

# Measurement of $F_2^{\text{cc}}$ and $F_2^{\text{bb}}$ using the H1 Vertex Detector and combination of $F_2^{\text{cc}}$ with $D^*$ method

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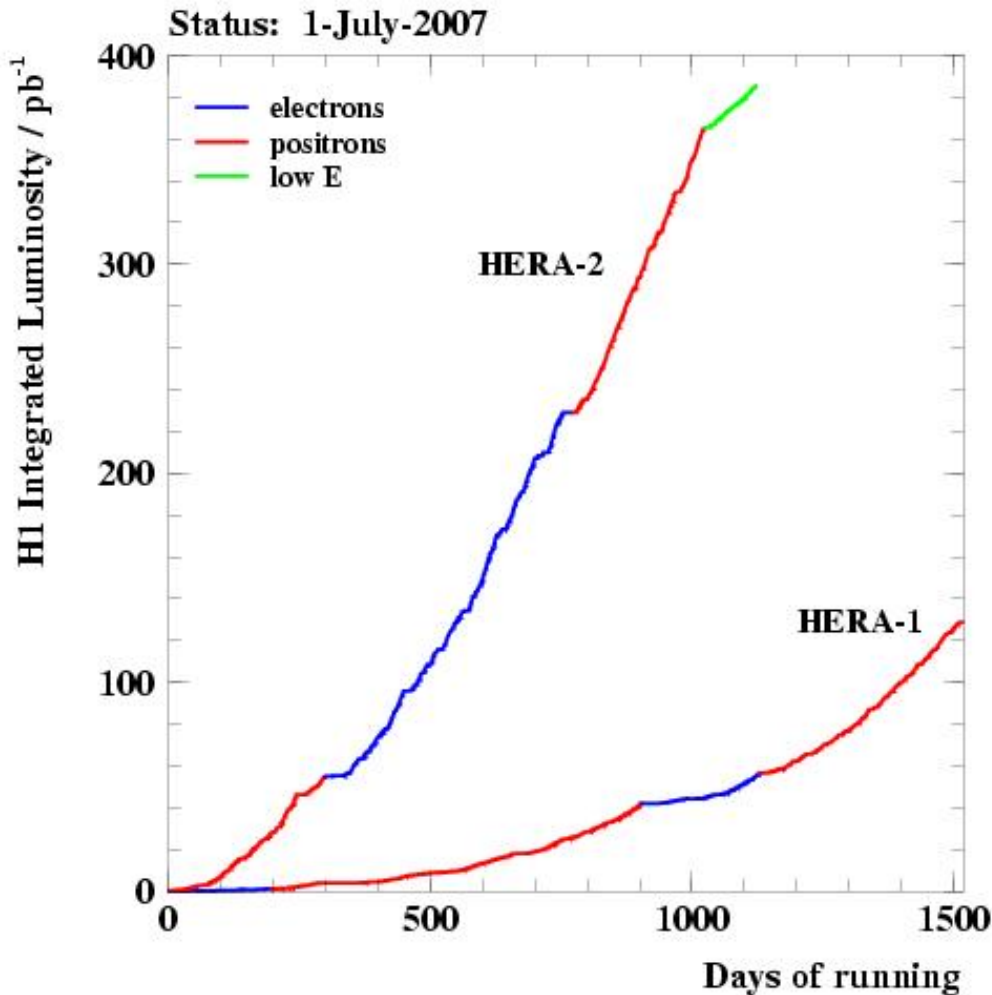


for the H1 Collaboration

- Motivation
- Experimental Techniques
- charm and beauty inclusive cross sections in DIS
- Combination of  $D^*$  and vertex detector methods

DIS 2009, Madrid 26<sup>th</sup>-30<sup>th</sup> April, 2009

# Available Data

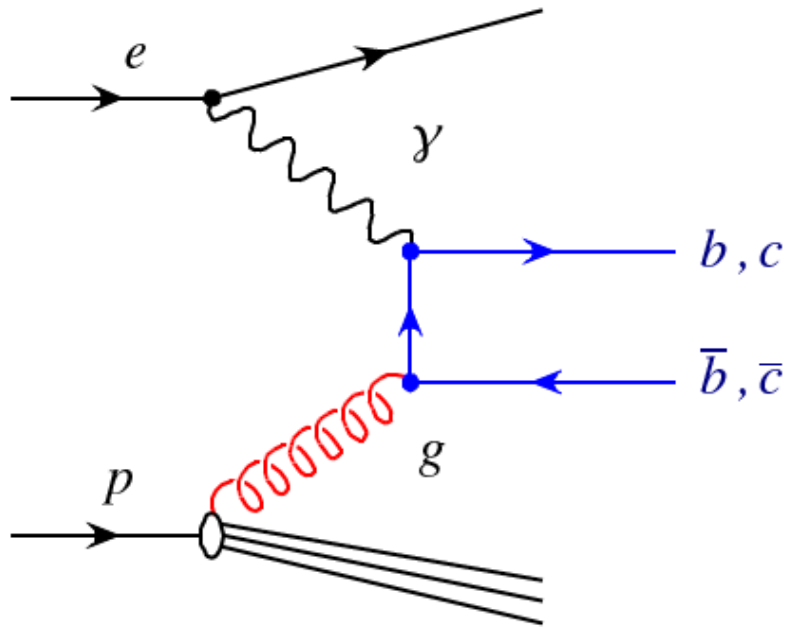


- In total  $\sim 500\text{pb}^{-1}$  of high energy data collected
- luminosity upgrade in 2001
- detectors adjusted

*Preliminary analyses on full HERA II data*

*Working on final publication and combination of results*

# Production of Heavy Quarks



Predominantly via *boson gluon fusion* (BGF)

Test of perturbative QCD:

multi-scale problem ( $Q^2, M^2, p_T^2$ )

Directly sensitive to gluon density in the proton (PDFs)

*Heavy quark contribution to structure function*

$F_2^{bb}$  measurements at high  $Q^2$   
important for LHC e.g.  $bb \rightarrow H$

$$\frac{d^2 \sigma^{b\bar{b}}}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} Y_+ \left[ F_2^{b\bar{b}}(x, Q^2) - \frac{y^2}{Y_+} F_L^{b\bar{b}}(x, Q^2) \right]$$

for low  $Q^2$  with  $Y_+ = (1 + (1-y)^2)$

# Heavy Quark Production

Number of theoretical approaches for treatment of quark mass:

*“massive”* (Fixed Flavour)  $Q^2 \sim M^2$ , neglects  $\alpha_s \ln Q^2 / M^2$

*“Massless”* (Zero Mass)  $Q^2 \gg M^2$ , resums  $\alpha_s \ln Q^2 / M^2$

Combination of massive/massless – *general mass* (GM) and *intermediate mass* (IM) flavour *number schemes* (NS).

## QCD Calculations:

- FFNS NLO Fixed Order BGF( $\alpha_s^2$ ) (final state - HVQDIS)
- GM-VFNS used in latest global PDF fits:
  - MSTW08 NLO* (BGF  $\alpha_s^2$ ), *MSTW08 NNLO* (BGF  $\alpha_s^3$ )
  - CTEQ 6.6 NLO* (BGF  $\alpha_s$ )

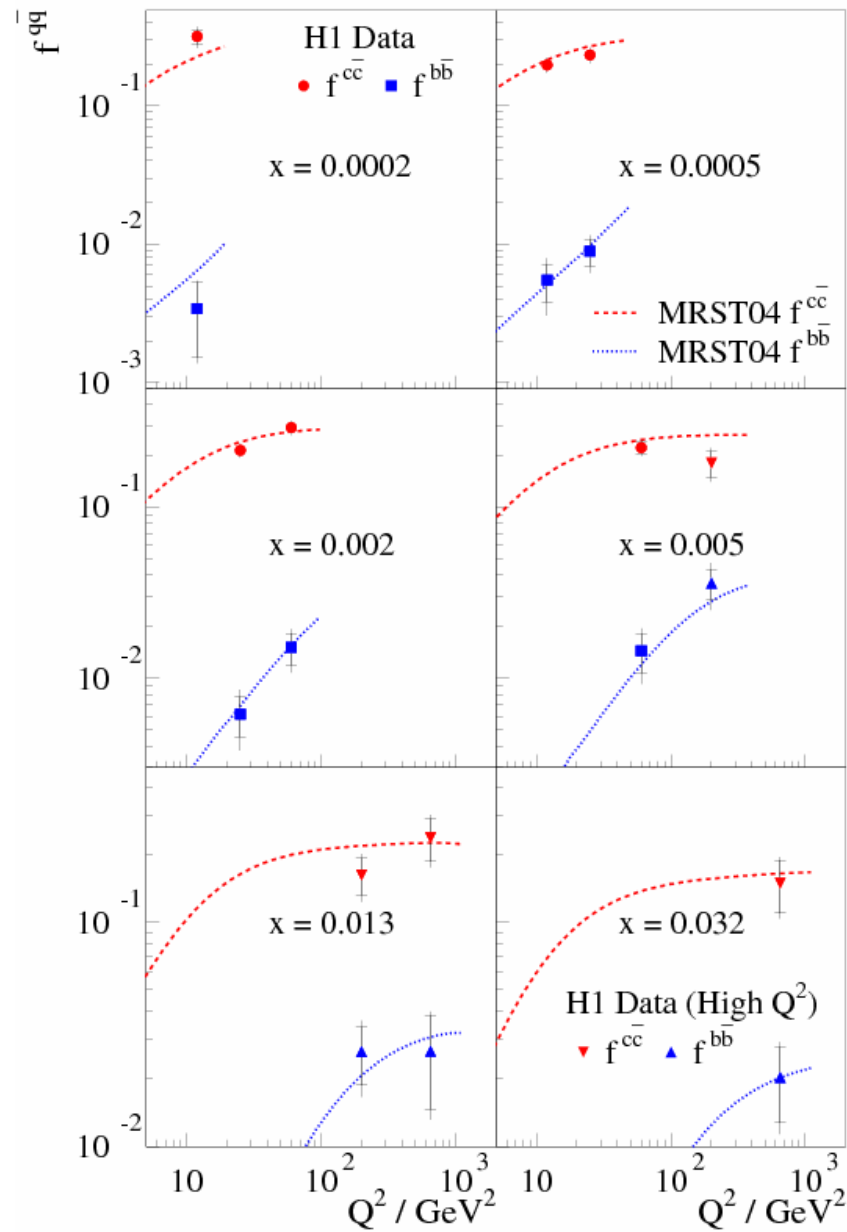
Monte-Carlo: LO ( $\alpha_s$ ) + Parton shower:

- $K_T$  factorisation, CCFM (CASCADE)
- Collinear factorisation, DGLAP (RAPGAP)

# Contribution to Cross Section

HERA I result:

- fraction of total DIS cross section from **charm** and **beauty**
- large charm fraction (~30%)
- small beauty fraction ~% (lower at low  $Q^2$ )
- mass thresholds visible
- reasonable description by QCD



# Tagging Heavy Quarks ( $c$ )

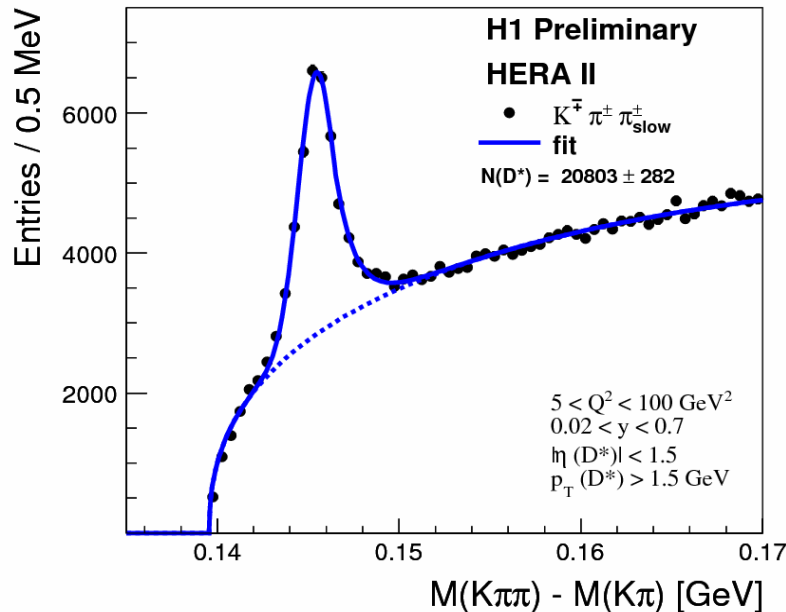
$D^*$  method for combination later      Use  $D^* \rightarrow D^0 \pi_s \rightarrow K \pi \pi_s$

Tracks reconstructed in H1 Central Tracking Detector

Full HERA II statistics ( $\sim 350 \text{ pb}^{-1}$ )

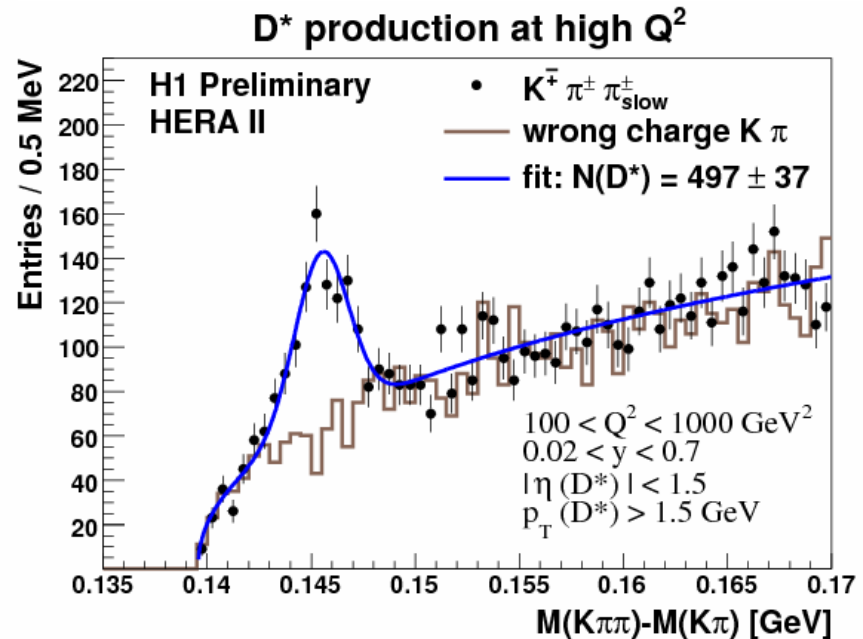
$5 < Q^2 < 100 \text{ GeV}^2$

H1prelim-08-072



$100 < Q^2 < 1000 \text{ GeV}^2$

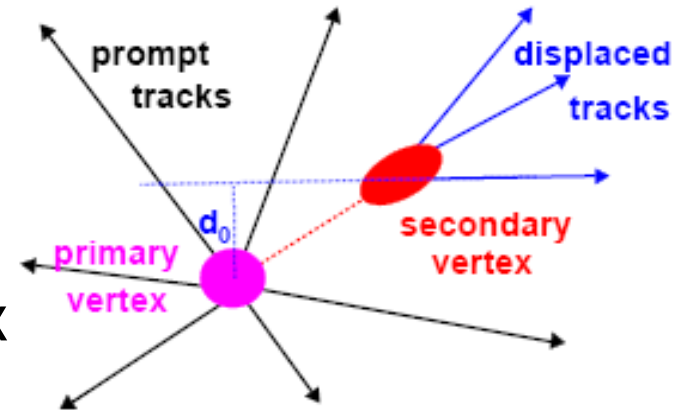
H1prelim-08-074



# Tagging Heavy Quarks ( $b$ )

Beauty quarks rarely produced, use properties of beauty hadrons:

- multiplicity
- lifetime (vertex detectors)
  - reconstruction of a secondary vertex
  - impact parameter  $\delta$

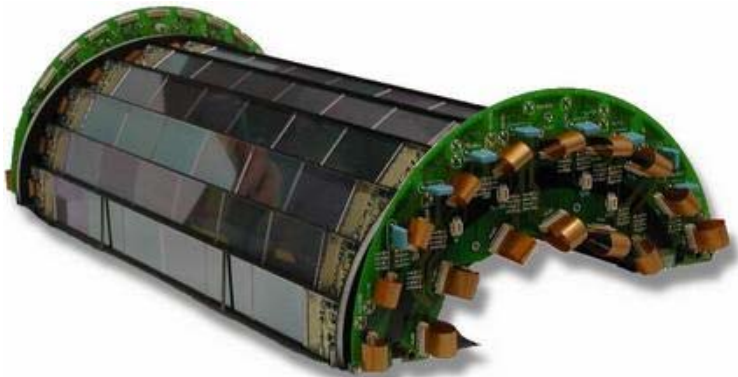


$4.5 < Q^2 < 1600 \text{ GeV}^2$  H1prelim-08-173

Measurement of charm as well. Higher efficiency and acceptance (inclusive measurement) but larger background compared with  $D^*$  method

# H1 Vertex Detector (CST)

**Central Silicon Tracker**  
( $30^\circ < \theta < 150^\circ$ )



- Rebuilt to take into account HERA II beam-line
- Double layer double sided strips
- Precise determination of impact parameter in transverse plane
- Resolution of  $|\delta|$  for hits in both layers:

$$33\mu m \oplus \frac{90\mu m}{P_T} [GeV]$$

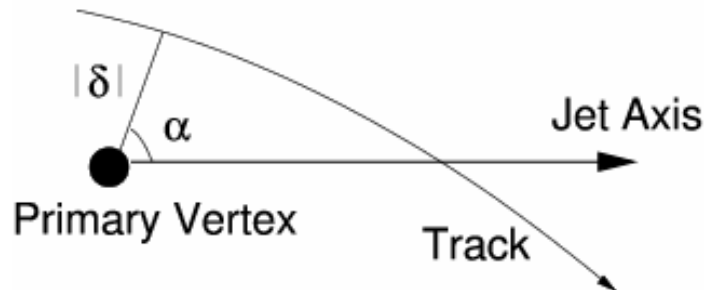


# Impact Parameter

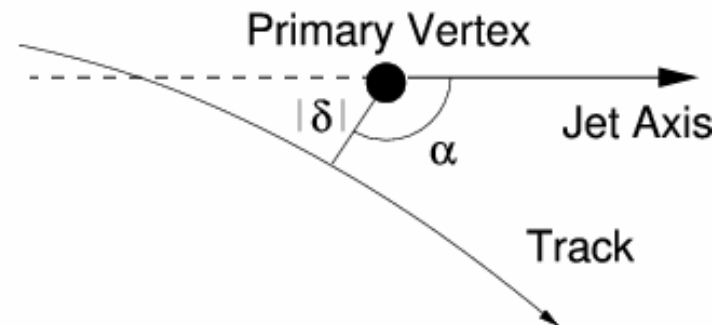
- Inclusive analysis: use all tracks with hits in silicon detector ( $p_t > 0.3 \text{ GeV}$ )
- Single track events can contribute to impact parameter
- Sign of impact parameter given wrt highest  $p_T$  jet axis

## Signed impact parameter $\delta$

$$\alpha < 90^\circ \rightarrow \delta = +|\delta|$$

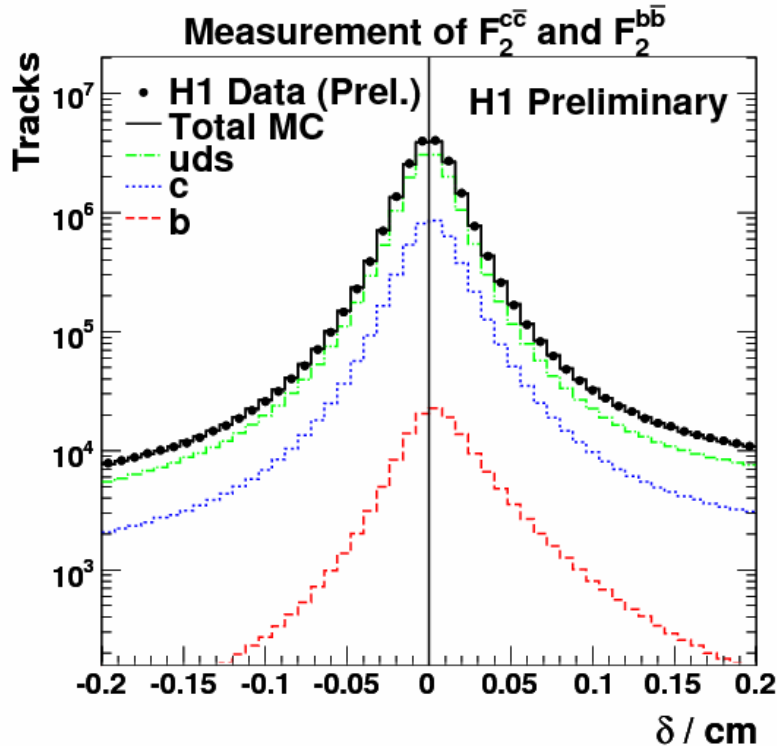


$$\alpha > 90^\circ \rightarrow \delta = -|\delta|$$



# Impact Parameter Significance

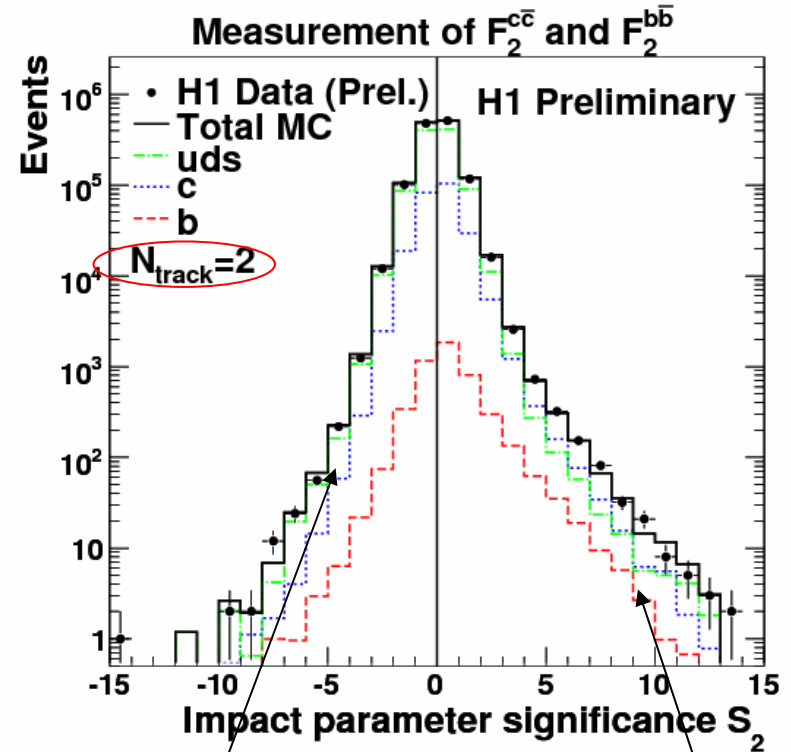
Signed Impact parameter  $\delta$



Charm and beauty asymmetric due to lifetime

Light flavours mostly symmetric

Significance  $S = \delta/\sigma(\delta)$



resolution

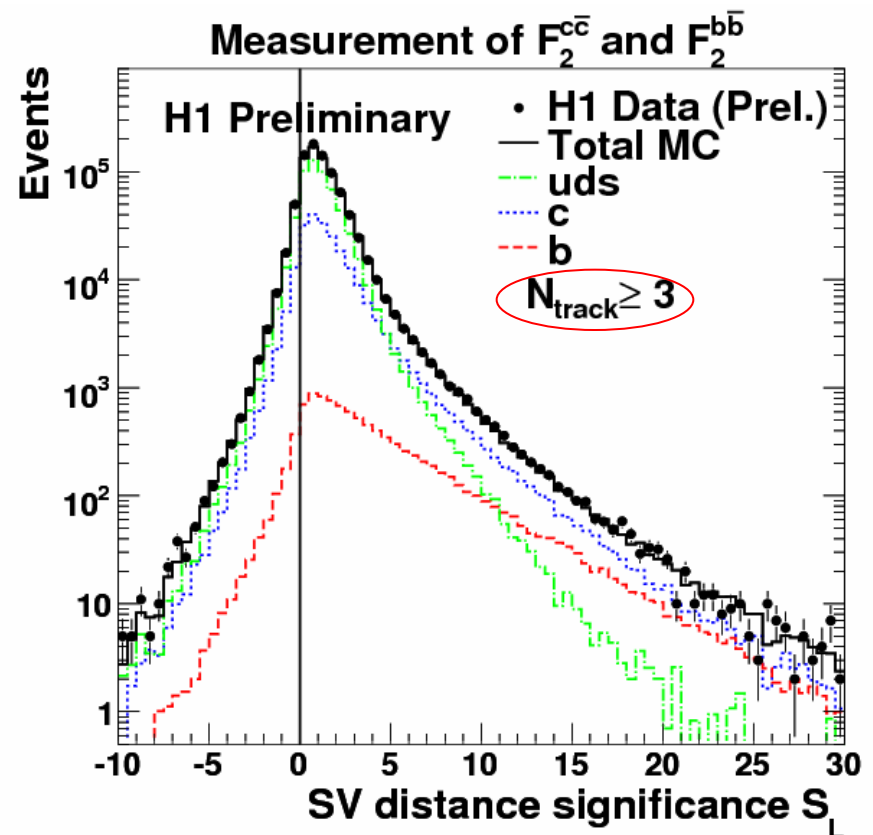
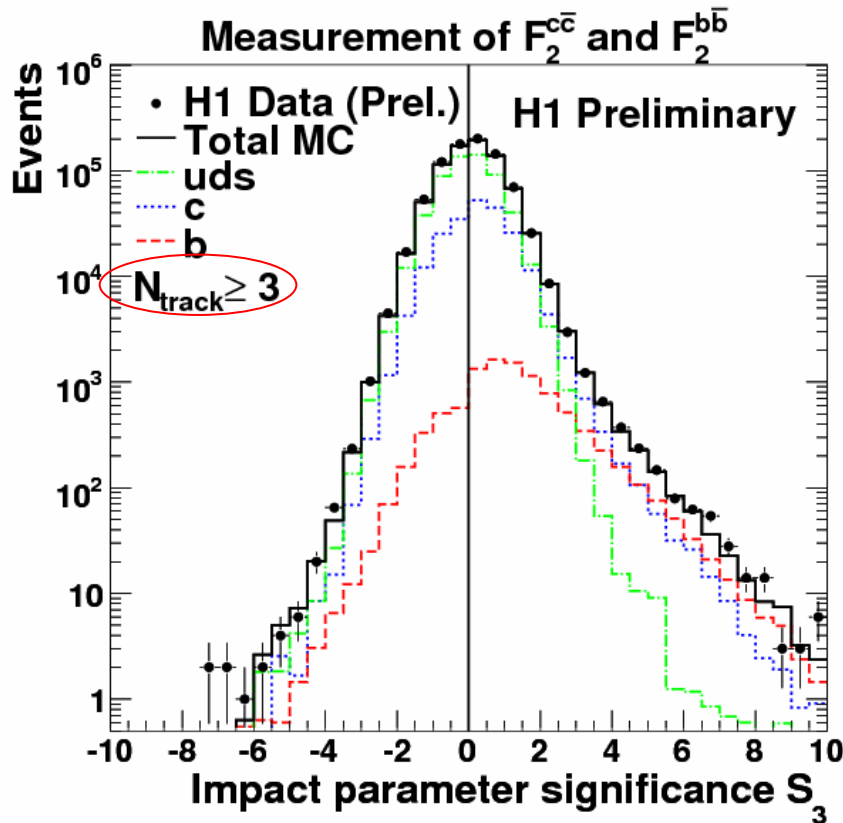
lifetime

$S_1$  highest  $|S|$  for  $N_{\text{track}}=1$

$S_2$  2<sup>nd</sup> highest  $|S|$  for  $N_{\text{track}}=2$

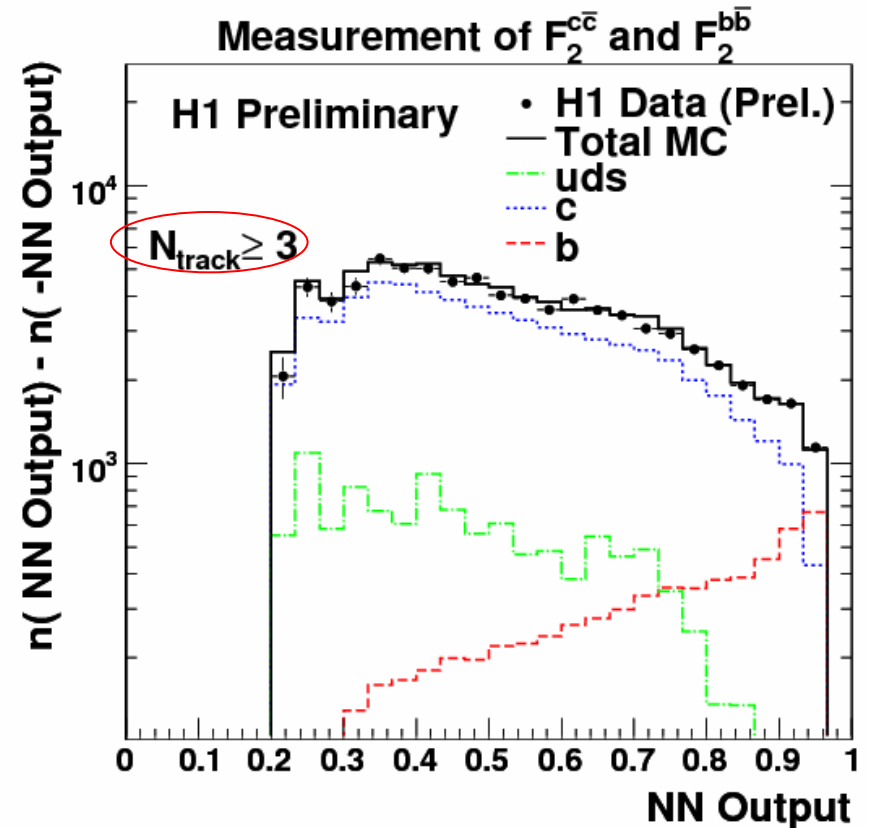
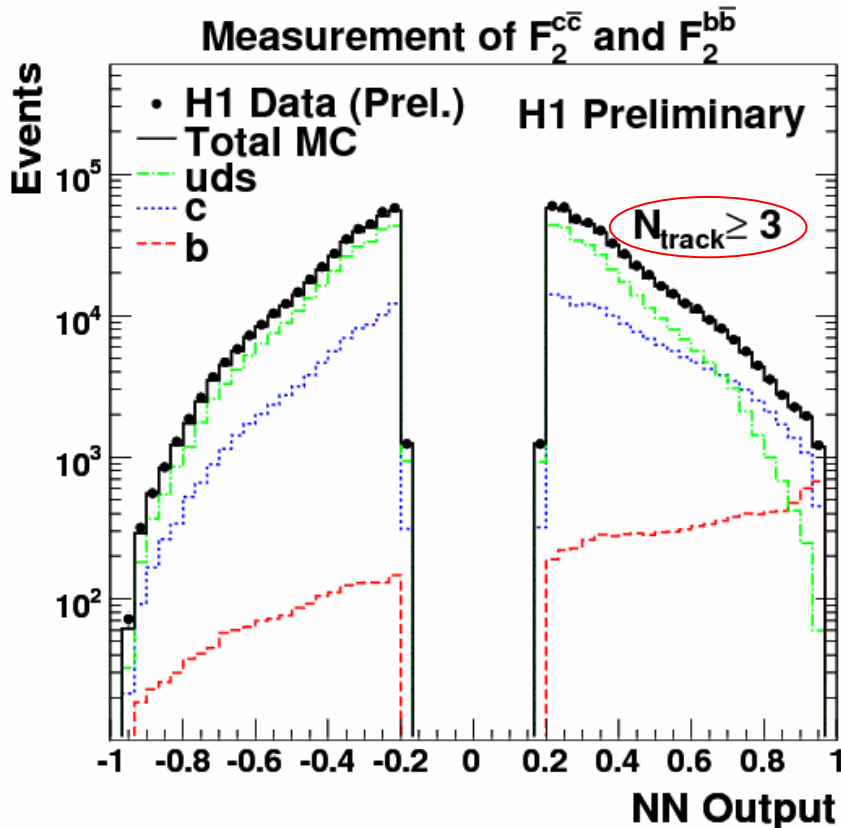
# Neural Network

- Improve  $c, b$  separation: use neural network for  $\geq 3$  tracks
- **Inputs:**  $S_1, S_2, S_3$ , sec. vertex decay length significance  $S_L$ , 1<sup>st</sup>(2<sup>nd</sup>) highest track  $p_T$ , number of CST (sec. vertex) tracks



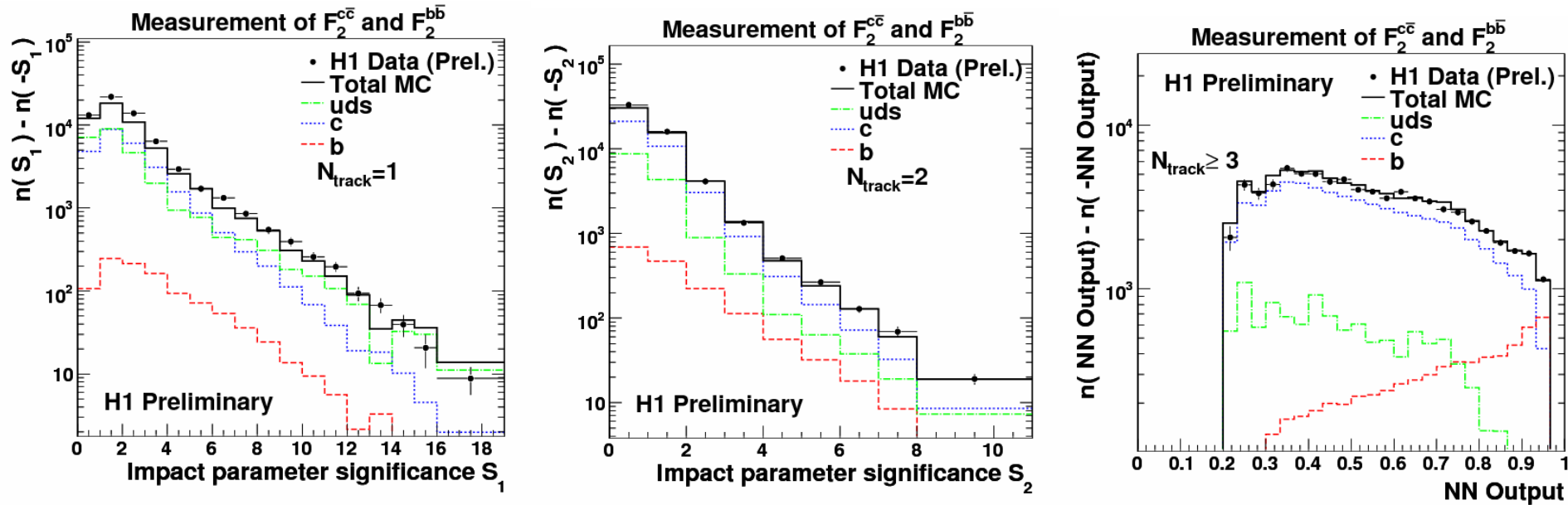
# Neural Network Output

- NN output gives clear separation of charm and beauty
- Sign given by  $S_1$ . Subtract -'ve from +'ve to reduce syst. error
- Fit subtracted  $S_1$ ,  $S_2$  and NN output to obtain c,b fractions



# Fitting Flavour Fractions

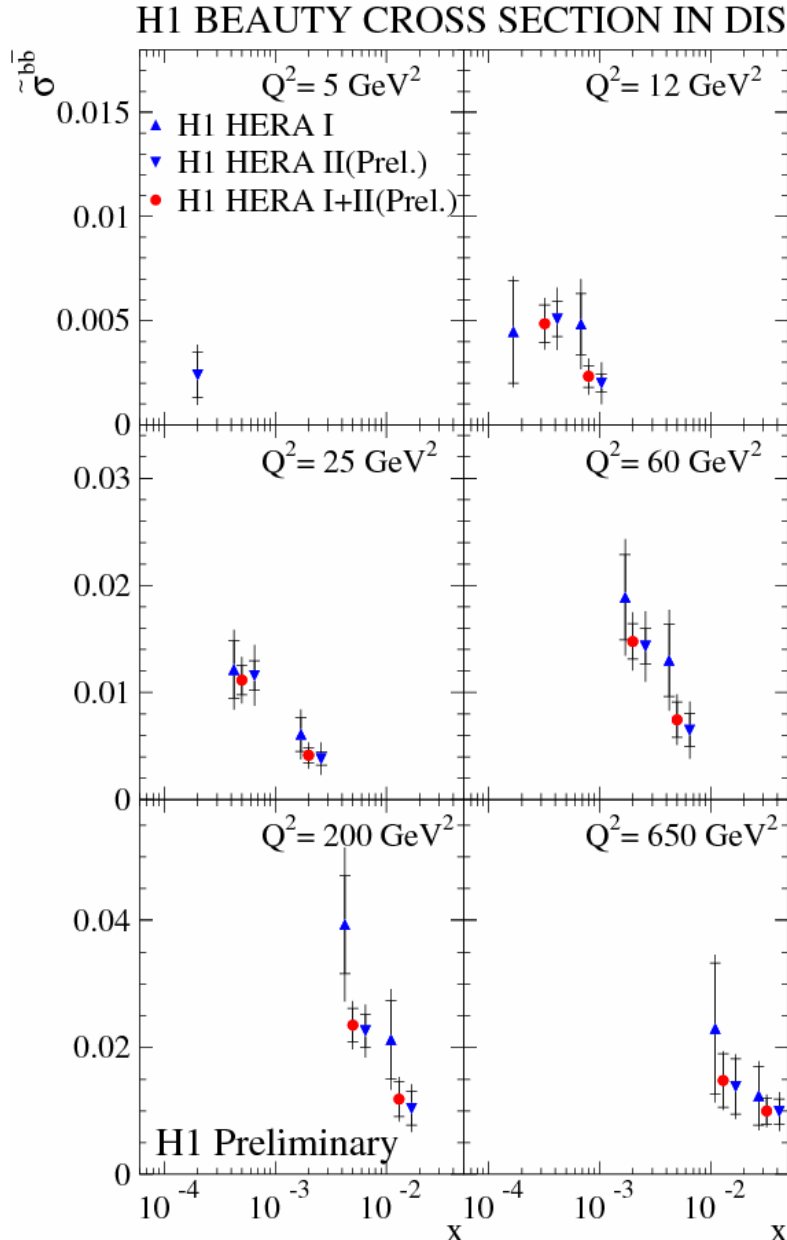
These distributions are fitted for  $\rho_c, \rho_b$  in each  $x, Q^2$  bin with  $\rho_{uds}$  constrained by total number of DIS events



$$\sigma^{cc}(x, Q^2) = \frac{\rho_c \cdot N_c^{\text{gen}}}{\rho_c \cdot N_c^{\text{gen}} + \rho_b \cdot N_b^{\text{gen}} + \rho_{uds} \cdot N_{uds}^{\text{gen}}} \sigma(x, Q^2) \delta_{\text{BCC}}$$

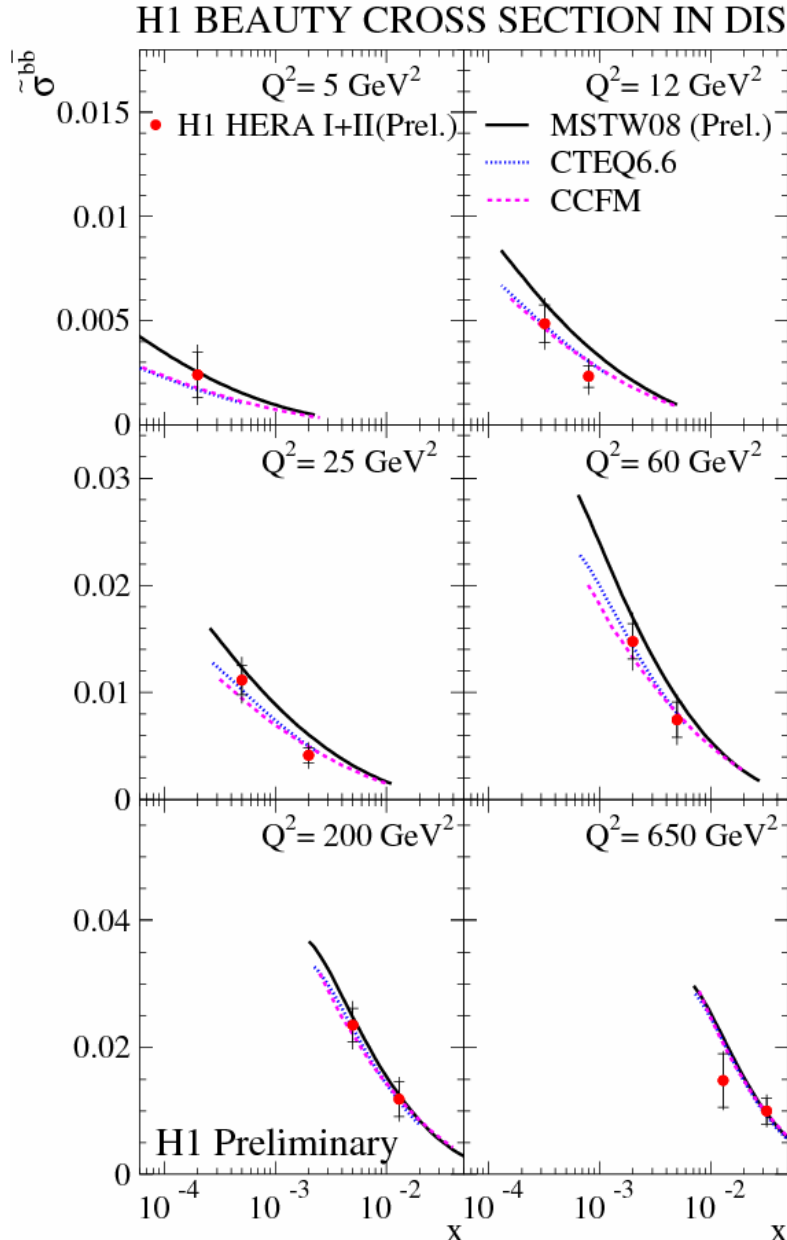
Normalisation from inclusive cross section  $\sigma(x, Q^2)$

# Inclusive $b$ Cross Section



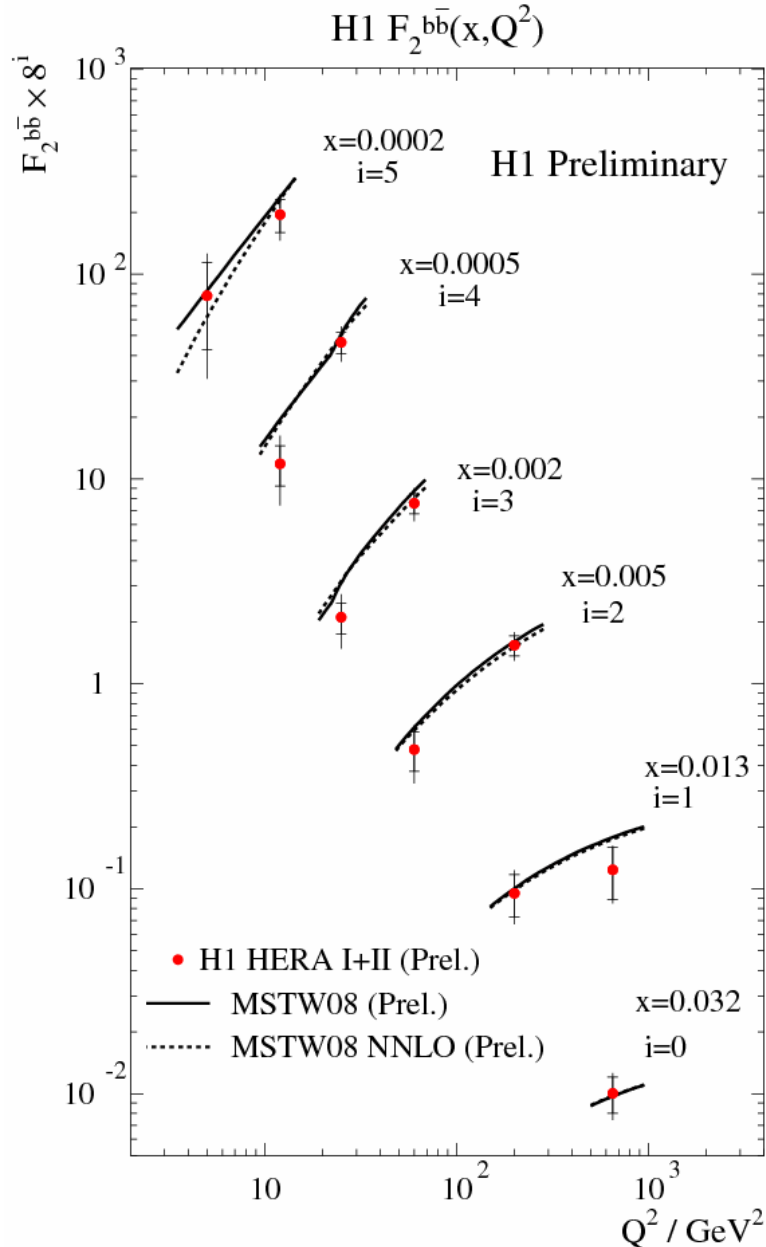
- Inclusive  $b$  cross section as function of  $x$  for fixed  $Q^2$
- Agreement with HERA I and improvement in precision
- Binning similar between HERA I and HERA II allows combination using the H1 “averaging” procedure (see later)
- Extension to lower  $Q^2$  for HERA II (improved method)

# Comparison of $\sigma^{bb}$ with theory



- Compare HERA I+II combined b cross section as function of  $x$  for fixed  $Q^2$  with theory
- Note rapid increase in magnitude from low  $Q^2$  to high  $Q^2$
- Described by NLO QCD and CCFM
- Differences in theory, generally within scale uncertainties

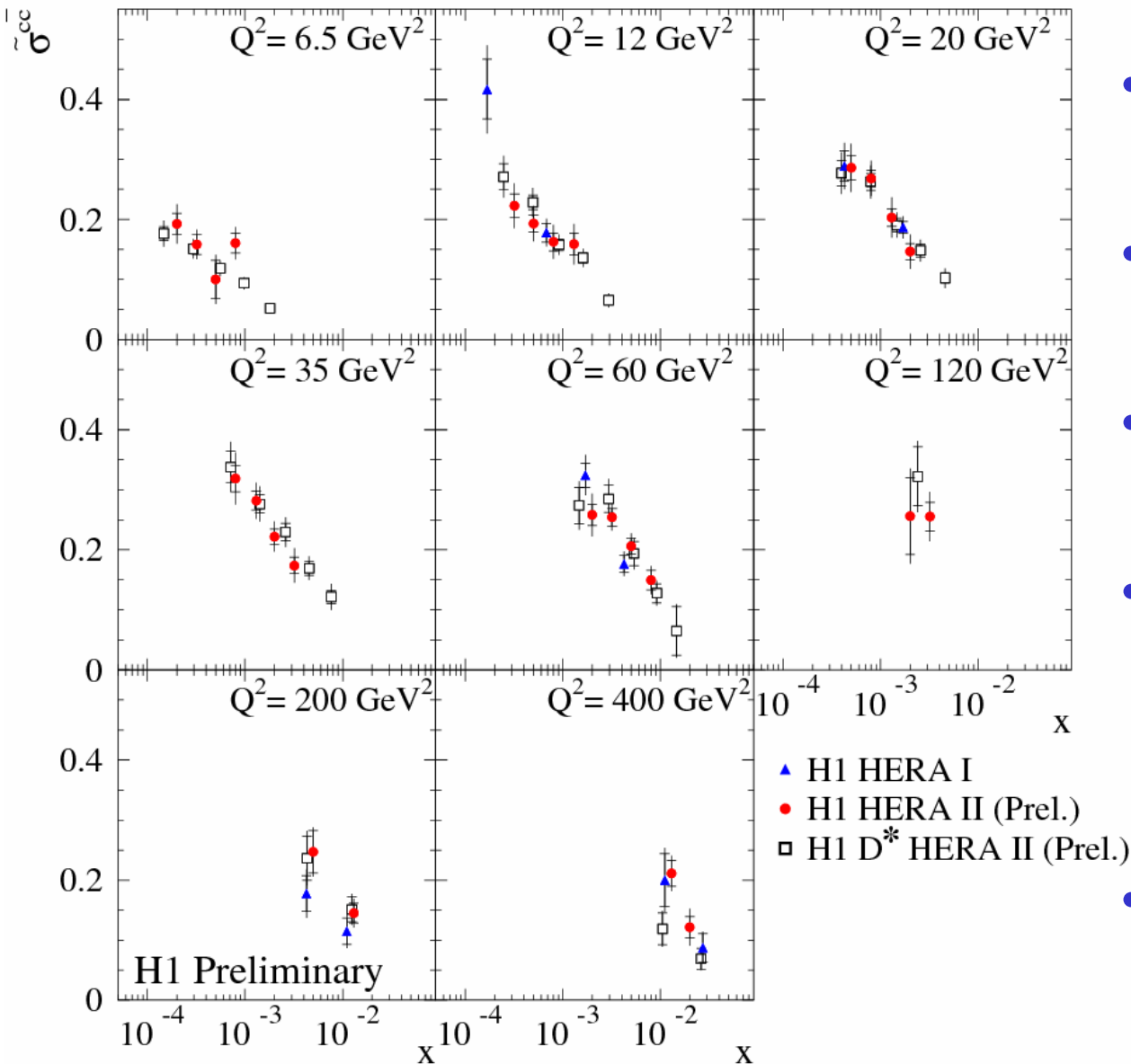
# Measurement of $F_2^{bb}$



- Beauty structure function versus  $Q^2$  for fixed  $x$
- NNLO predictions available
- Differences between NLO and NNLO small except for  $Q^2 < (m_b)^2$
- Data well described

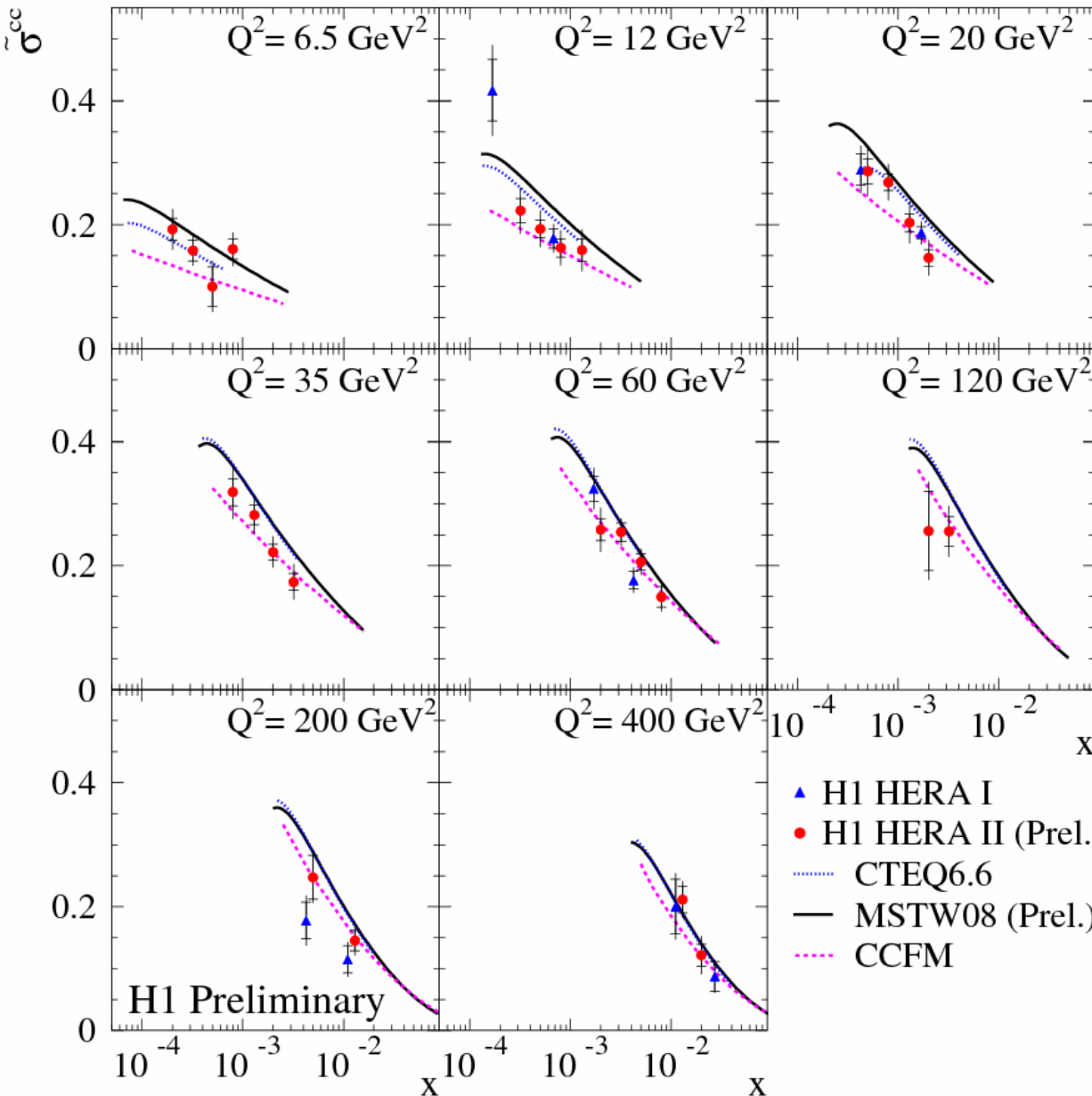


# Inclusive Charm Cross Section



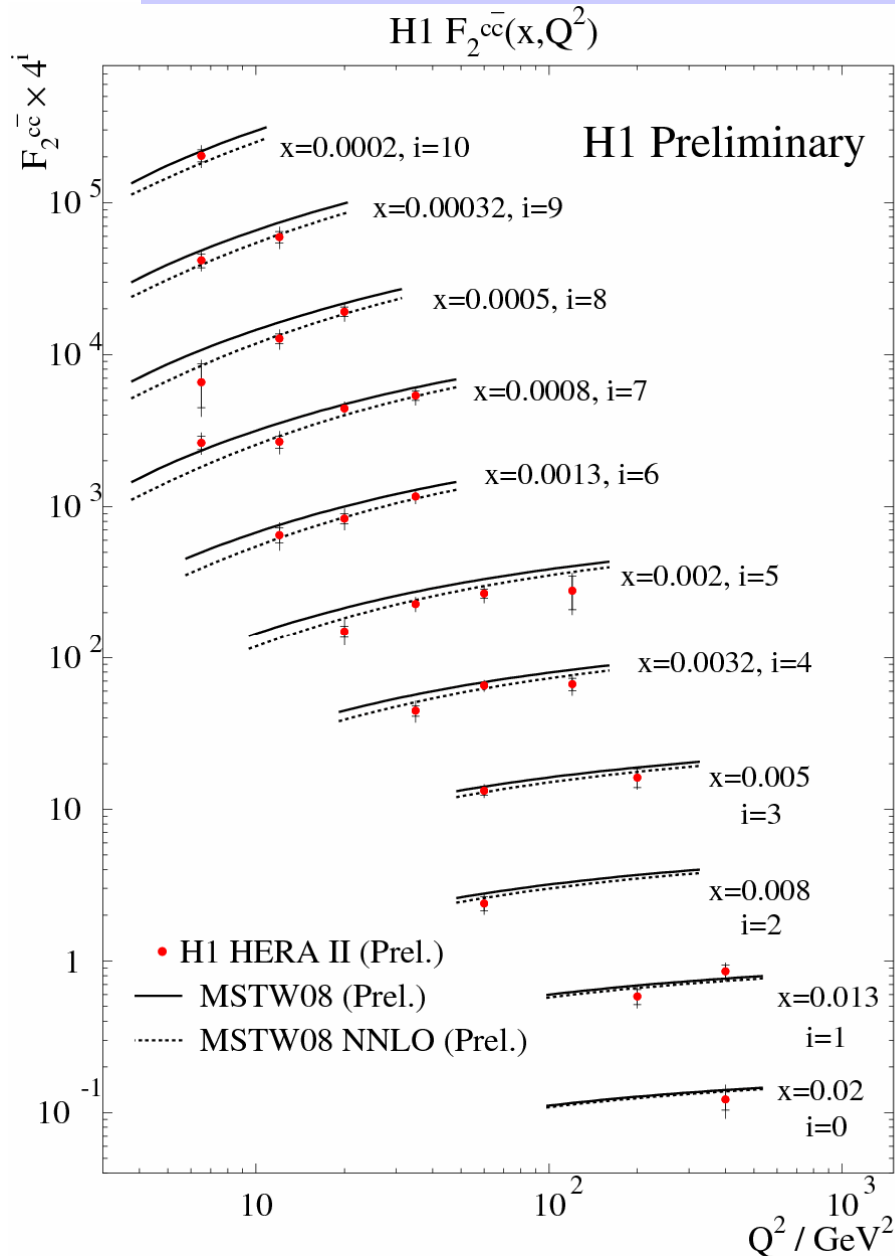
- HERA I and HERA II measurements agree
- Finer binning means no combination
- Method agrees well with results from  $D^*$
- $D^*$  measurements from DGLAP extrap.. No uncertainty shown (see details later)
- $D^*/\text{lifetime}$  give best precision at low/high  $Q^2$

## Inclusive Charm Cross Section



- Data described by QCD predictions
- CTEQ and MSTW NLO predictions very similar. Small difference at low  $Q^2$
- CCFM lower predictions especially at low  $Q^2$  but still reasonable

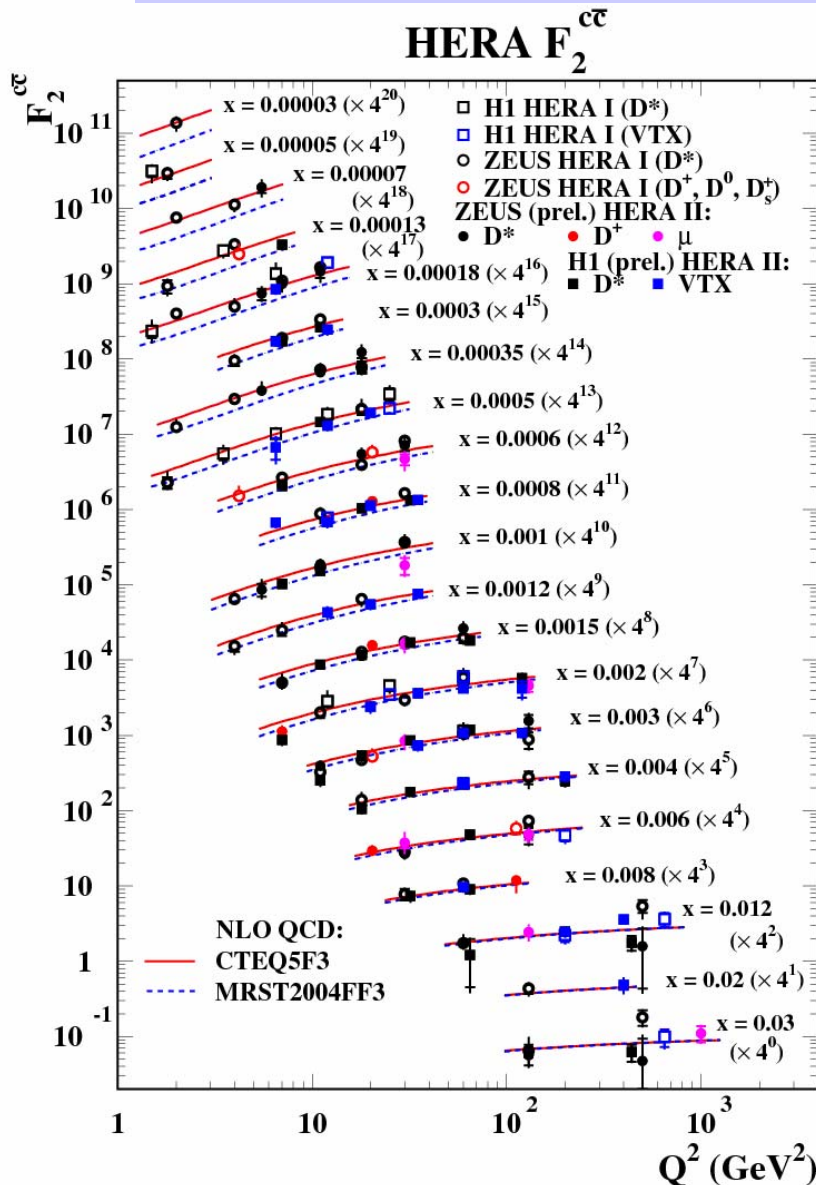
# Measurement of $F_2^{cc}$



- Look at H1 lifetime data vs  $Q^2$  for fixed  $x$
- Difference between MSTW NNLO and NLO larger for charm than beauty
- MSTW NNLO somewhat better description than NLO

What does all the HERA data look like...?

# Measurements of $F_2^{\text{cc}}$

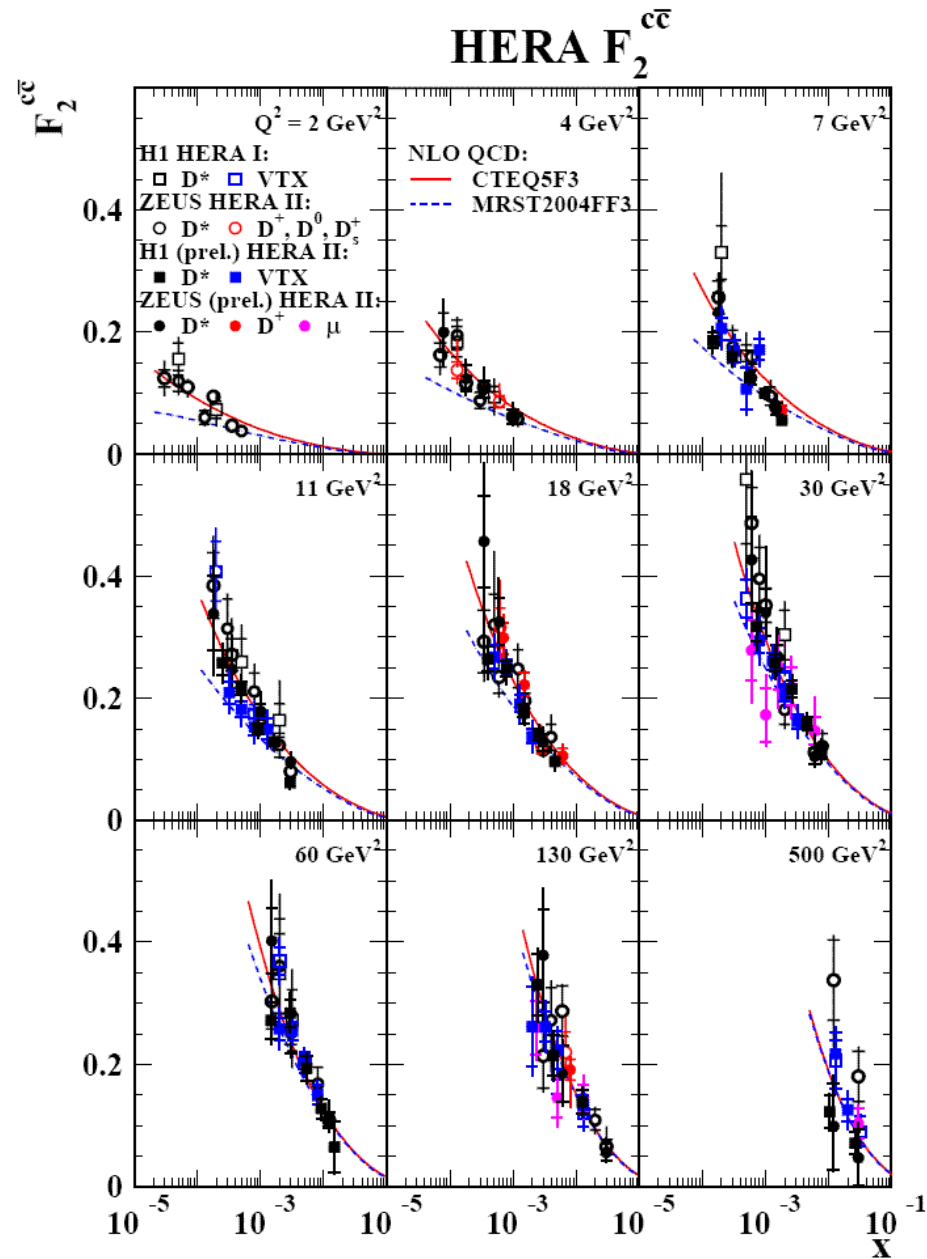


Plenty(!) of measurements:

- different precision
- different systematics
- (partially) different phase space

Can make use of different measurements by  
*combination of data*

# Motivation: gain in precision



Gain in precision to make the message more conclusive:

- combine different tag methods
- combine H1 and ZEUS

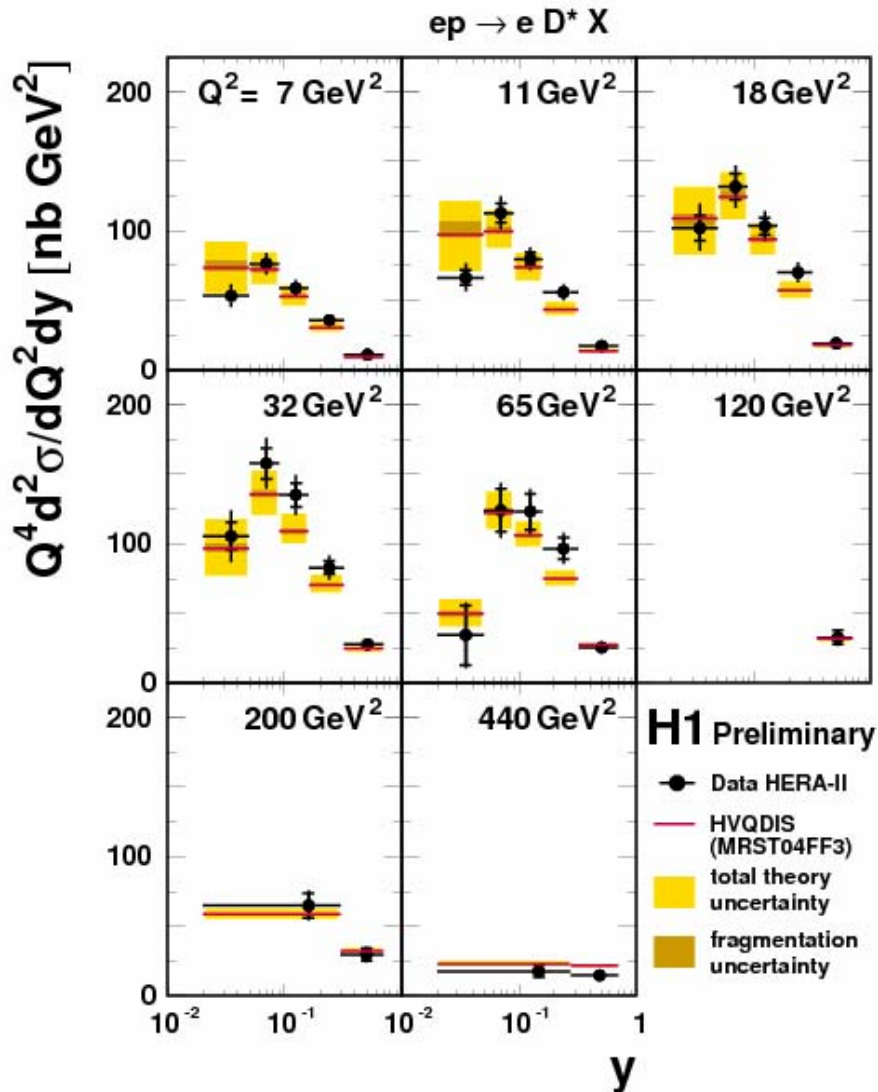
Get more discrimination between models?

As a *start* take most recent measurements of H1

# Averaging procedure

- Data in combination:
  - H1 Preliminary “lifetime” HERA-II
  - H1 Preliminary  $D^*$  HERA-II. Inclusive cross section obtained from differential cross section( $Q^2, y$ ) using NLO FFNS (see next slide)
- Measurements at different  $x$  and  $Q^2$ :
  - point swimming to the common grid using FFNS NLO DGLAP (Riemersma), PDF MRST04FF,  $m_c=1.43$  GeV
- Correlation of experimental uncertainties taken into account
  - 20 sources of point-to-point systematic correlations
  - 3 correlated sources between the methods

# Note on $D^*$ extrapolation



Extrapolation factors  
calculated from ratio of  
 $\sigma_{vis}(Q^2, y)$  to  $\sigma_{tot}$

Use either NLO FFNS (HVQDIS)  
or CCFM (CASCADE)

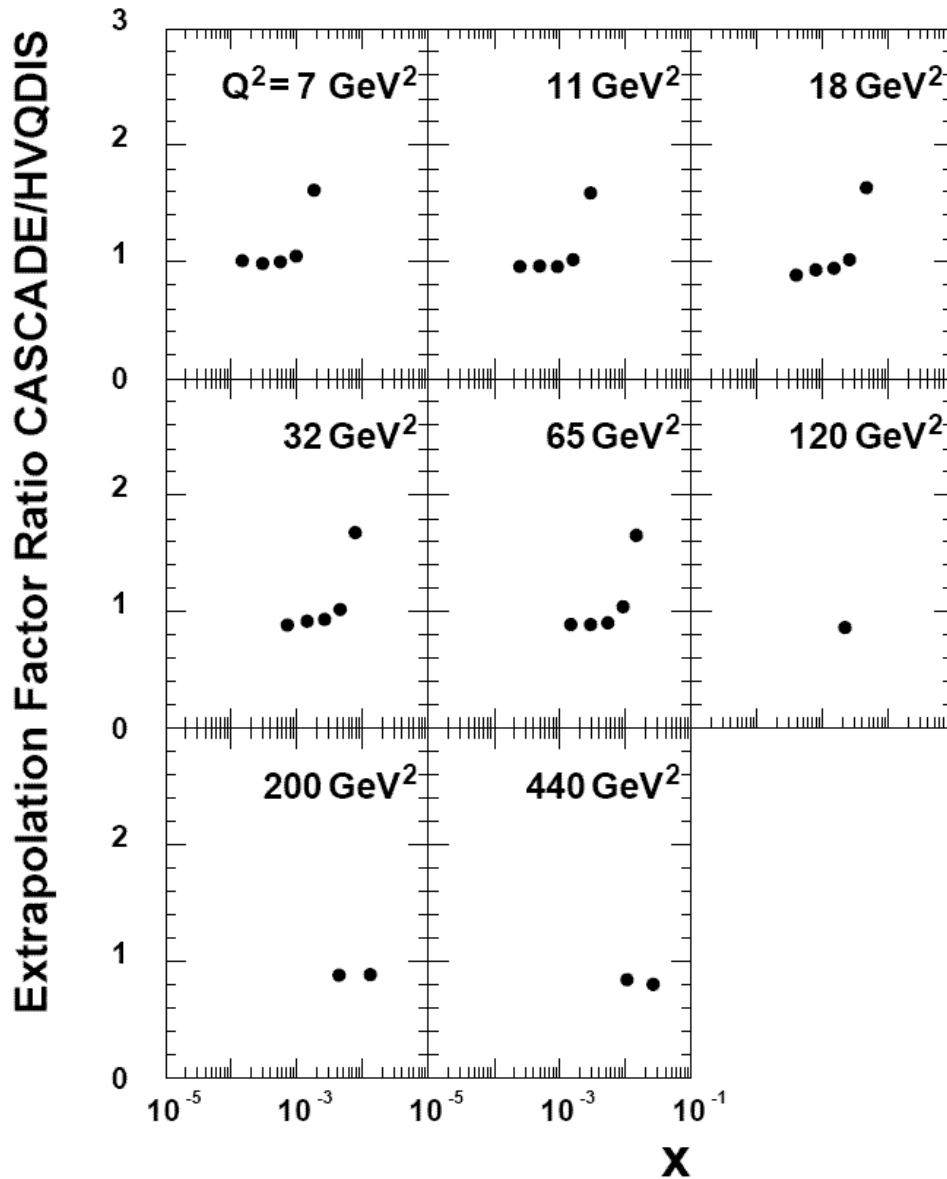
Extrapolation values in the  
range:

$1.5 - 5$

*high  $Q^2$  - low  $Q^2$  (low  $y$ /high  $x$ )*

*See talk from A. Jung*

# D\* extrapolation



Differences in extrapolation factors HVQDIS vs CASCADE:

Generally <10% (low x) but up to 100% (high x). Due to:

- LO+PS vs NLO
- Different evolution
- Different hadronization

Highest  $x$  points not included in the combination procedure

Difference accounted for as an additional model uncertainty



# Averaging procedure: definition

$$\chi^2(M^{i,true}, \Delta\alpha_j) = \sum_i \frac{\left[ M^{i,true} - \left( M^i + \sum_j \frac{\partial M^i}{\partial \alpha_j} \frac{M^{i,true}}{M_i} \Delta\alpha_j \right) \right]^2}{\left( \sigma_i \frac{M^{i,true}}{M_i} \right)^2} + \sum_j \frac{(\Delta\alpha_j)^2}{\sigma_{\alpha_j}^2}$$

Detailed in H1 paper  
[arXiv:0904.0929](https://arxiv.org/abs/0904.0929)

$M^i$  measured central values

$\sigma_i$  statistical + uncorrelated systematic error

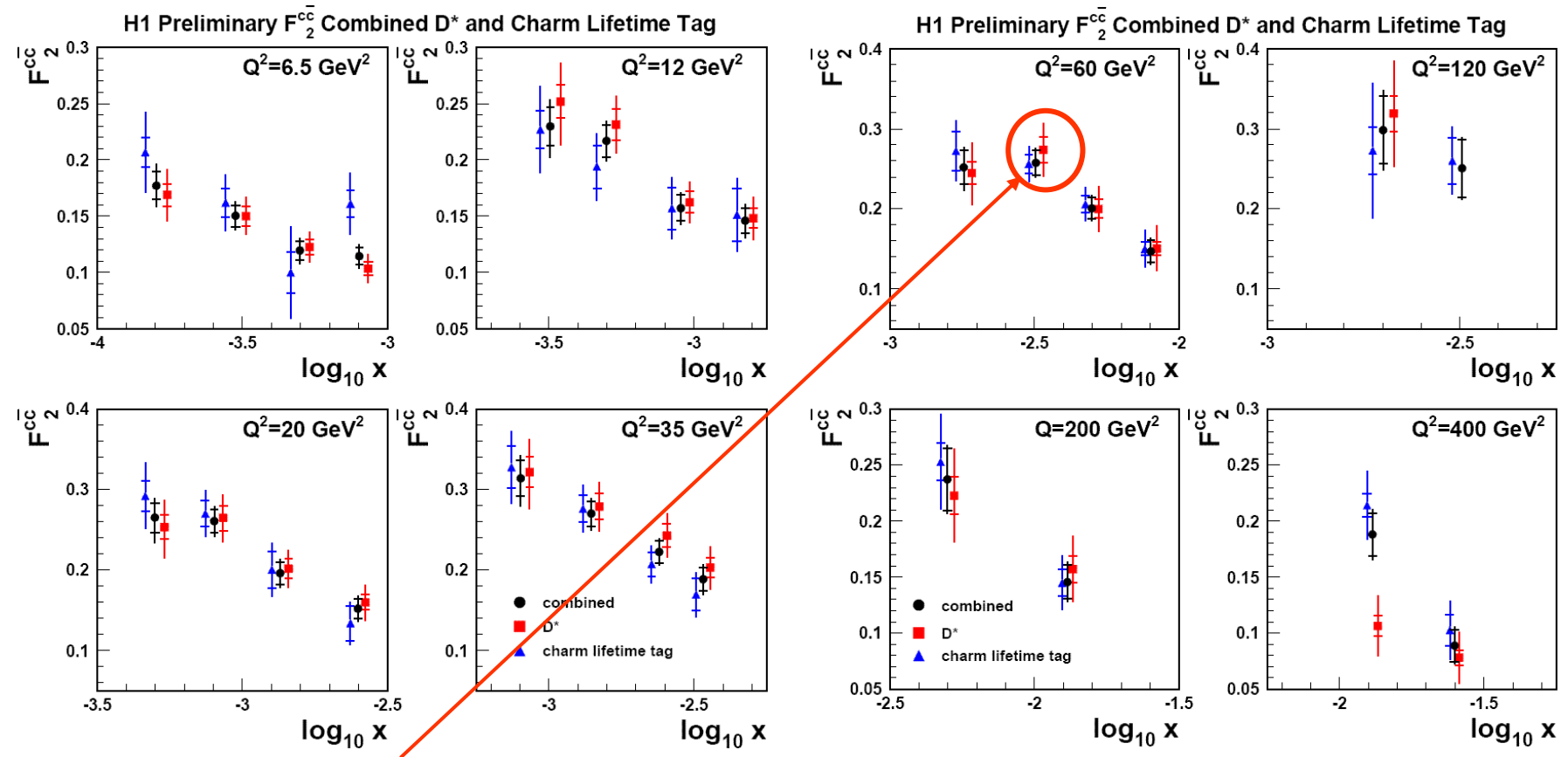
$\sigma_{\alpha_j}$  – correlated systematic error

$dM^i/d\alpha_j$  – sensitivity of data  $i$  to systematic uncertainty  $j$

$M^{i,true}$  - fitted combined data  $D^*$  + lifetime

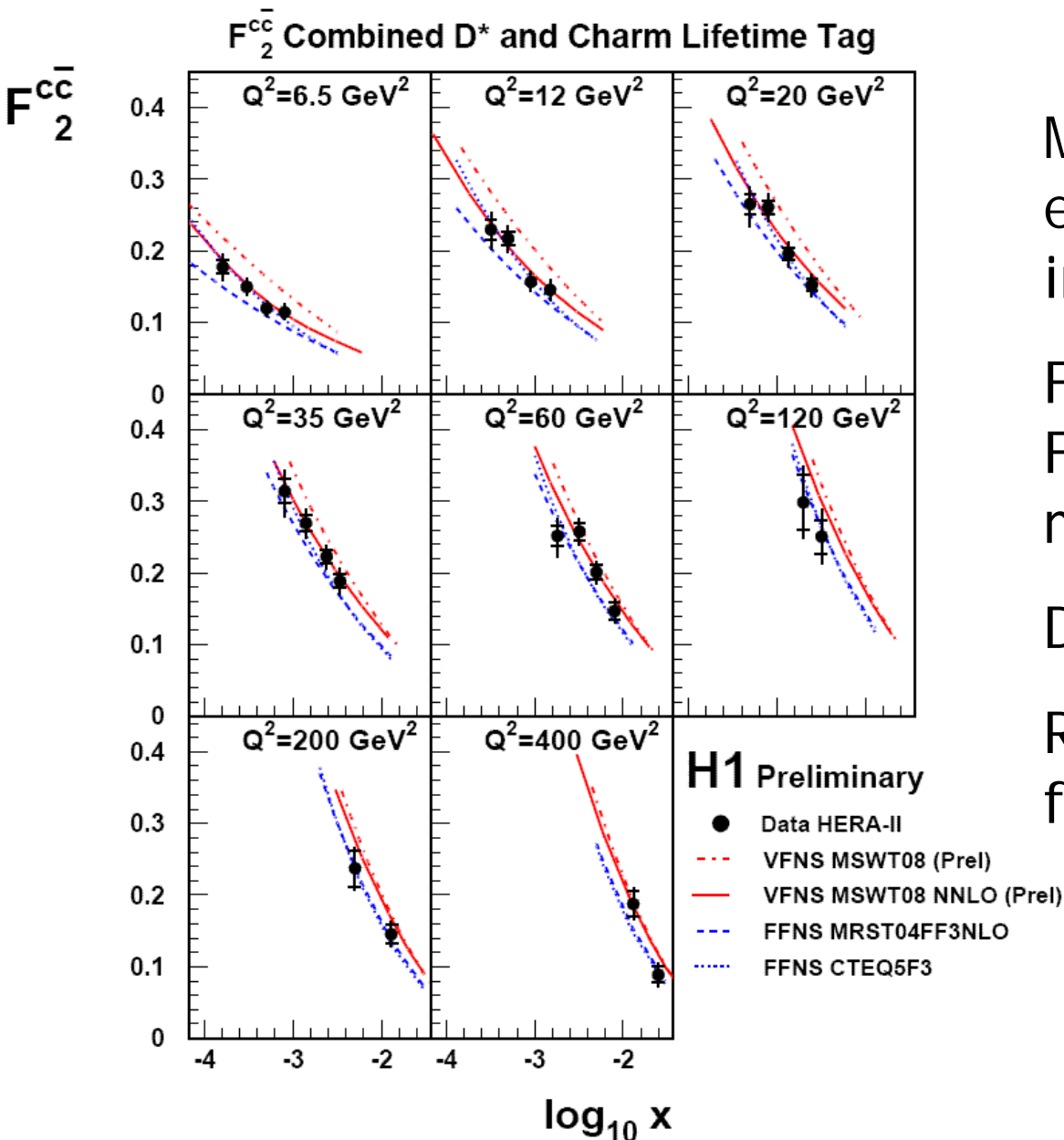
$\Delta\alpha_j$  – fitted shifts of correlated uncertainties

# Results: precision improvement



- Most gain (50%) where D\* and lifetime similar precision
- Overall improvement in precision (10-50%)
- Results stable wrt variation of systematic treatment,  $\chi^2 = 26/25$

# Results



Model dependence in extrapolation factors included in systematics

$F_2^{cc}$  can be compared with FFNS and GM VFNS models

Description reasonable

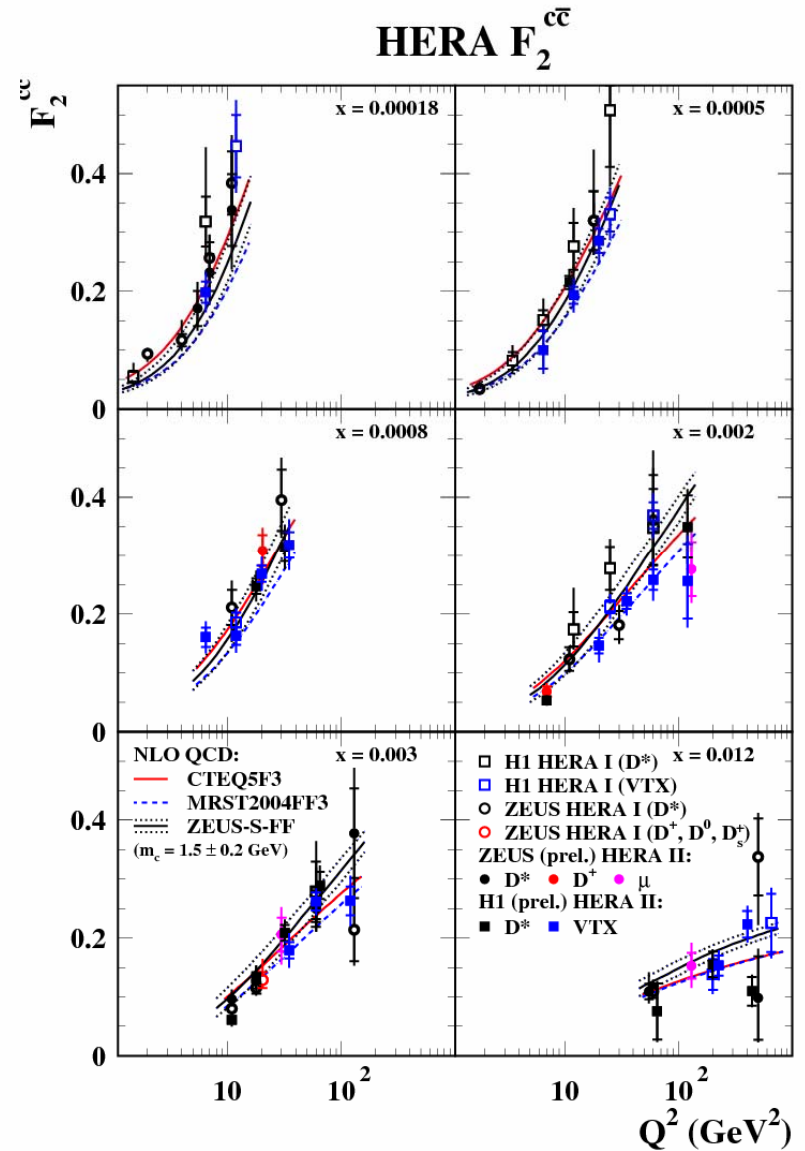
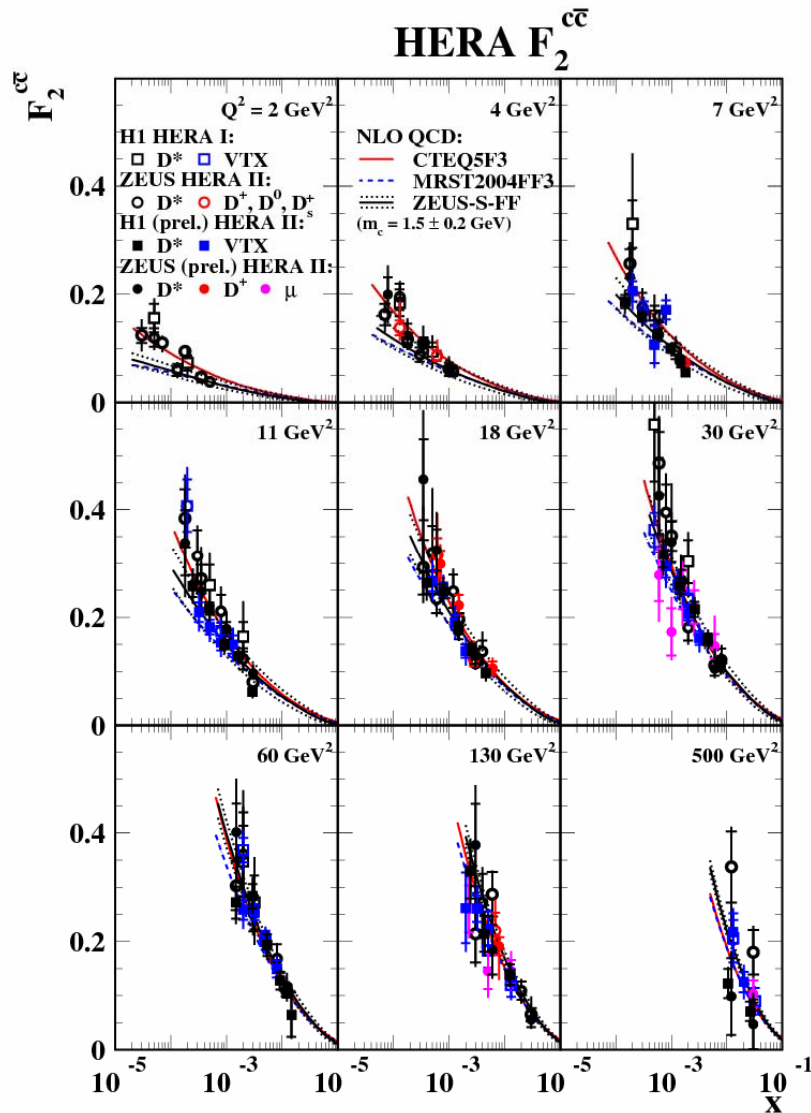
Room for improvement for some models

# Conclusions

- Presented H1 measurements of the heavy flavour content of the proton from HERA II and HERA I data
- Extraction of structure functions  $F_2^{cc}$  allows comparison of different measurement techniques
- Extra precision can be gained from combination (improvement 10-50%)
- Combination H1 + ZEUS is worked on
- Data are described by (N)NLO pQCD calculations
- Final data with improved precision (expected soon) will help to constrain theory mass treatments and PDFs for LHC era

# Back Up

# Scale Uncertainty (c)



# Scale Uncertainty (b)

