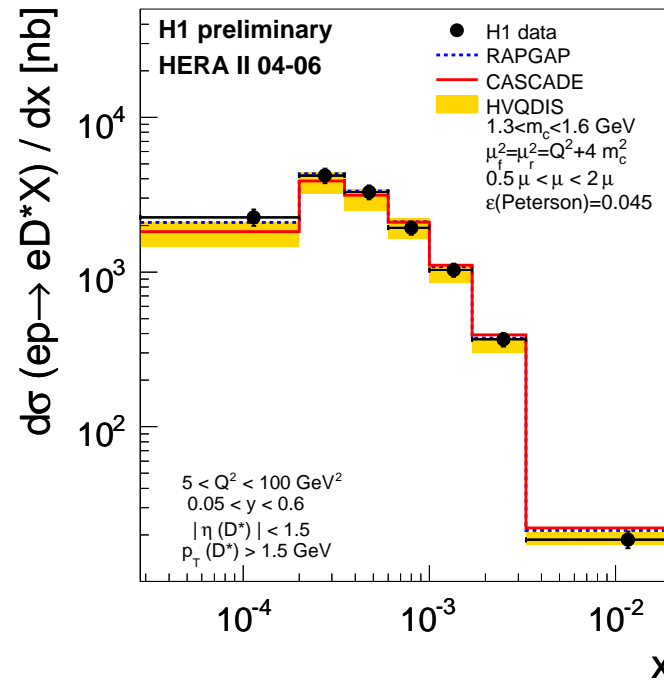
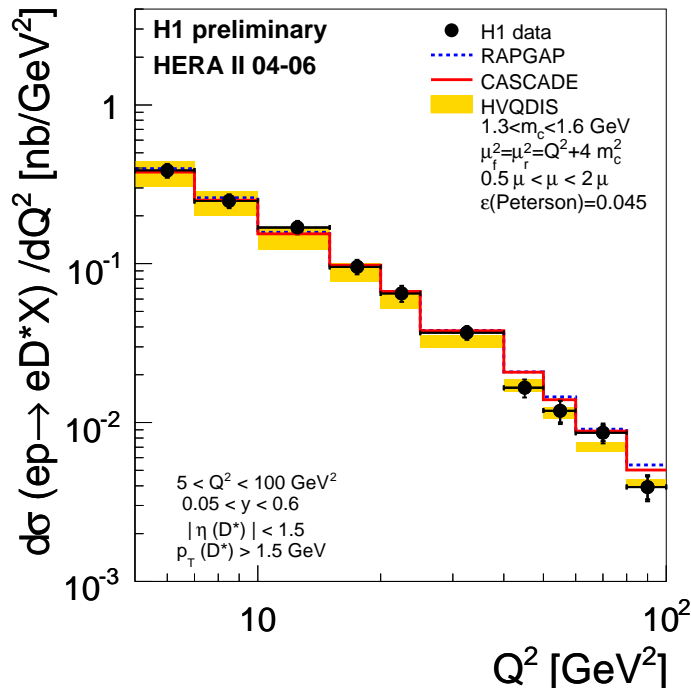
data and MC agree for

LO+parton shower (RAPGAP, CASCADE)

as well as for NLO (HVQDIS)



## Visible $D^*$ cross section



$$5 < Q^2 < 100 \text{ GeV}^2$$

$$0.05 < y < 0.6$$

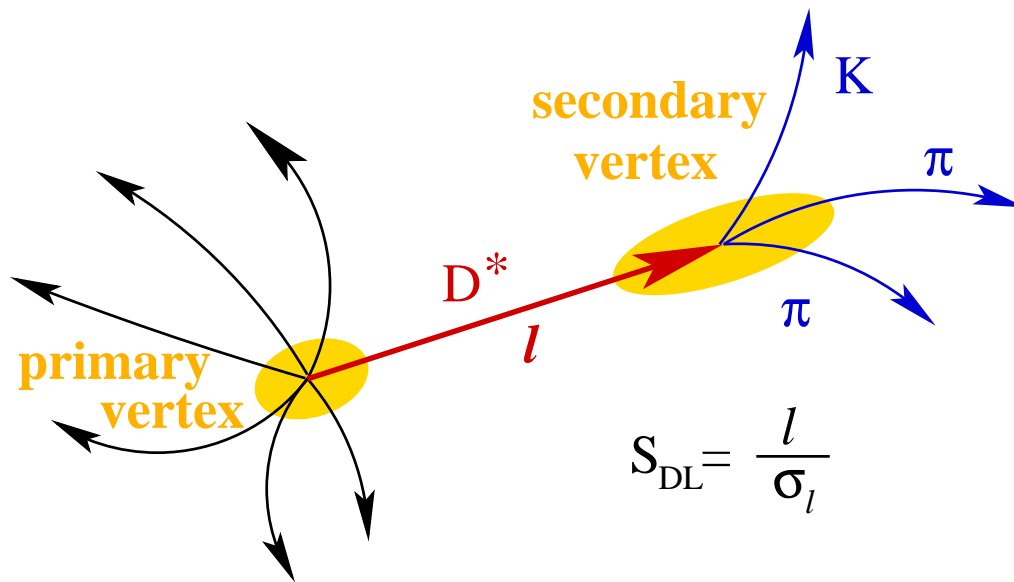
$$p_t(D^*) > 1.5 \text{ GeV}$$

$$|\eta(D^*)| < 1.5$$

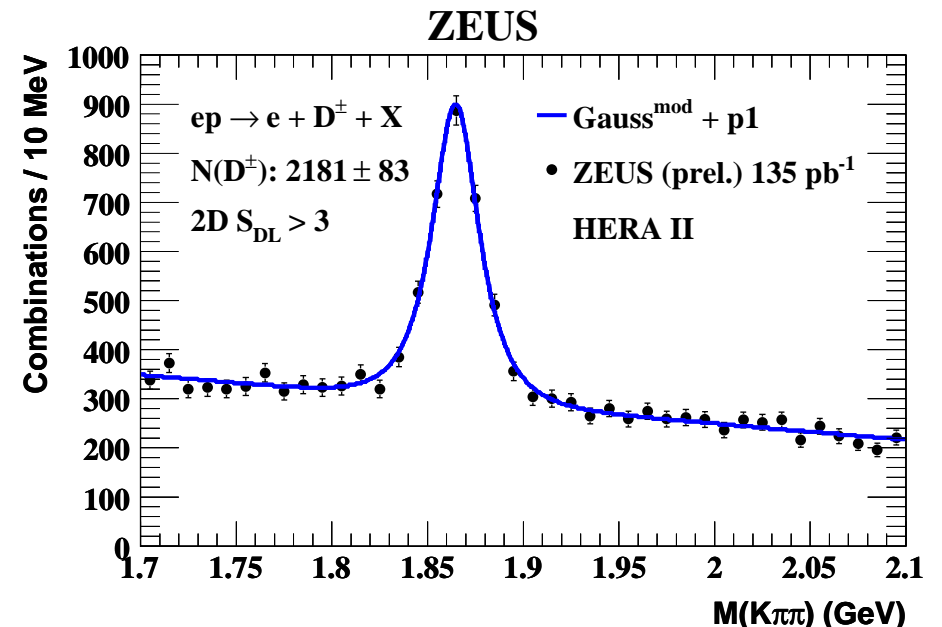
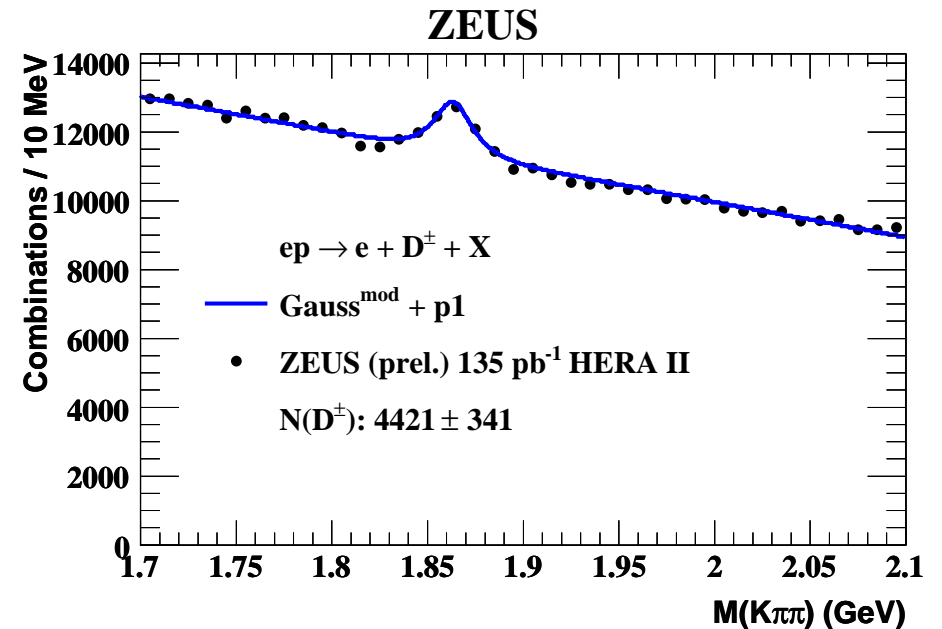
# Charm tagging: $D^+ \rightarrow K^- \pi^+ \pi^+$

## Long lifetime of $D^+$

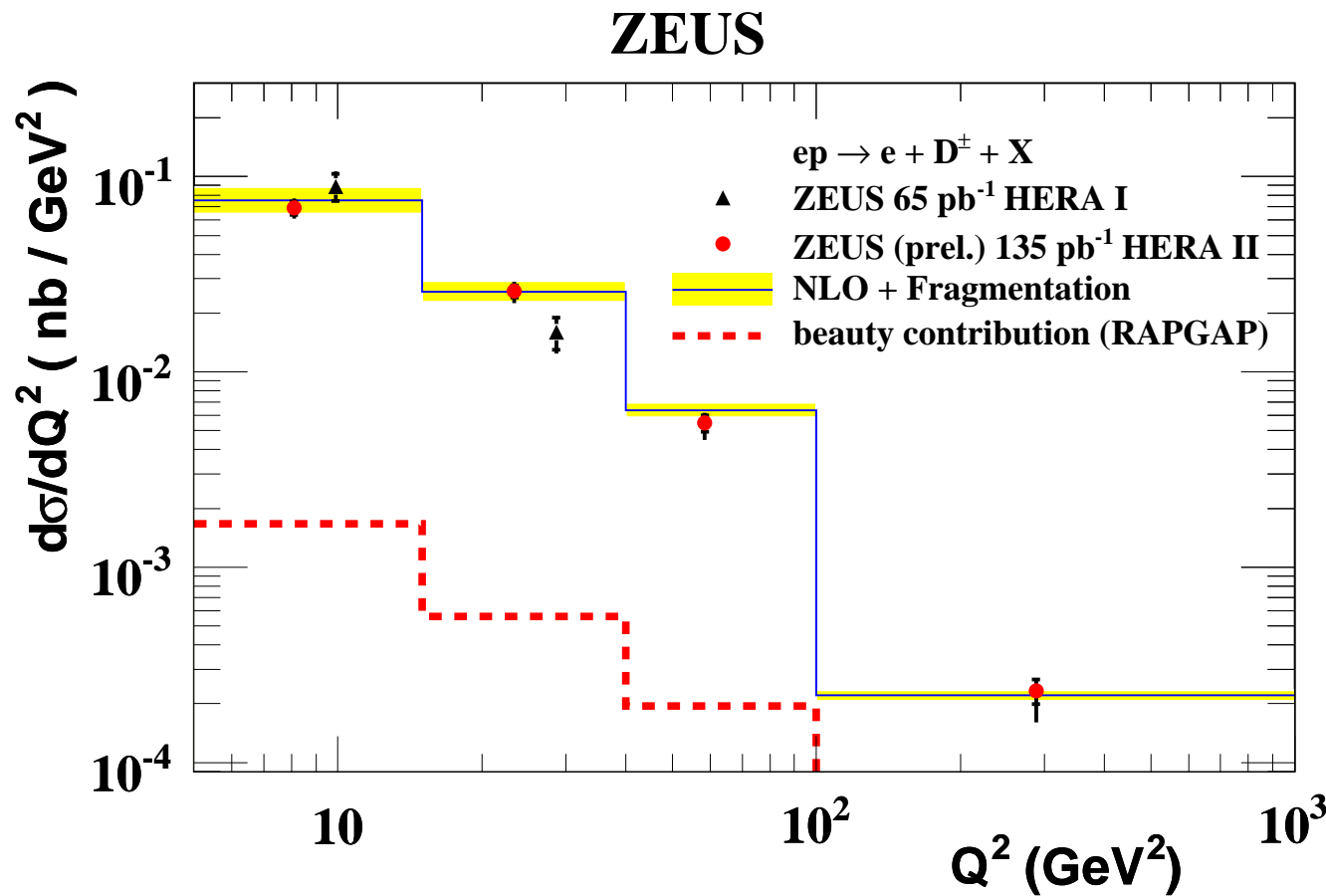
→ improved S/N ratio by cutting on the significance of the decay length (new method for HERA II)



Reduction of the statistical error from 7.7% to 3.8%



# $D^+ \rightarrow K^- \pi^+ \pi^+$ in DIS



- only 30% of available data used yet
- agreement between HERA I and HERA II measurements (different analysis methods)
- for some kinematic ranges error dominated by NLO uncertainty

Good description of data by NLO QCD  
(HVQDIS)

$$1.5 < Q^2 < 1000 \text{ GeV}^2$$

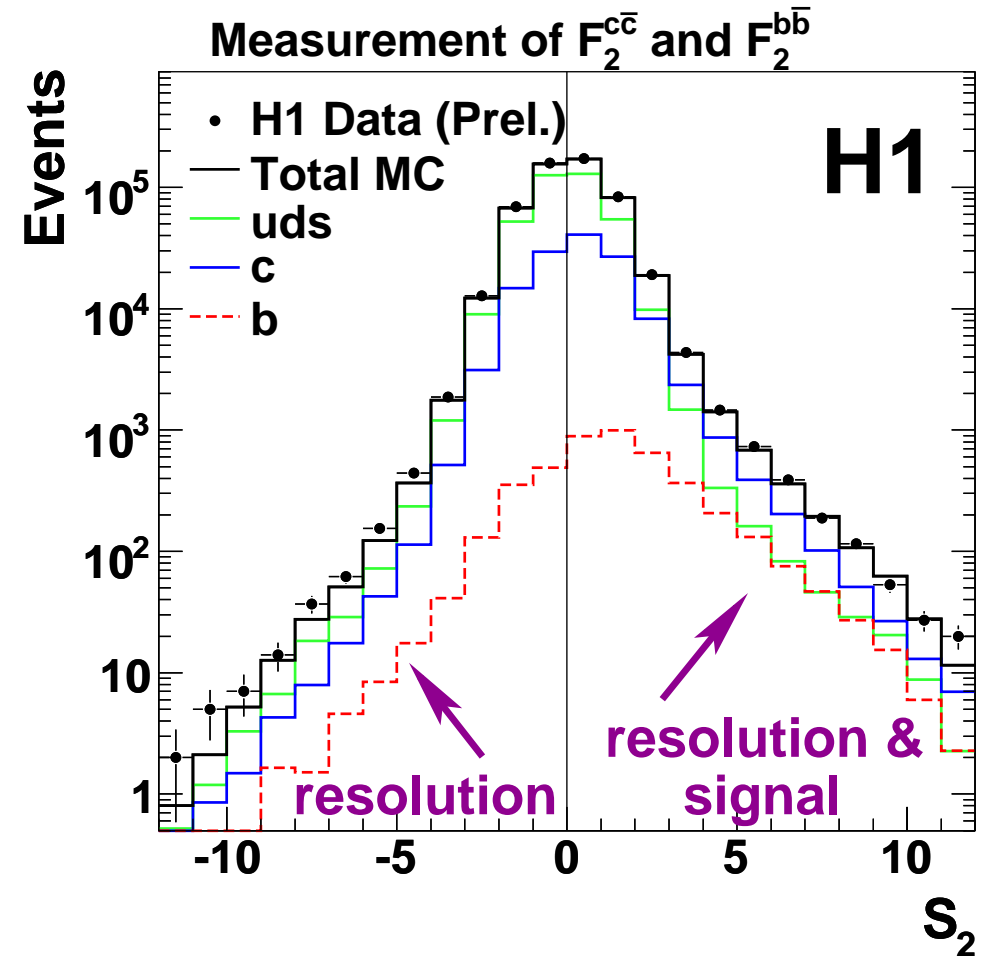
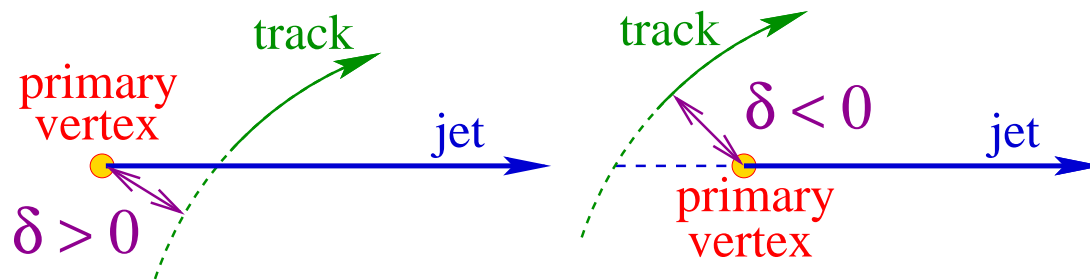
$$0.02 < y < 0.7$$

$$p_t(D) > 3 \text{ GeV}$$

$$|\eta(D)| < 1.6$$

# Inclusive Impact Parameter tagging

- inclusive method:  
use all tracks ( $p_t > 500$  MeV)  
with vertex detector information
- study significance of the  
(signed) impact parameter  
 $S = \delta/\sigma(\delta)$
- separation of beauty, charm  
and light quarks



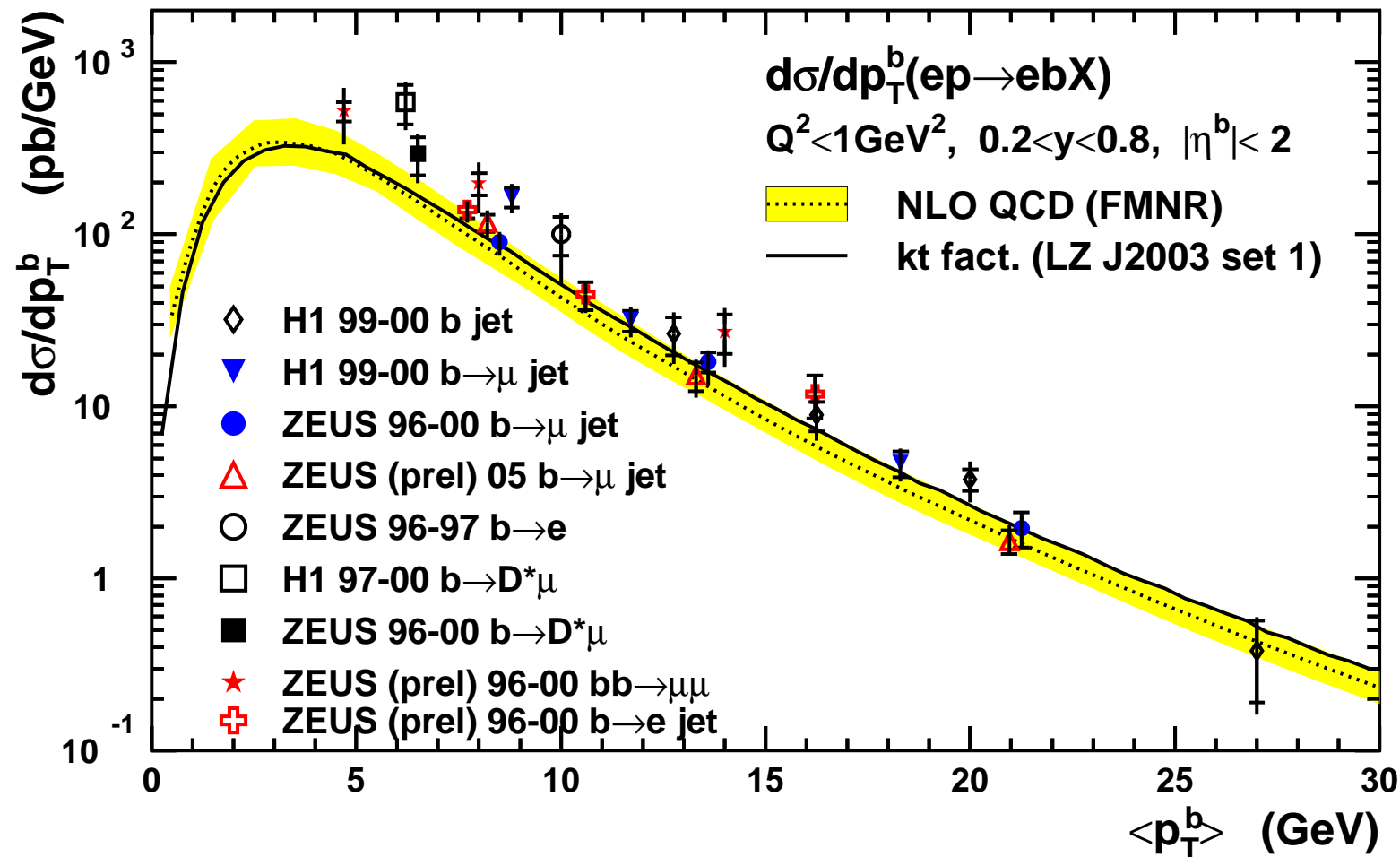
$S_2$ : track with 2<sup>nd</sup> highest significance

$$12 < Q^2 < 650 \text{ GeV}^2 \quad p_t^{\text{track}} > 0.5 \text{ GeV}$$

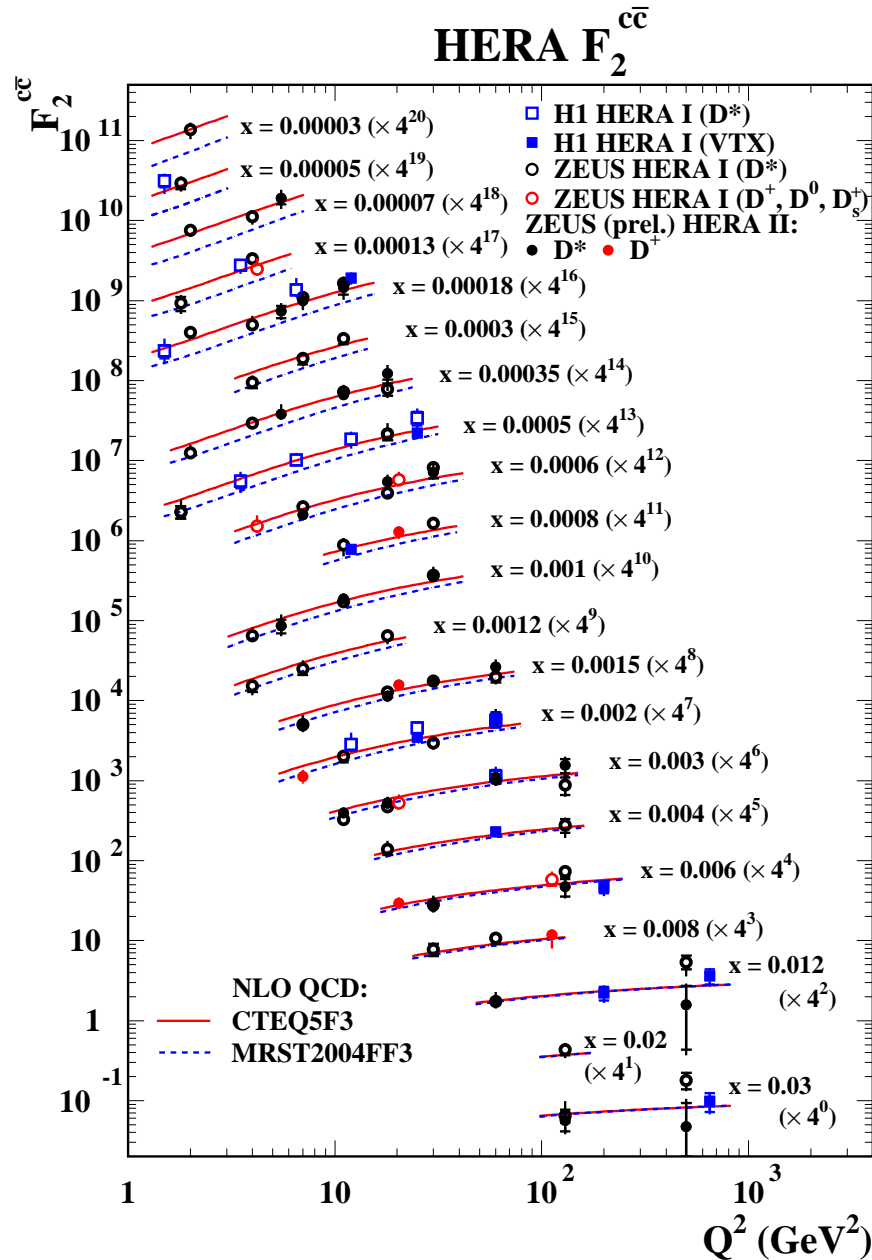
$$0.0002 < x < 0.0032$$

# Beauty photoproduction

## HERA



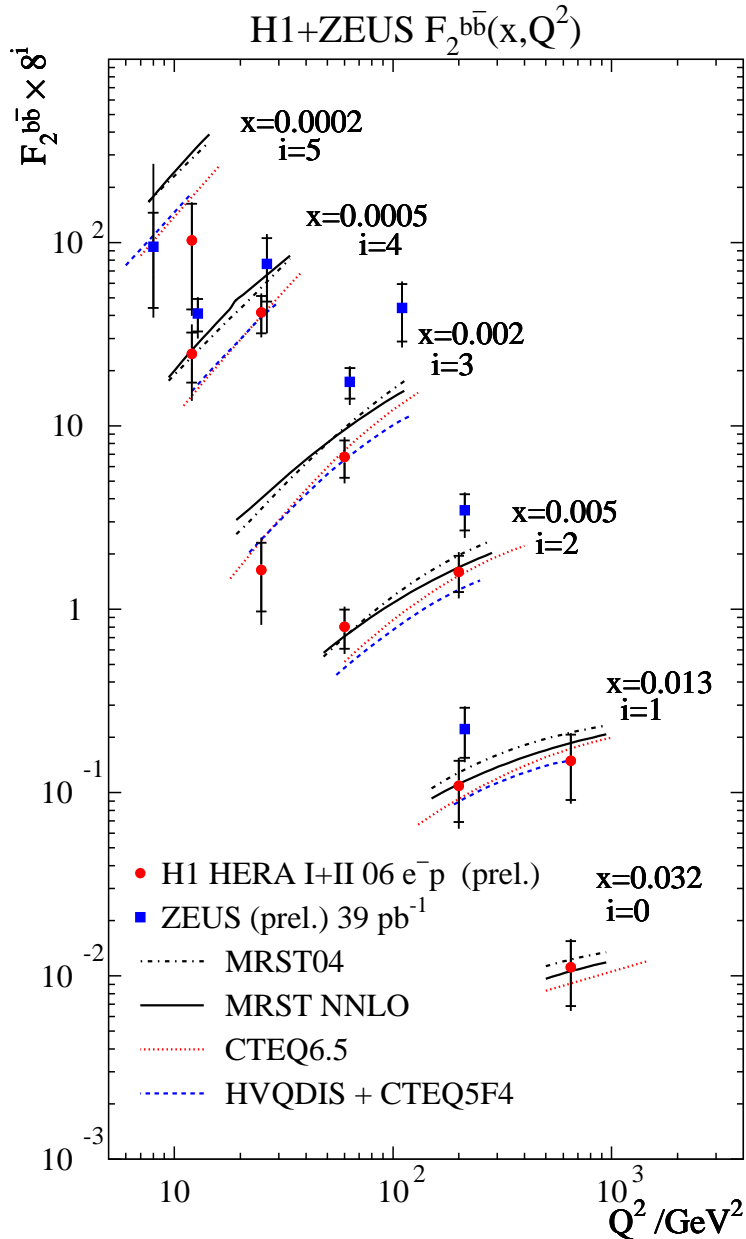
cross sections for  $b$ -production extrapolated using NLO calculations  
data at upper edge of NLO prediction



$$\frac{d^2\sigma^{ep \rightarrow c\bar{c}X}}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} \left( Y_+ F_2^{c\bar{c}}(x, Q^2) + \dots \right)$$

$$Y_+ = 1 + (1 - y)^2$$

- all available measurements in good agreement
- scaling violation observed at low  $x$
- PDF's differ at low  $x$
- good agreement with NLO



## First measurements of $F_2^{b\bar{b}}(x, Q^2)$ :

- rise with gluon density  
(towards smaller  $x$  and higher  $Q^2$ )
- MRST04 and CTEQ6.5 predictions differ by a factor of 2
- experimental errors too large to distinguish between theories/PDFs
- data described by NNLO calculation within large statistical errors

analysis of full data set ongoing

# Summary

- Heavy Flavour production in  $ep$ -collisions: testing ground for
  - perturbative QCD calculations
  - gluon density in the proton (PDF's)
- Charm production:
  - high statistics
  - H1 and ZEUS using different analysis methods agree in the results
  - good description by NLO calculations
- Beauty production:
  - reasonable description within uncertainties
  - whole HERA data needed to reduce statistical uncertainties
- Structure functions  $F_2^{c\bar{c}}$ ,  $F_2^{b\bar{b}}$ :
  - data described well by predictions
  - charm data is sensitive to PDF's

looking forward to analyses using full HERA statistics

# Backup slides

# $F_2^{c\bar{c}}$ extraction: H1 and ZEUS

$$\frac{d^2\sigma^{ep\rightarrow c\bar{c}X}}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4x} \left\{ (1 + (1-y)^2) \underset{\text{dominant contri-}}{\underset{\text{bution to } \sigma}{F_2^{c\bar{c}}(x, Q^2)}} - y^2 \underset{\text{significant}}{\underset{\text{at high } y}{F_L^{c\bar{c}}(x, Q^2)}} + \dots x \underset{\text{significant}}{\underset{\text{at high } Q^2}{F_3^{c\bar{c}}}} \right\}$$

- ZEUS extracts  $F_2^{c\bar{c}}$  from D meson cross sections using HVQDIS to extrapolate to the full meson phase space:

$$F_{2,meas}^{c\bar{c}}(x_i, Q_i^2) = \frac{\sigma_{i,meas}(ep \rightarrow D^* X)}{\sigma_{i,theo}(ep \rightarrow D^* X)} \cdot F_{2,theo}^{c\bar{c}}(x_i, Q_i^2)$$

- H1 measures charm inclusively:

$$\tilde{\sigma}^{c\bar{c}}(x, Q^2) = \tilde{\sigma}(x, Q^2) \frac{P_c N_c^{MC}}{P_c N_c^{MC} + P_b N_b^{MC} + P_l N_l^{MC}} \cdot \delta_{BCC}$$

$P_{c,b,l}$  are the fractions of charm, beauty and light flavour from the fit and  $\tilde{\sigma}$  is the inclusive reduced cross section.

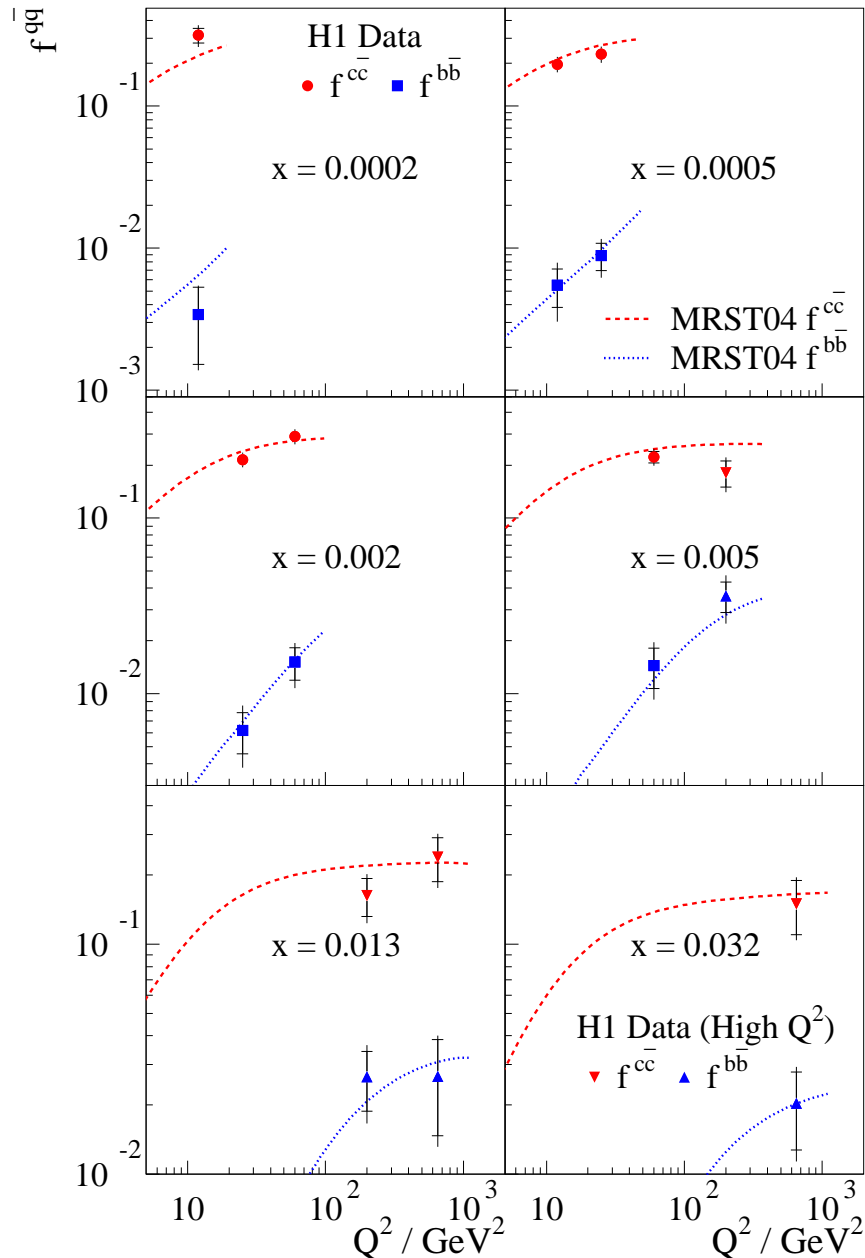
# PDF schemes and parameter

| PDF             | Order        | Scheme, Nf | $\mu^2$                           | $M_b$ ( GeV) |
|-----------------|--------------|------------|-----------------------------------|--------------|
| MRST04          | $\alpha_s^2$ | VFNS       | $Q^2$                             | 4.3          |
| MRST NNLO       | $\alpha_s^3$ | VFNS       | $Q^2$                             | 4.3          |
| CTEQ6.5         | $\alpha_s^2$ | VFNS       | $Q^2 + M^2$                       | 4.5          |
| HVQQDIS+CTEQ5F4 | $\alpha_s^2$ | FFNS, 4    | $\frac{1}{4} (p_t^2 + Q^2 + M^2)$ | 4.75         |
| CTEQ6HQ         | $\alpha_s^2$ | VFNS       | $Q^2 + M^2$                       | 4.5          |

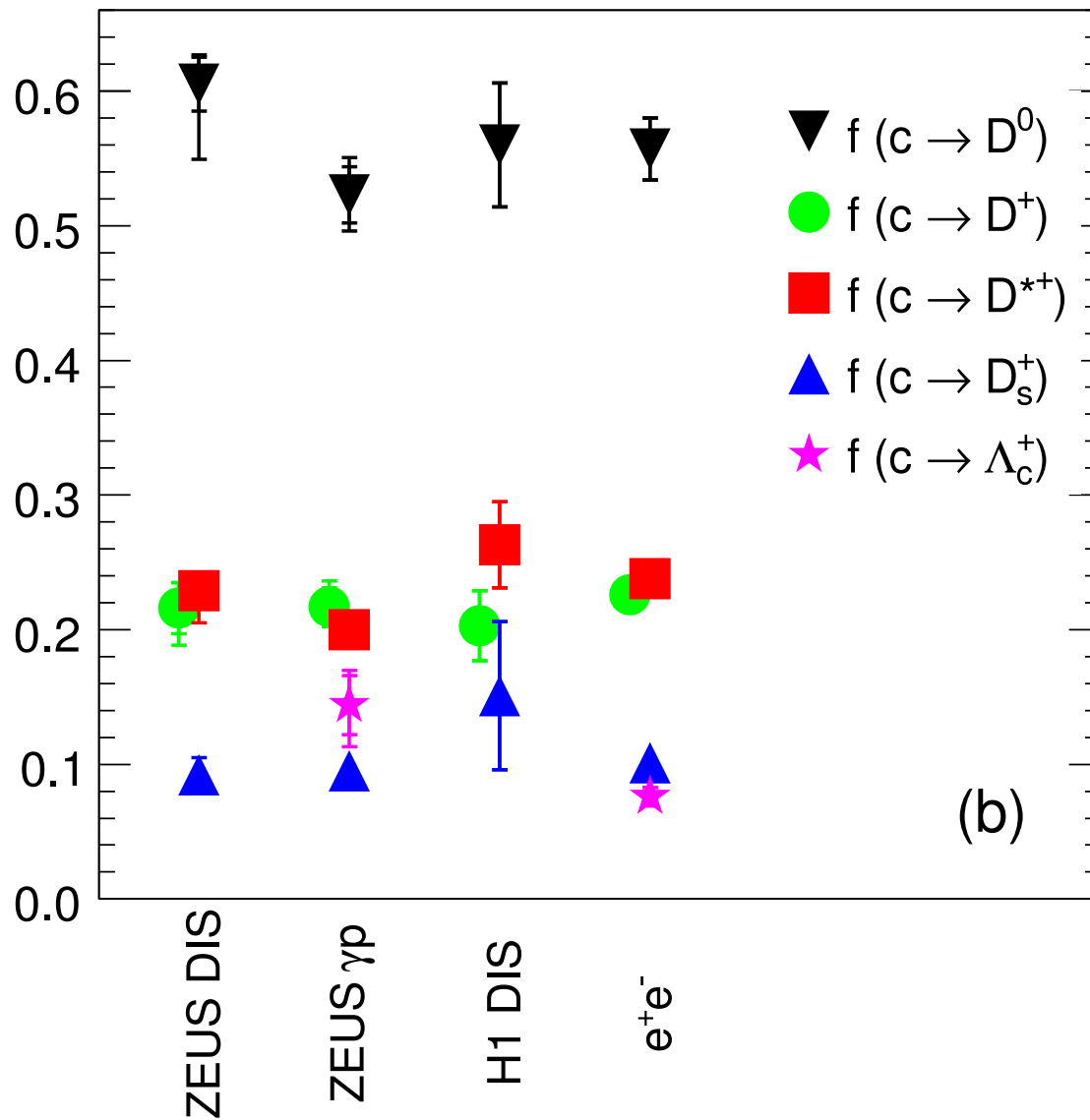
Theory predictions except HVQQDIS+CTEQ5F4  
provided by P. D. Thompson, hep-ph/0703103

charm and beauty contribution to  $F_2$ :

- large charm fraction up to  $\sim 30\%$
- small beauty fraction  $\sim \text{few } \%$
- reasonable agreement with NLO QCD prediction

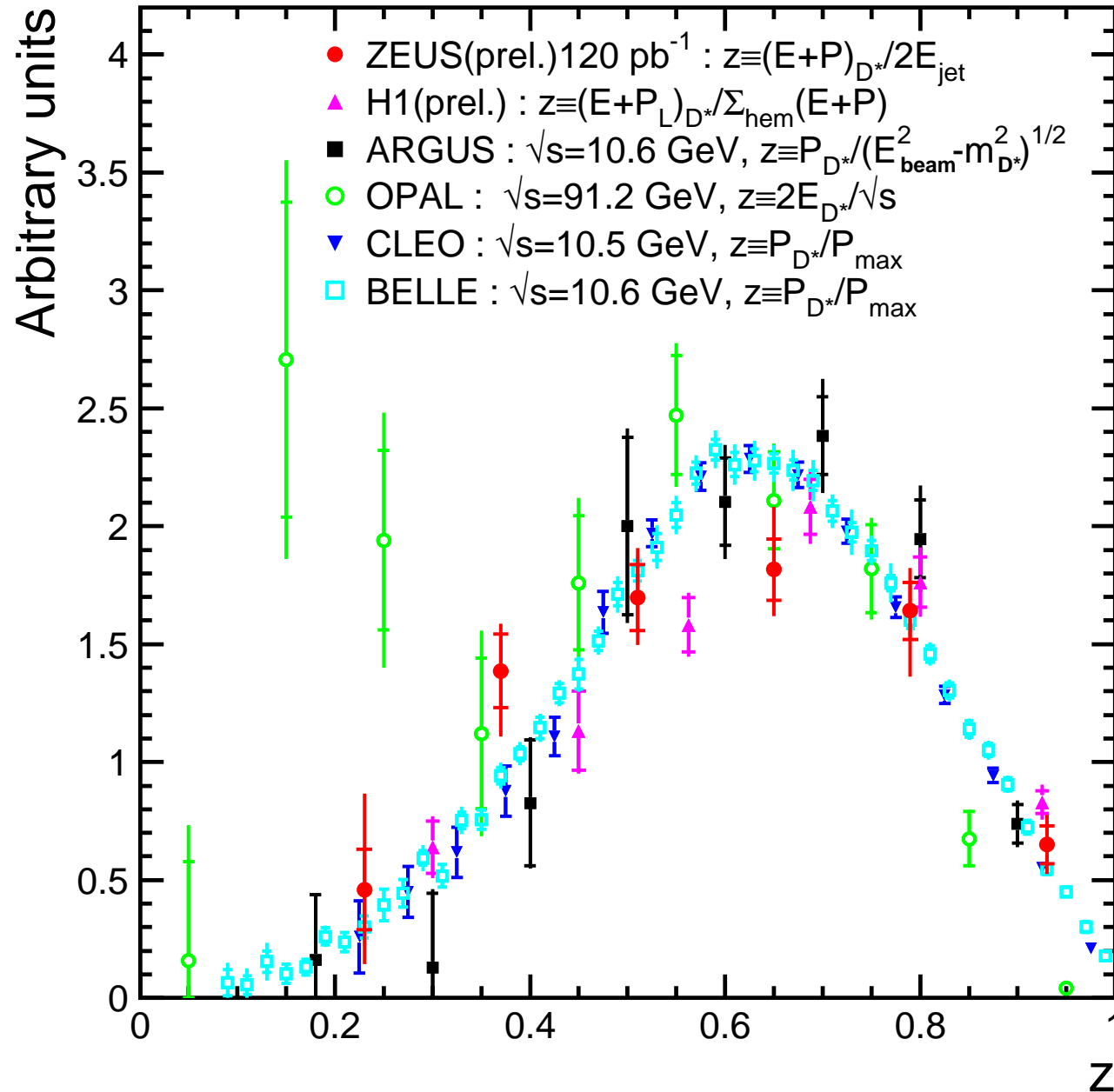


# Fragmentation fractions



- fraction of charm quarks hadronising as a particular  $D$  meson
- agreement between HERA and LEP experiments

# Fragmentation function



Energy transfer:

$$z = \frac{E_{D^*}}{E_c}$$

- Hadronization of quarks into Hadrons not calculable in pQCD
- quark  $\rightarrow$  meson transition described by phenomenological transition function
- expected to be universal

**similar spectra**

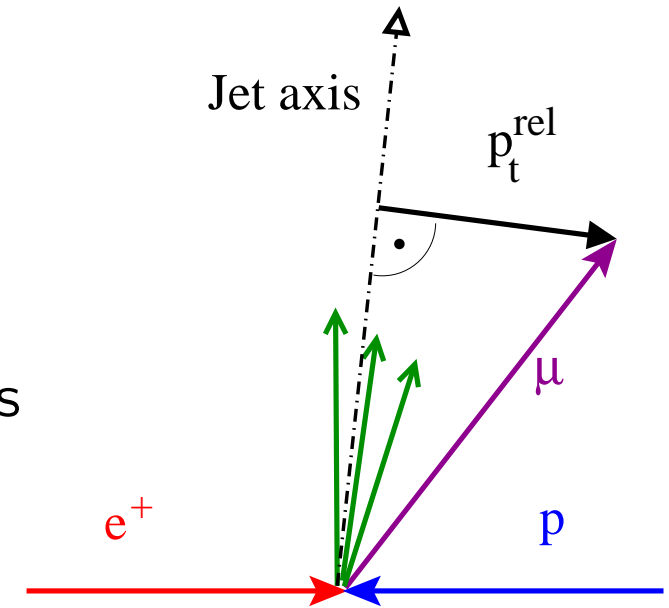
# Beauty tagging: $p_t^{rel}$

## Why beauty?

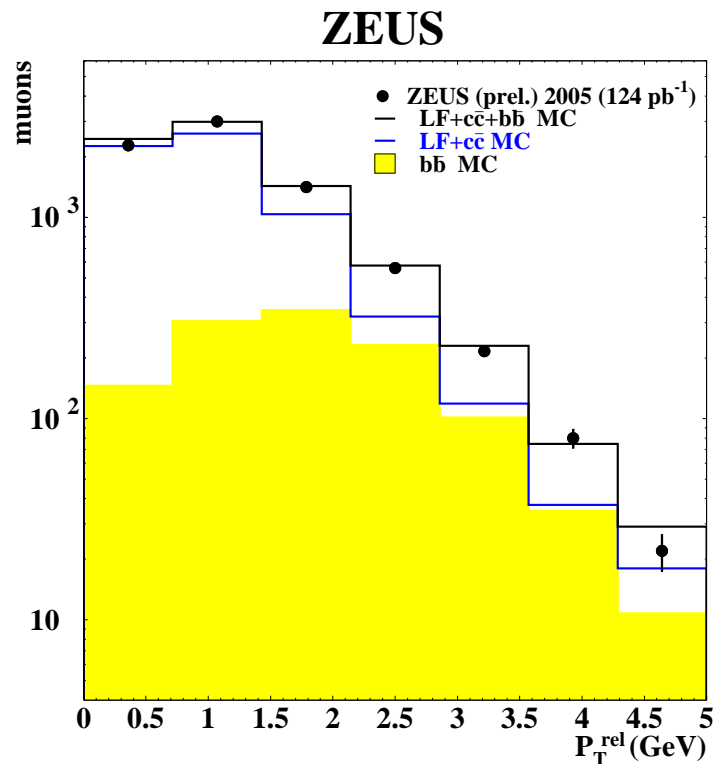
$\sigma_{b\bar{b}}/\sigma_{c\bar{c}} \sim 0.05 \Rightarrow$  hard to identify beauty, but  
 $m_b > m_c \Rightarrow$  pQCD should become more reliable

## How to identify $b \rightarrow \mu \bar{\nu} X$ ?

2 jet events (BGF) with tagged  $\mu$  in one of the jets



Large  $b$  mass causes high  $p_t$  of  $\mu$  relative to the jet ( $p_t^{rel}$ )



$$Q^2 < 1 \text{ GeV}^2$$
$$0.2 < y < 0.8$$

$$E_t^{jets} > 7(6) \text{ GeV} \quad |\eta(jets)| < 2.5$$
$$p_t(\mu) > 2.5 \text{ GeV} \quad -1.6 < \eta(\mu) < 2.3$$

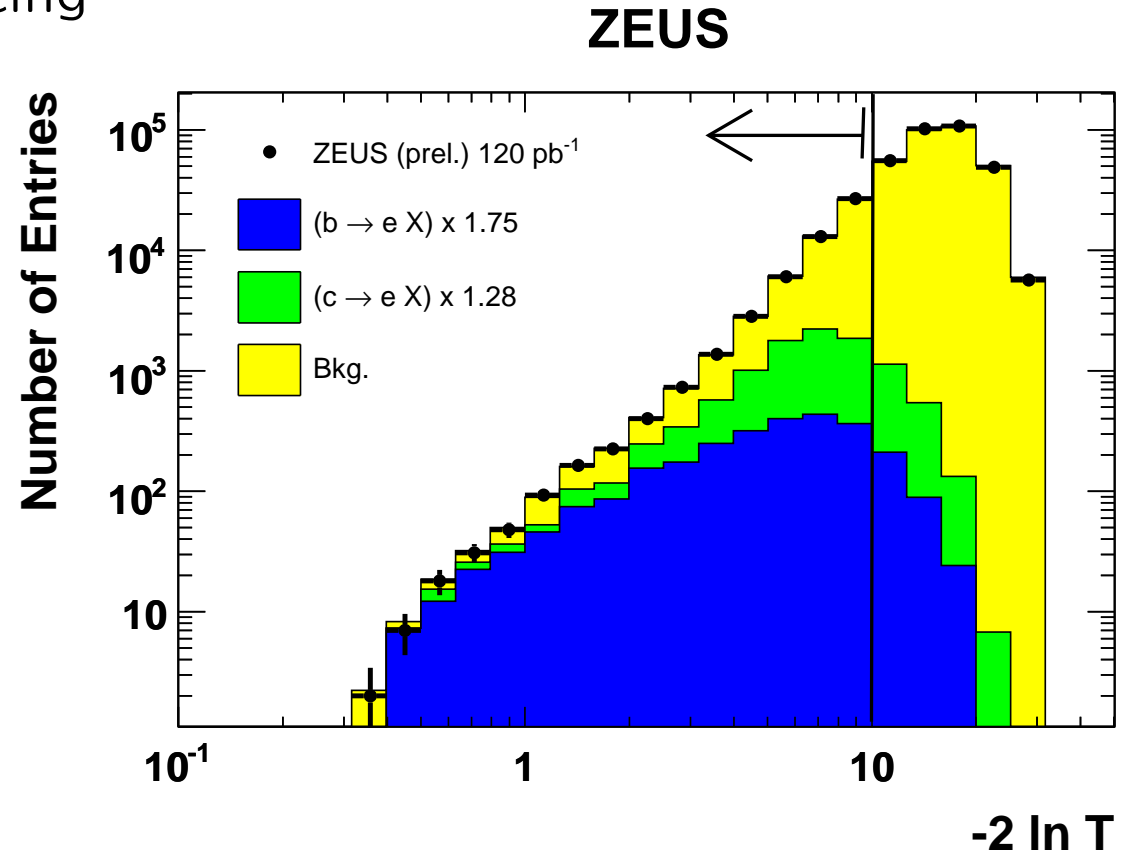
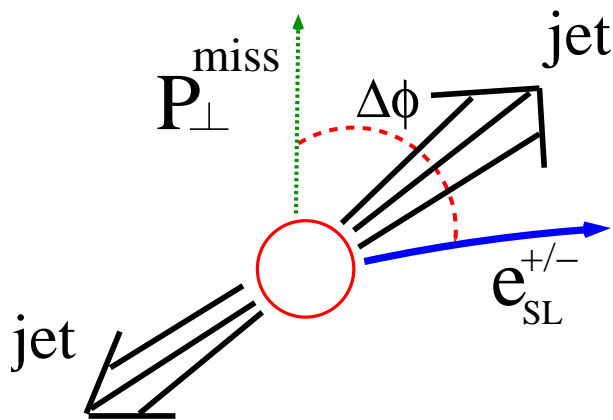
# Beauty in Dijet $\gamma p$ using electrons

Likelihood function of discriminating input variables:

$$\left. \begin{array}{l} dE/dx \\ f_{EMC} \\ E_{EFO}/p_{trk} \end{array} \right\} \text{e-identification}$$

$$\Delta\phi \quad b, c \leftrightarrow \text{LF separation}$$

$$p_t^{rel} \quad b \leftrightarrow c \text{ separation}$$



$$Q^2 < 1 \text{ GeV}^2$$

$$0.2 < y < 0.8$$

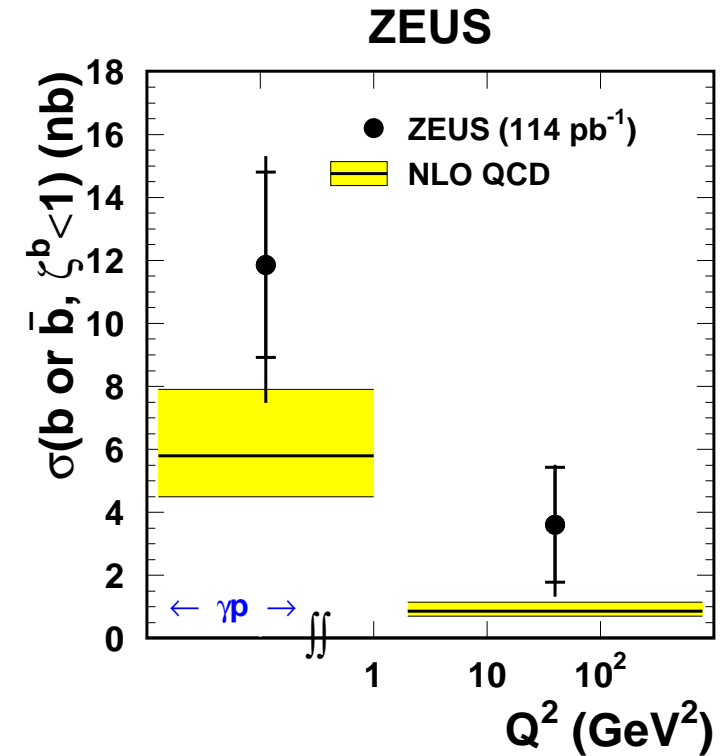
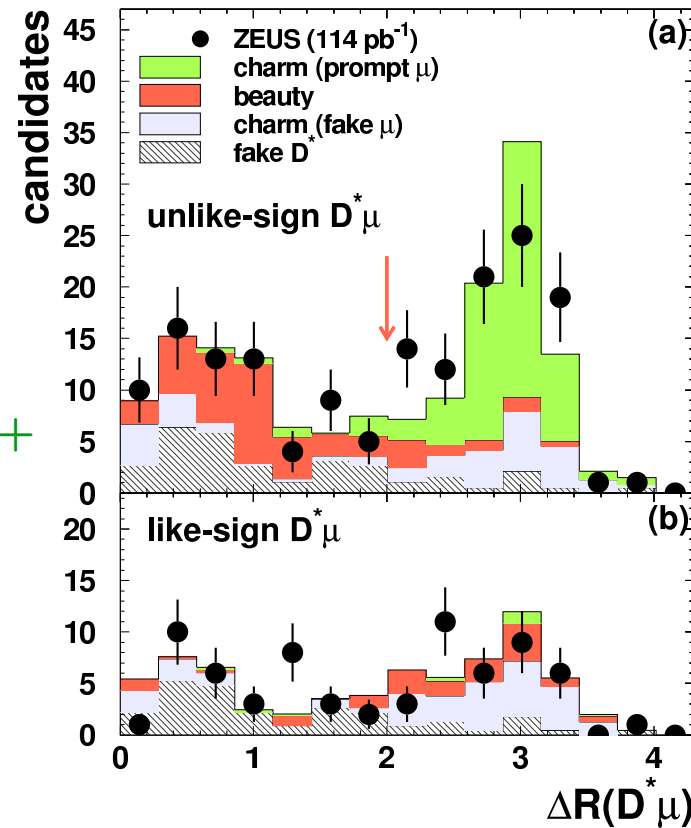
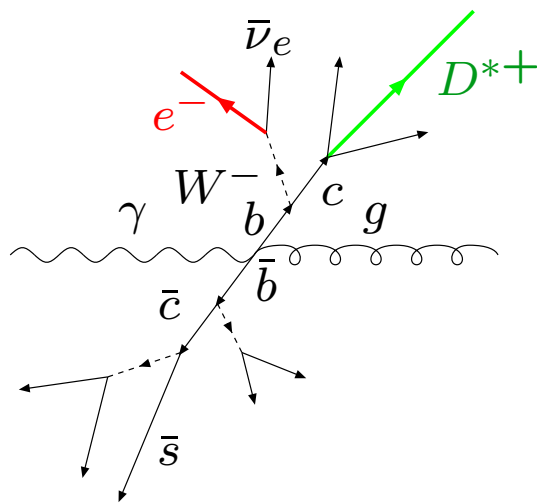
$$E_t^{jets} > 7(6) \text{ GeV} \quad |\eta(jets)| < 2.5$$

$$p_t(e) > 0.9 \text{ GeV} \quad |\eta(e)| < 1.5$$

# Double tagging of $b\bar{b}$ -pair

use two direct flavour tags ( $D^* + \mu$  or  $\mu + \mu$ )

- strong background reduction;  
no jets needed
- low  $p_t$  accessible

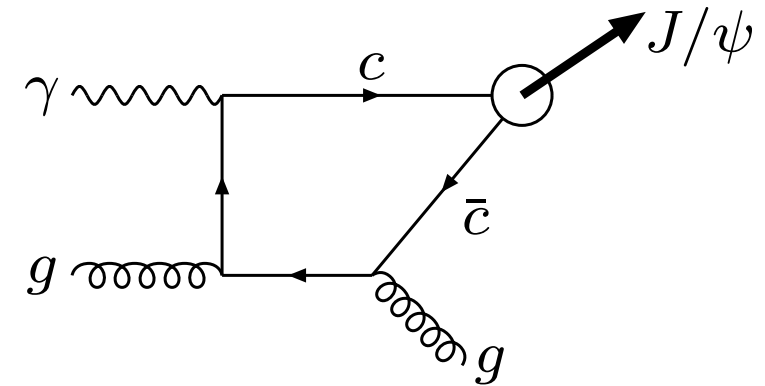


- measurement exceeds NLO QCD prediction
- compatible within errors
- agreement with corresponding H1 result

# Inelastic $J/\psi$ production

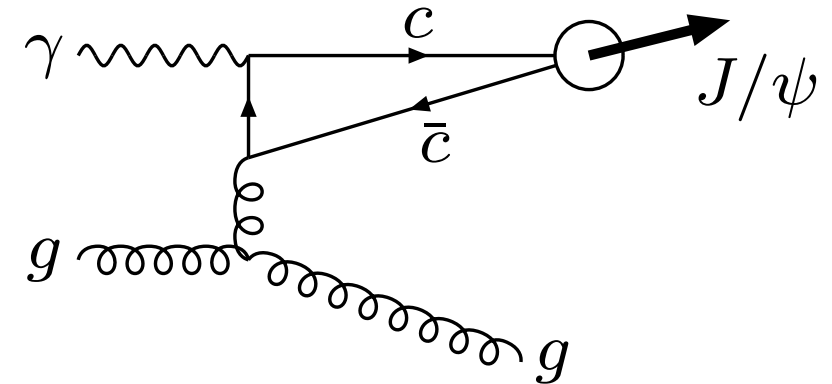
## Colour Singlet (CS) contribution

- directly calculable
- available at LO and NLO

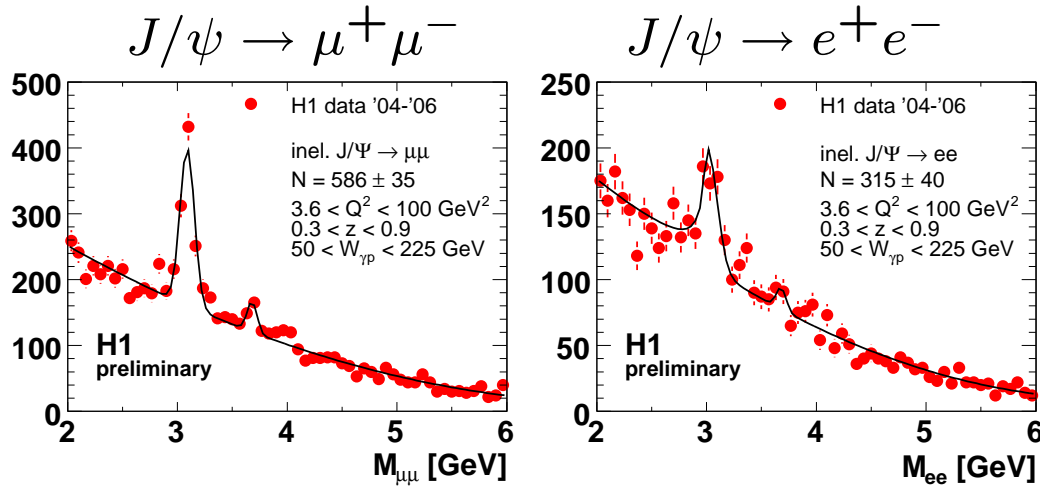


## Colour Oktet (CO) contribution

- introduced in non-relativistic QCD model (NRQCD)
- described by long distance matrix elements (LDME)
- parameterized from Tevatron data
- prediction for HERA, LO only



# Inelastic $J/\psi$ production



- $Q^2$  distribution
  - too hard in CASCADE
  - too steep in EPJPSI
- double differential cross sections in  $z$  and  $p_t^{*2}$ 
  - well described by leading order MC (colour singlet only)
  - no direct indications for colour octet

$$\begin{aligned}
 &3.6 < Q^2 < 100 \text{ GeV}^2 \\
 &50 < W_{\gamma p} < 225 \text{ GeV} \\
 &0.3 < z < 0.9 \\
 &p_{t,\psi}^* > 1 \text{ GeV}
 \end{aligned}$$

Monte Carlo (CS):

- CASCADE  
(scaled by 0.5)
- EPJPSI  
(scaled by 1.4)

