

Structure Function Measurements at HERA and their impact for the LHC



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On Behalf of the H1 and ZEUS Collaborations

2011 Lake Louise Winter Institute

The HERA Collider



World's only ep collider (Desy-Hamburg)
Data taking: Fall 1992 - June 2007

e^{\pm} (27.5 GeV) \rightarrow \star \leftarrow p (820/920 GeV)

HERA-I (1992-2000)

$L \sim 130 \text{ pb}^{-1}/\text{experiment}$

Mostly e^+p

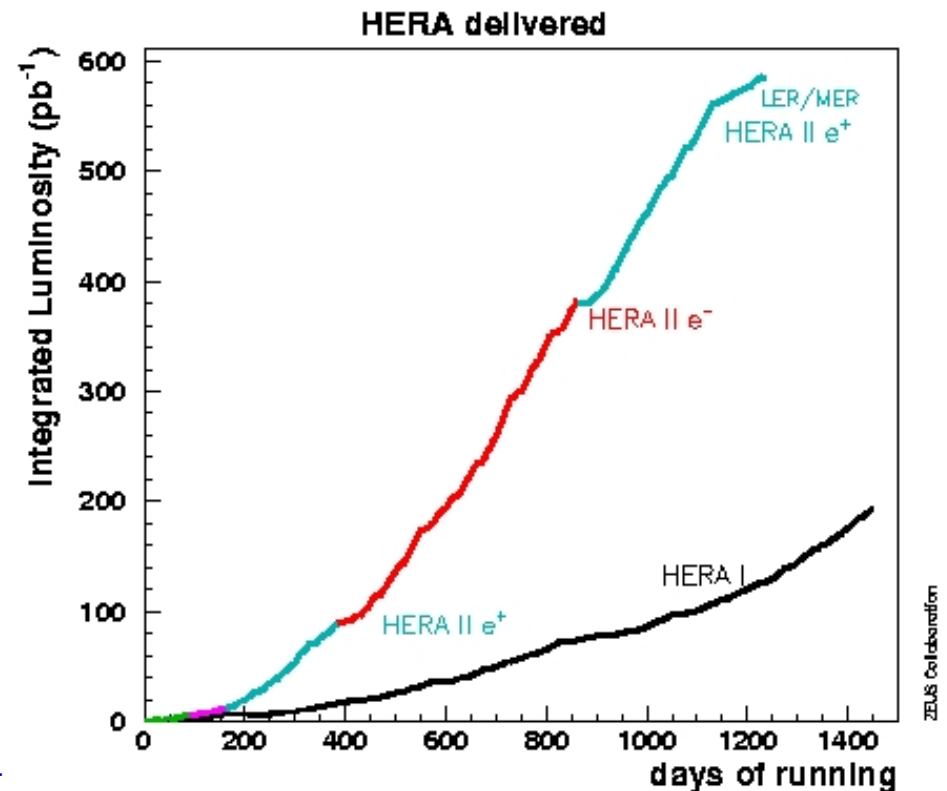
HERA-II (2003-2007)

$L \sim 360 \text{ pb}^{-1}/\text{experiment}$

Similar amounts of e^+p and e^-p

Long. polarized lepton beams ($P \sim 0.35$)

Last months: Runs at reduced \sqrt{s} for F_L



HERA and the Structure of the Proton

HERA data is our main source of knowledge on proton structure:

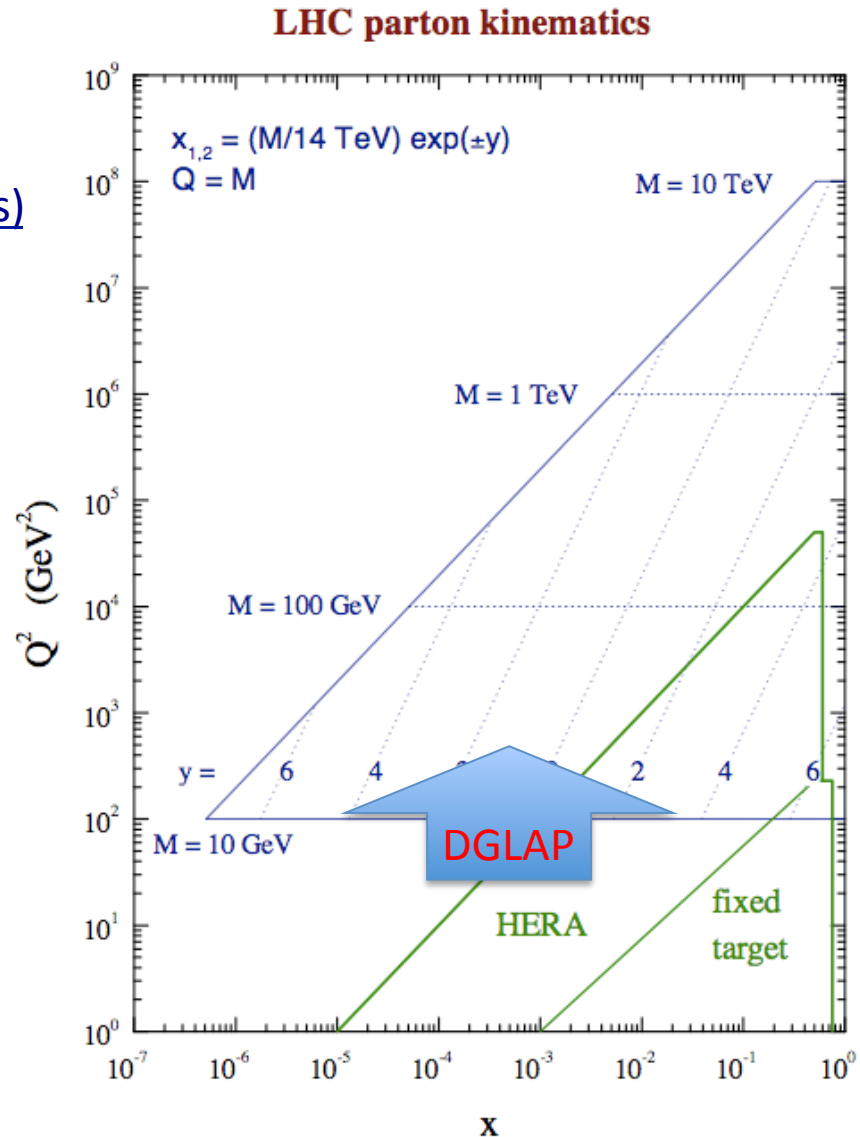
→ proton's parton distribution functions (PDFs)

Combine the H1 and ZEUS data in order to provide the most precise input to DGLAP analyses

Assume validity of (N)NLO DGLAP equations and extrapolate HERA results into the LHC region

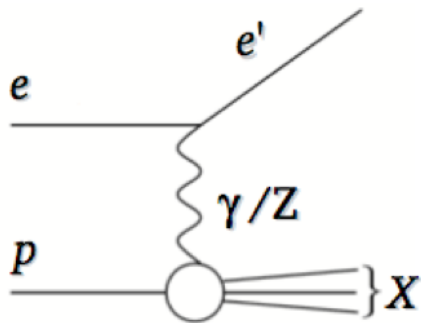
Due to QCD factorization, a very precise determination of the PDFs is crucial for:

- Very stringent tests of the Standard Model
- Searches of Physics Beyond the SM (need to control QCD Background)

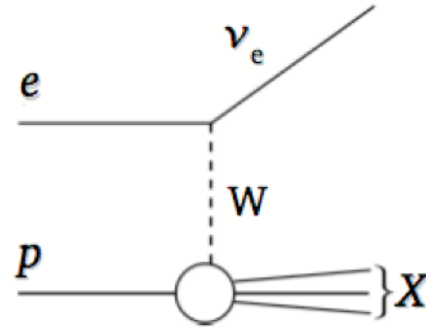


DIS processes and cross sections

NC: $e p \rightarrow e' X$



CC: $e p \rightarrow \nu_e X$



Kinematic variables:

- Virtuality exchanged boson

$$Q^2 = -q^2 = -(k - k')^2$$

- Bjorken scaling variable

$$x = \frac{Q^2}{2p \cdot q}$$

Double differential and “reduced” cross sections:

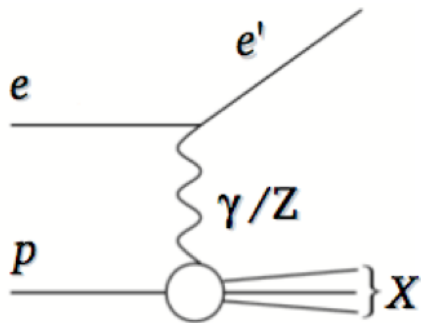
$$\text{NC: } \sigma_{r,\text{NC}}^{\pm} = \frac{d^2 \sigma_{\text{NC}}^{e^{\pm}p}}{dx dQ^2} \cdot \frac{Q^4 x}{2\pi \alpha^2 Y_+} = F_2 \mp \frac{Y_-}{Y_+} x F_3 - \frac{y^2}{Y_+} F_L$$

$$\text{CC: } \sigma_{r,\text{CC}}^{\pm} = \frac{d^2 \sigma_{\text{CC}}^{e^{\pm}p}}{dx dQ^2} \cdot \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 = \frac{1}{2} \left(Y_+ W_2^{\pm} \mp Y_- x W_3^{\pm} - y^2 W_L^{\pm} \right)$$

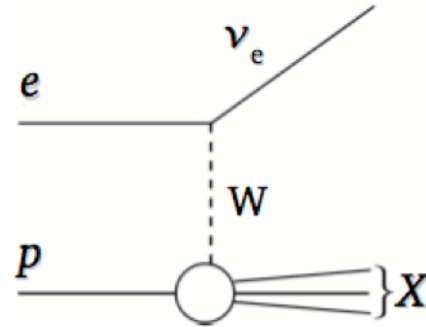
with $Y_{\pm} = 1 \pm (1 - y)^2$

DIS processes and cross sections

NC: $e p \rightarrow e' X$



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Structure Functions, PDFs and DGLAP evolution equations:

$$x^{-1} F_2(x, Q^2) = \sum_{i=q,g} \int_x^1 \frac{d\xi}{\xi} C_{2,i} \left(\frac{x}{\xi}, \alpha_s(\mu^2), \frac{\mu^2}{Q^2} \right) f_i(\xi, \mu^2)$$

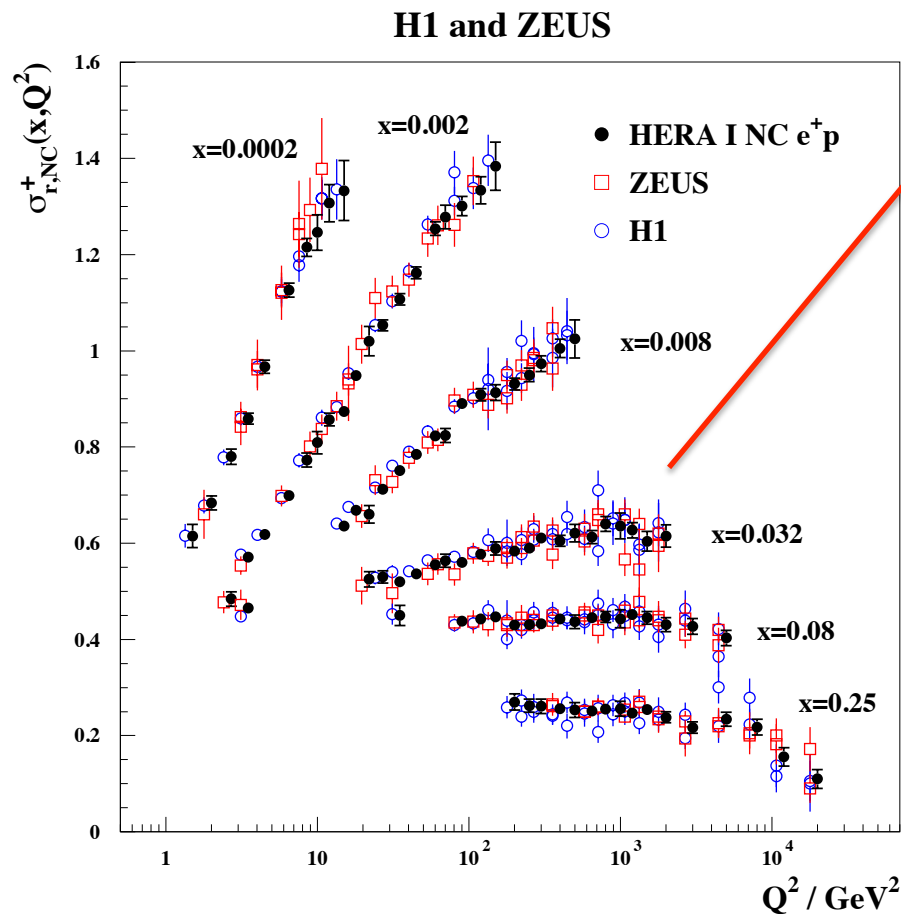
$$\frac{d}{d \ln \mu^2} f_i(\xi, \mu^2) = \sum_k \left[P_{ik}(\alpha_s(\mu^2)) \otimes f_k(\mu^2) \right] (\xi)$$

Results I will Cover

- Combination of the H1 and ZEUS data and DGLAP fits:
 - HERA-I inclusive cross sections: JHEP 1001:109(2010)
 - Precise determination of the sea quarks and gluons at mid- and low-x
 - HERA-I + $F_2(\text{charm})$ data:
 - Constraints on the charm mass and study of different heavy quarks schemes
 - HERA-I + low energy data:
 - Longitudinal structure function
 - Impact of these low-x, low- Q^2 data on PDFs
 - HERA-I+HERA-II Inclusive cross sections (high- Q^2):
 - Better determination of the valence quarks at high-x
- As an illustration of the above, will show predictions for Tevatron and LHC observables based on HERAPDFs:
 - high-Et Jets, W/Z , Higgs and top

Preliminary

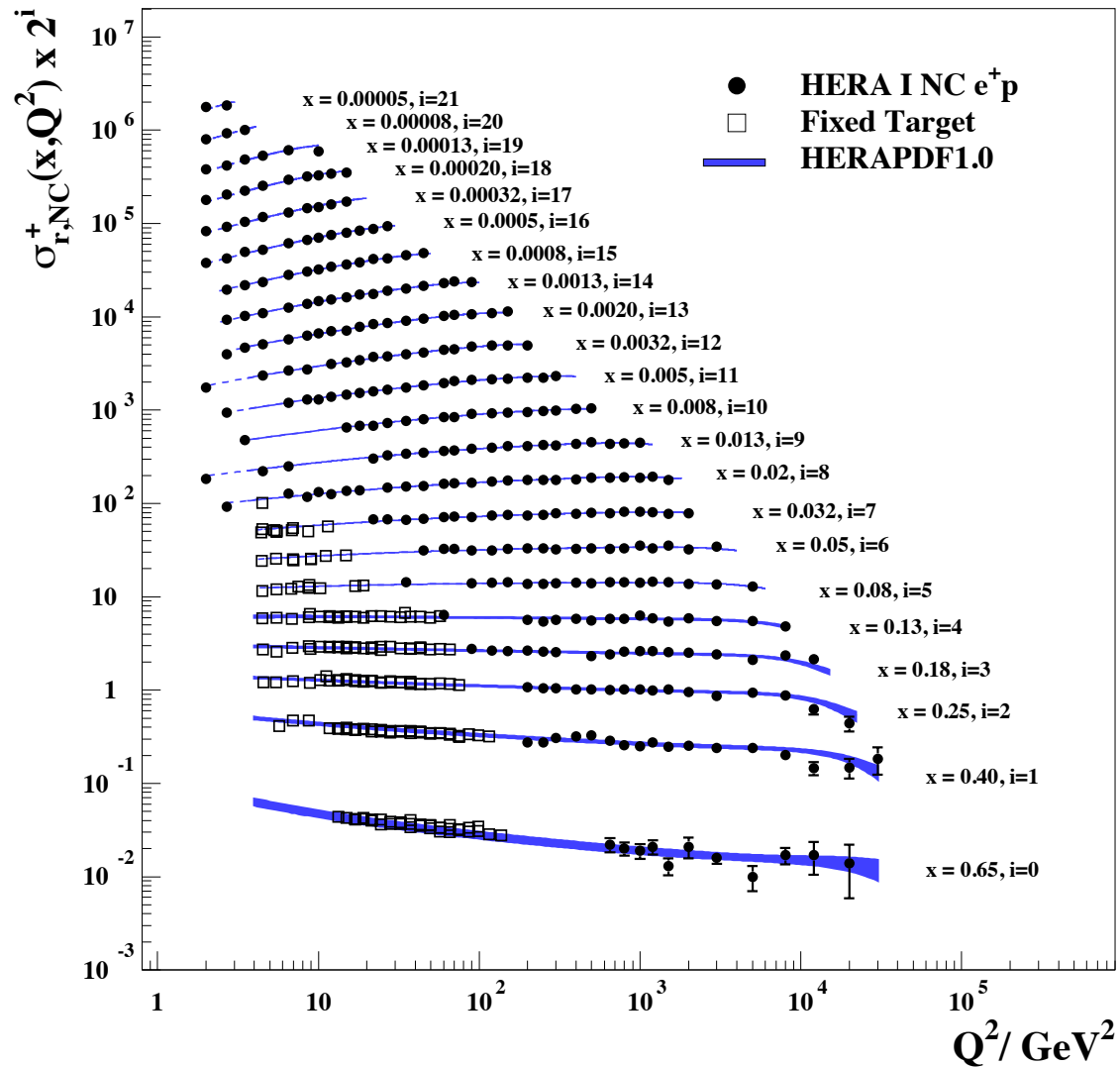
Combination of HERA I data



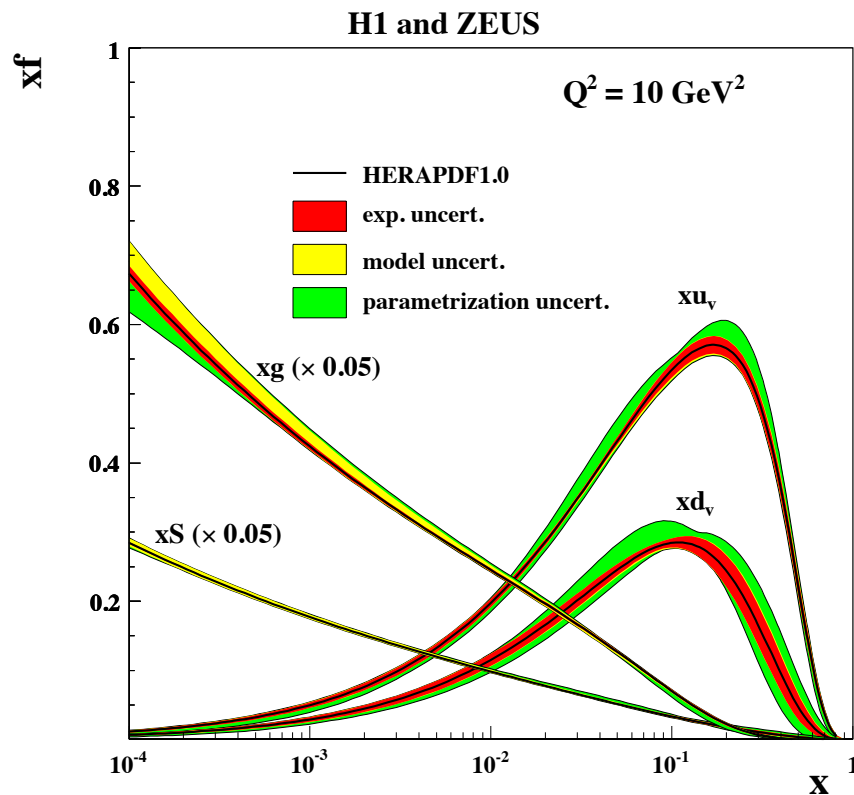
- Combined are all published HERA-I NC,CC $e^\pm p$ cross section measurements
 - 1402 data points
 - 110 syst. error sources (and correlations)
 - details on the χ^2 combination method:
 - see JHEP 1001:109(2010) [arXiv:0904.0929]
- Data show good consistency:
 - $\chi^2/\text{ndof} = 637/656$
 - small shift of global norms
 - distribution of pulls
- Experiments “cross calibrate” each other
 - 1-2% total uncert. in the low- mid- Q^2 region

Combination of HERA I data

H1 and ZEUS



DGLAP Analysis of HERA-I data: HERAPDF 1.0

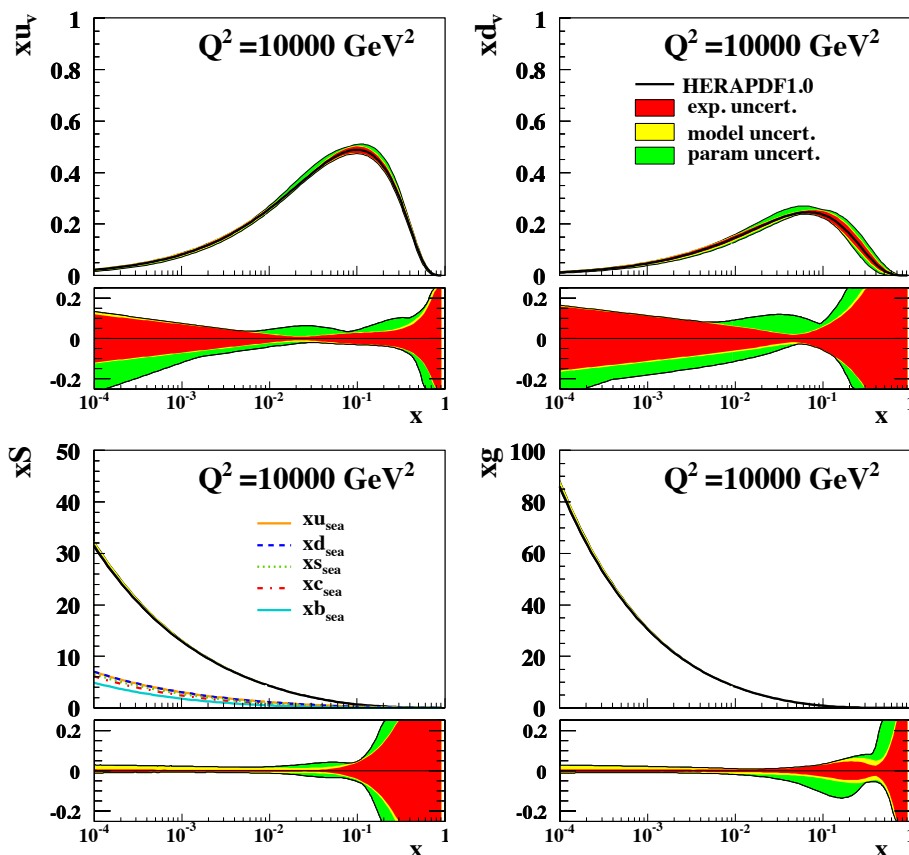


- NLO DGLAP analysis based only on the HERA-I, fully consistent, combined dataset:
 - no need for heavy target/deuterium corrections or strong isospin assumptions
 - $\chi^2/\text{ndof} = 574/582$
- Massive treatment for heavy flavours (RT-VFNS)
- Detailed study of uncertainties:
 - experimental, model and parametrisation

The very precise HERAPDF1.0 set is available in LHAPDF since v5.8.1

DGLAP Analysis of HERA-I data: HERAPDF 1.0

H1 and ZEUS



Experimental uncertainty:

Consistent data set \rightarrow use $\Delta\chi^2=1$

Model Uncertainty:

Following variations were considered

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c [GeV]	1.4	1.35 ^(a)	1.65
m_b [GeV]	4.75	4.3	5.0
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.5 ^(b)	2.5 ^(c,d)

Parametrization uncertainty:

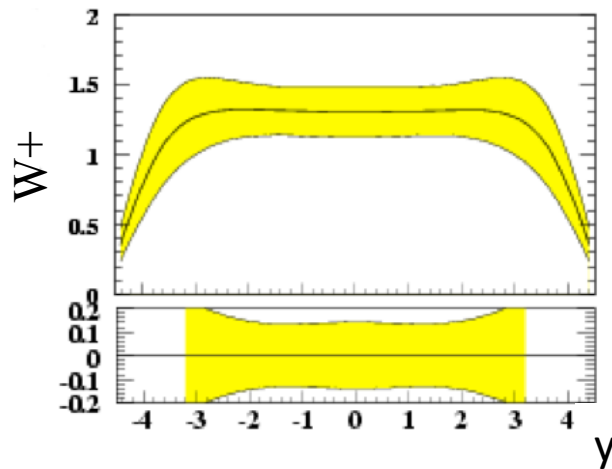
Envelope from DGLAP Fits using variants of the parametrisation form at Q_0^2

$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

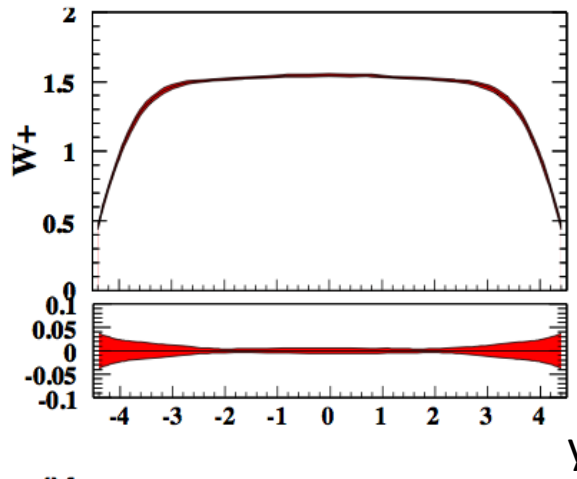
At the scale $Q^2=10\,000\text{ GeV}^2$ (relevant to LHC)
the sea and gluon densities are known at the % level for $x \leq 10^{-1}$

W and Z production at the LHC

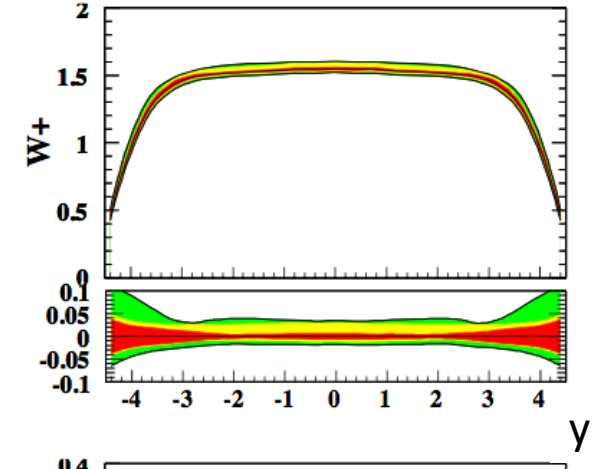
$\sqrt{s}=14$ TeV



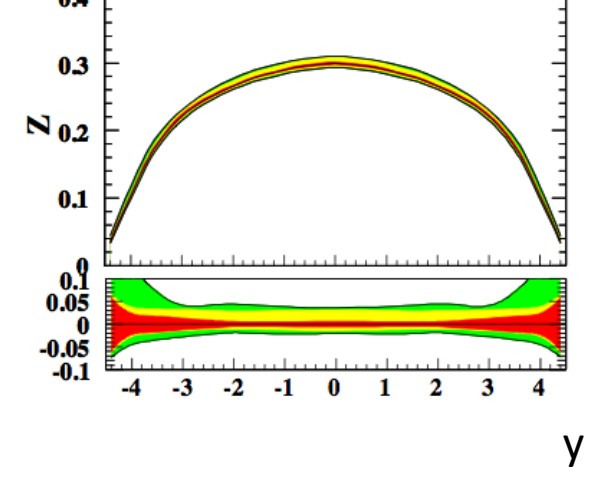
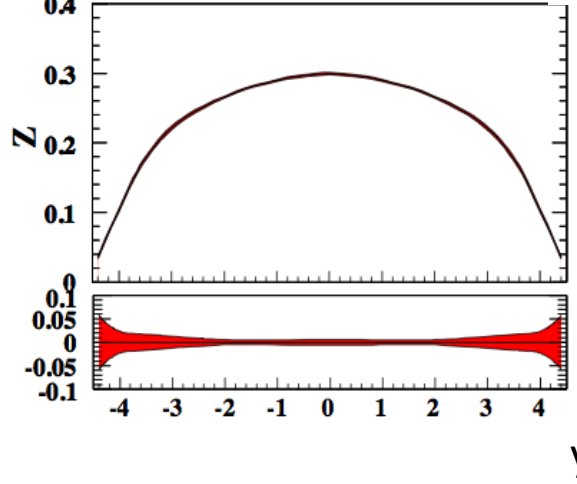
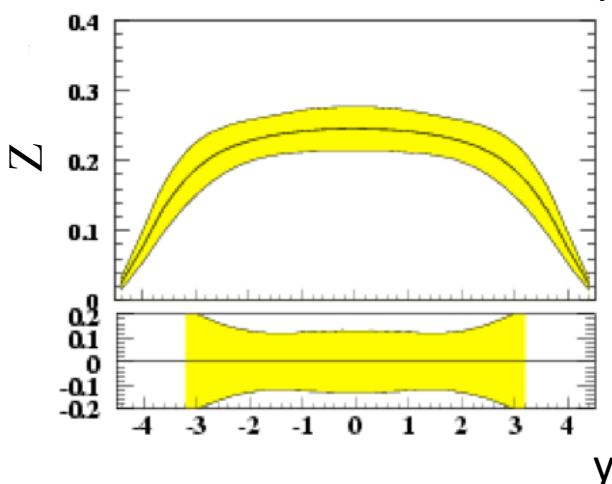
Without HERA data (exp. only)
~15% uncertainty



HERAPDF1.0 (exp. only)
~ 1% uncertainty!

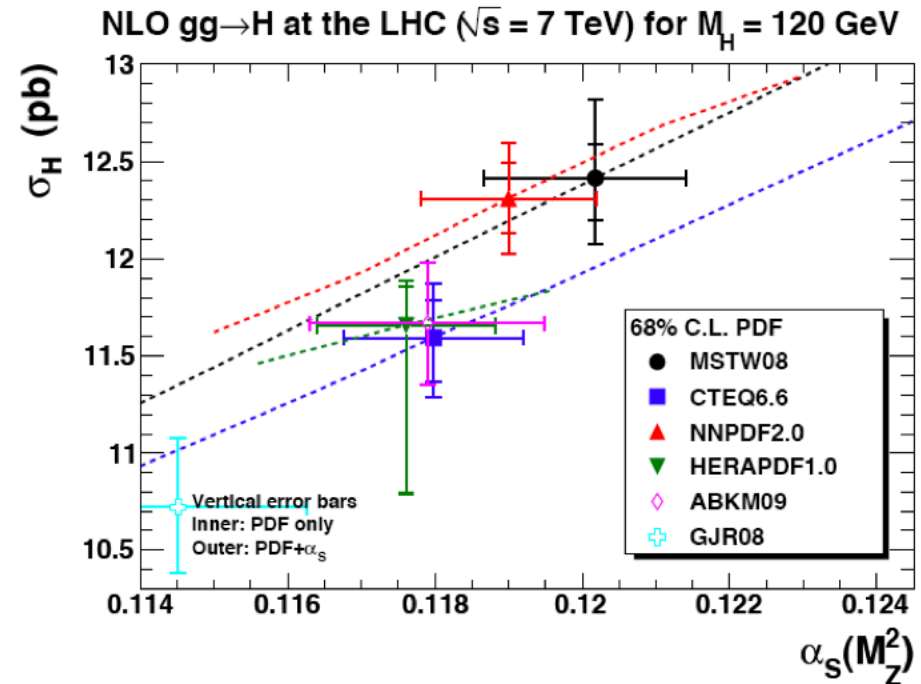
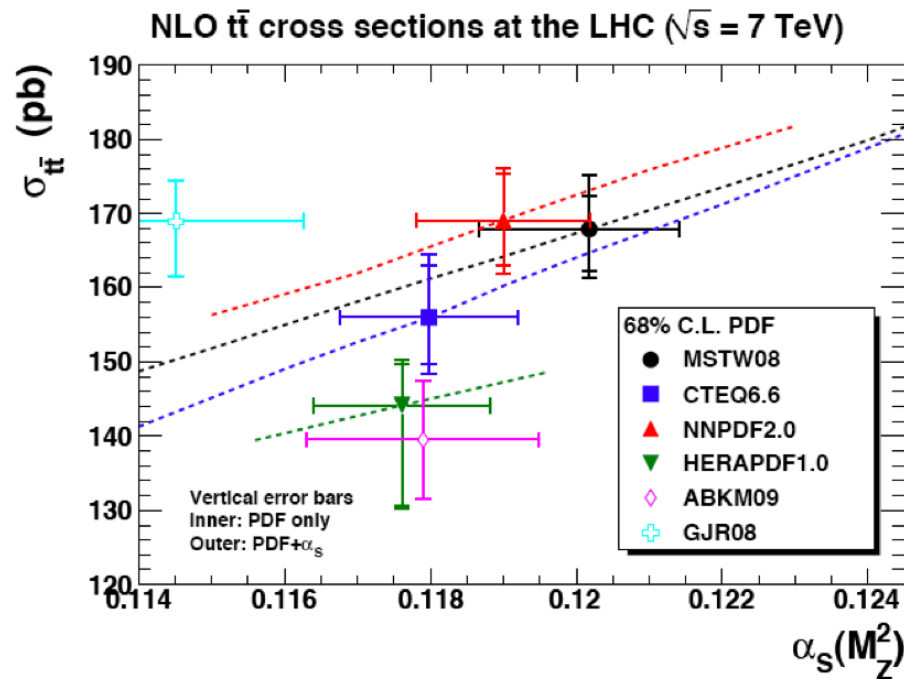


HERAPDF1.0 (total)
~ 5% uncertainty



Benchmarking PDFs: LHC cross sections

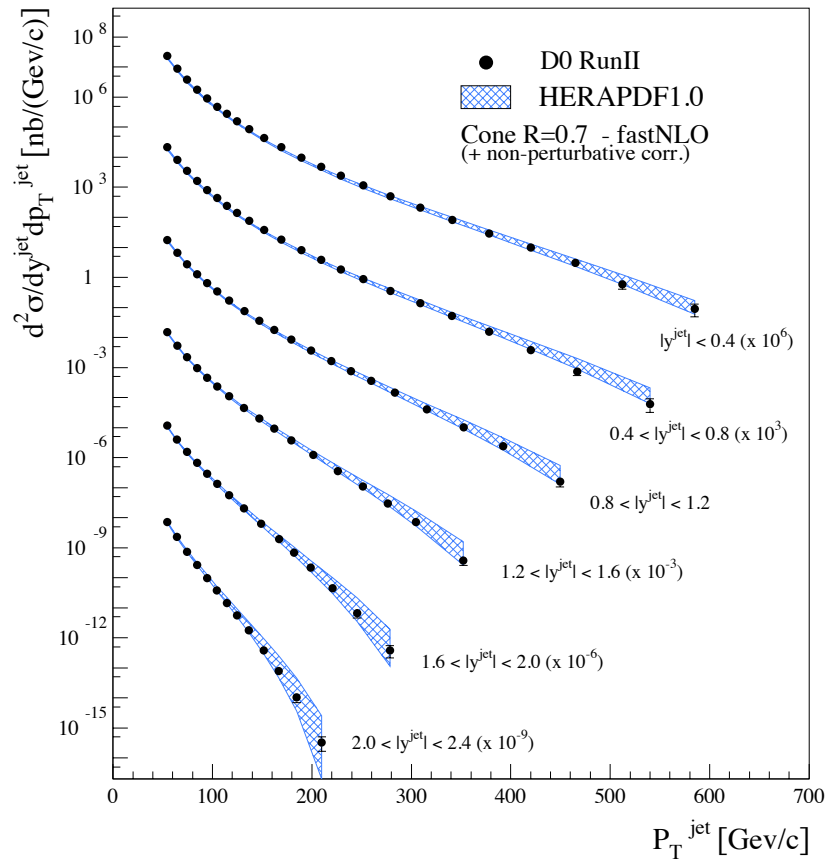
e.g. gluon-gluon dependent cross sections such as Higgs and $t\bar{t}$



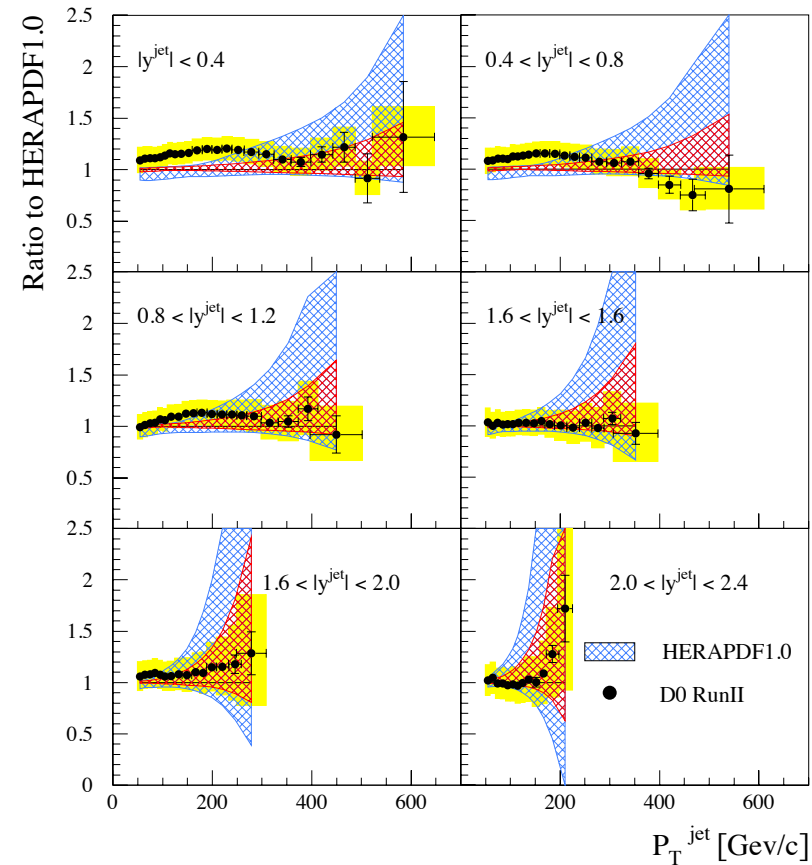
- HERA experiments fully involved in this benchmark activity
- HERAPDF1.0 provides realistic uncertainty for LHC cross sections
(often dominant parameterization uncert. not accounted for in most global fit groups)

HERAPDF1.0 and Tevatron jets

Tevatron Jet Cross Sections



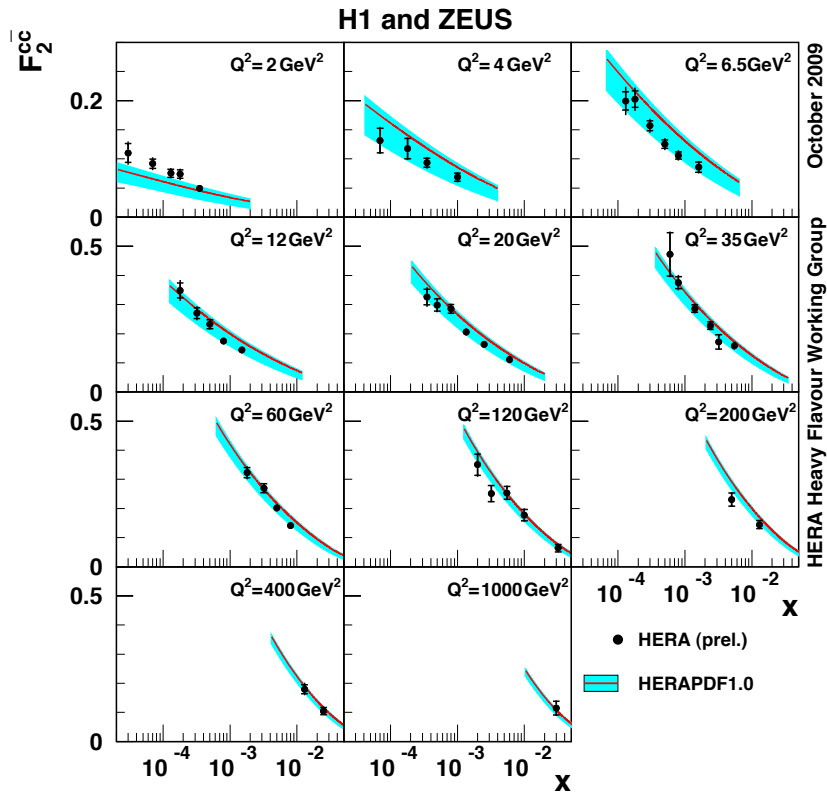
Tevatron Jet Cross Sections



- Predictions based on HERAPDF1.0 agree with Tevatron results
- Test PDF universality and collinear factorization
- Similar results for W/Z production (not shown)

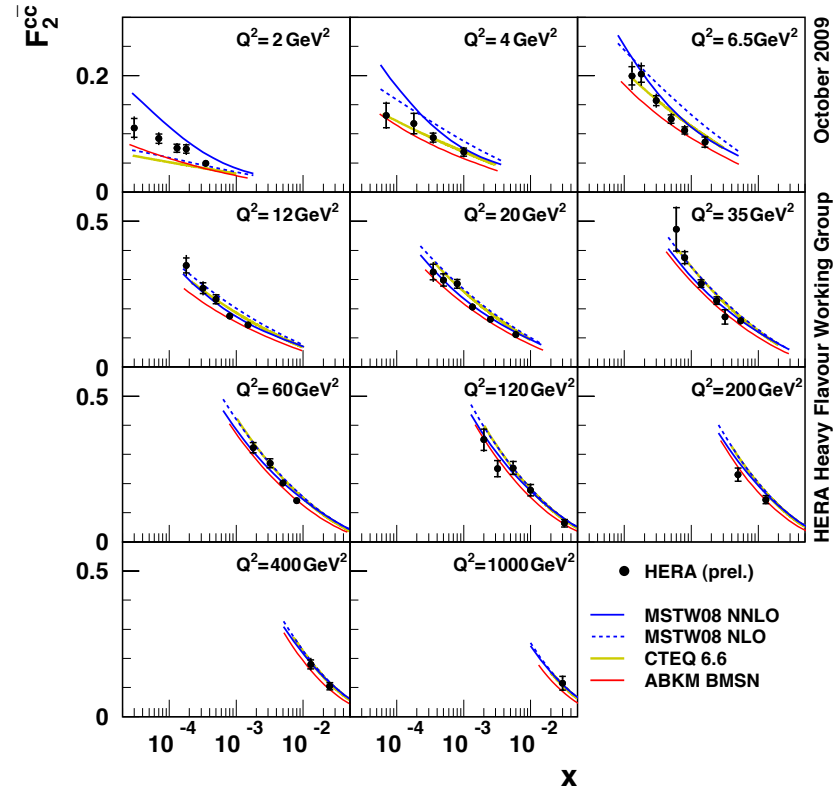
F_2^{charm} at HERA

Combine H1 and ZEUS charm data:



Reasonable agreement with QCD prediction, based on HERAPDF1.0, when accounting for uncertainty on m_c

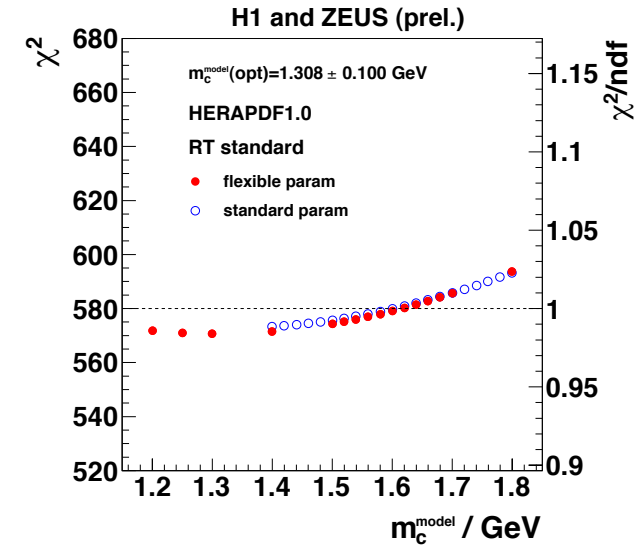
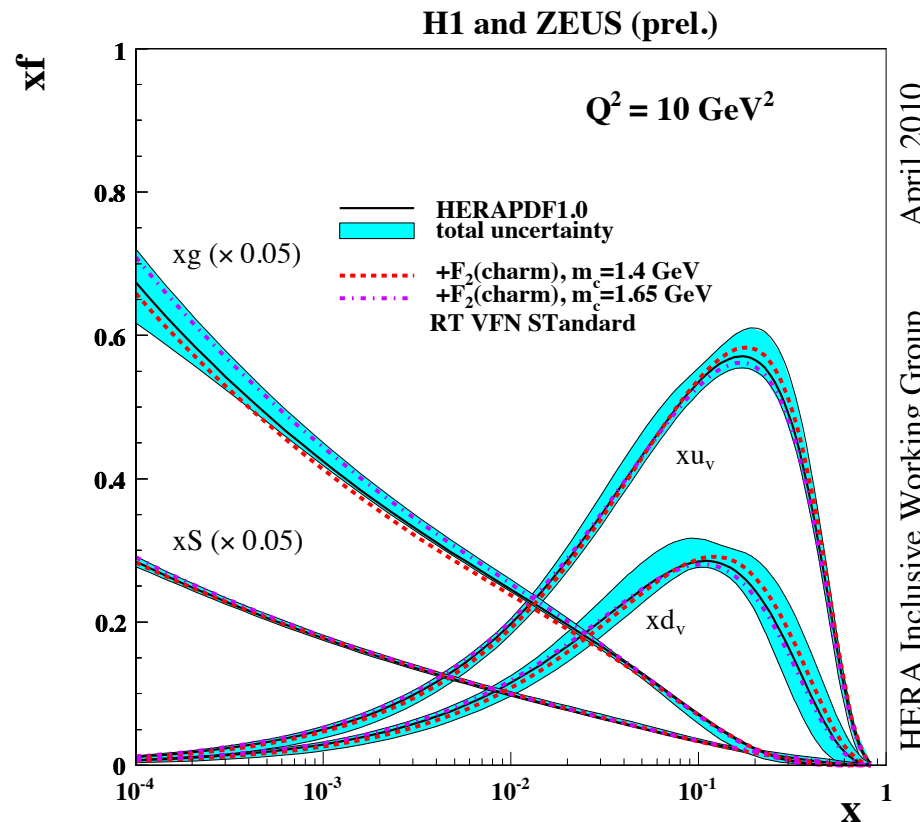
Uncertainty band: $1.35 < m_c < 1.65 \text{ GeV}$



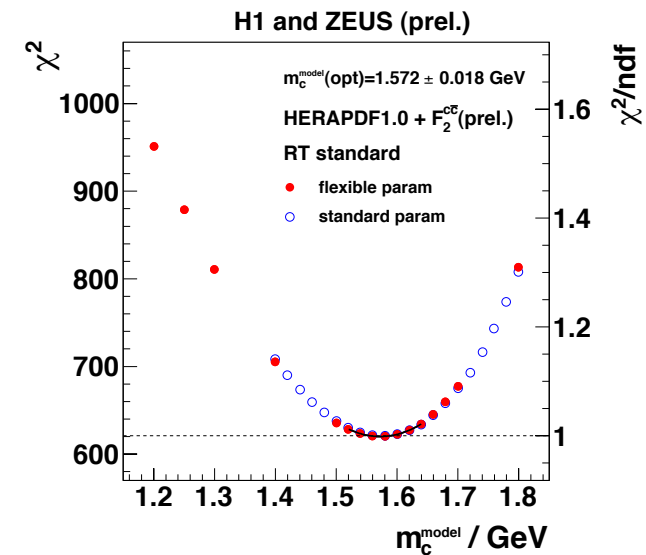
Precision of the combined measurements (5-10%) such that we can start to study differences among General Mass Variable Flavour Number Schemes (GM-VFNS)

Including charm data in the HERAPDF fit

...does not change PDF significantly
but increases sensitivity to charm mass

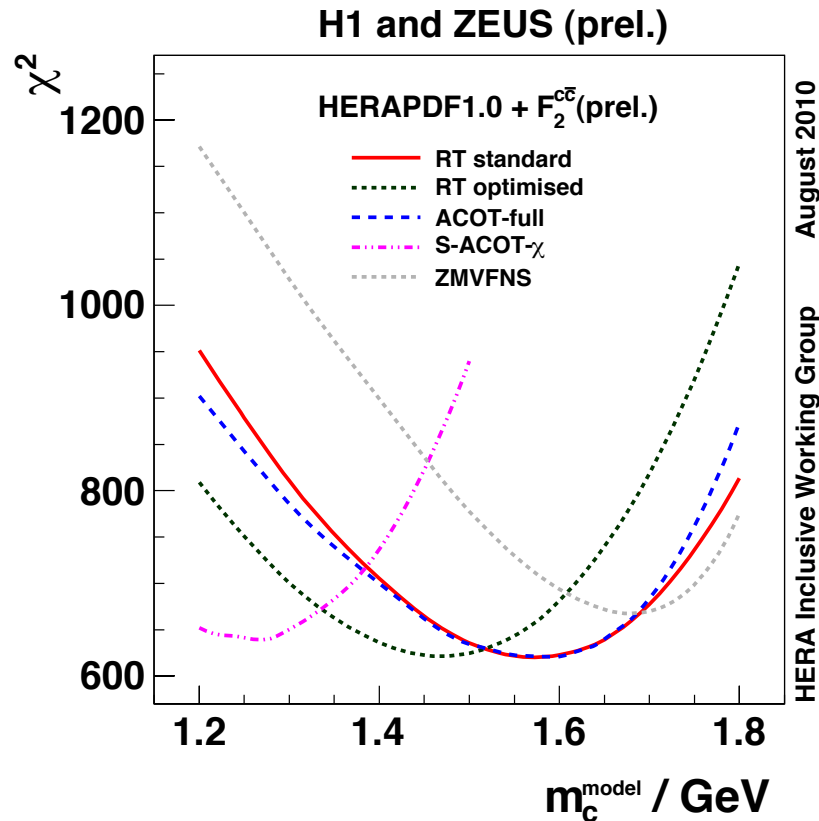


without charm

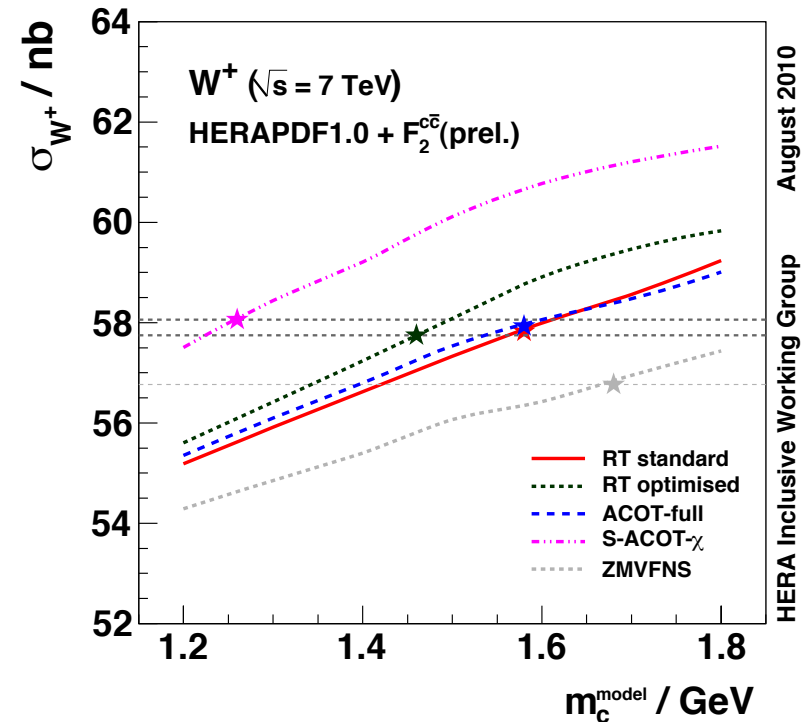


with charm

Charm, VFNS schemes and W predictions at LHC



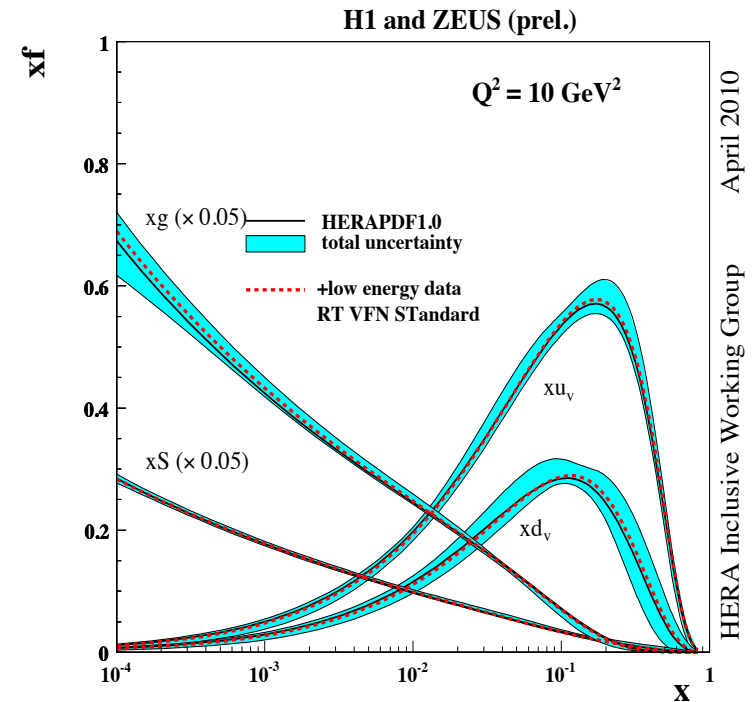
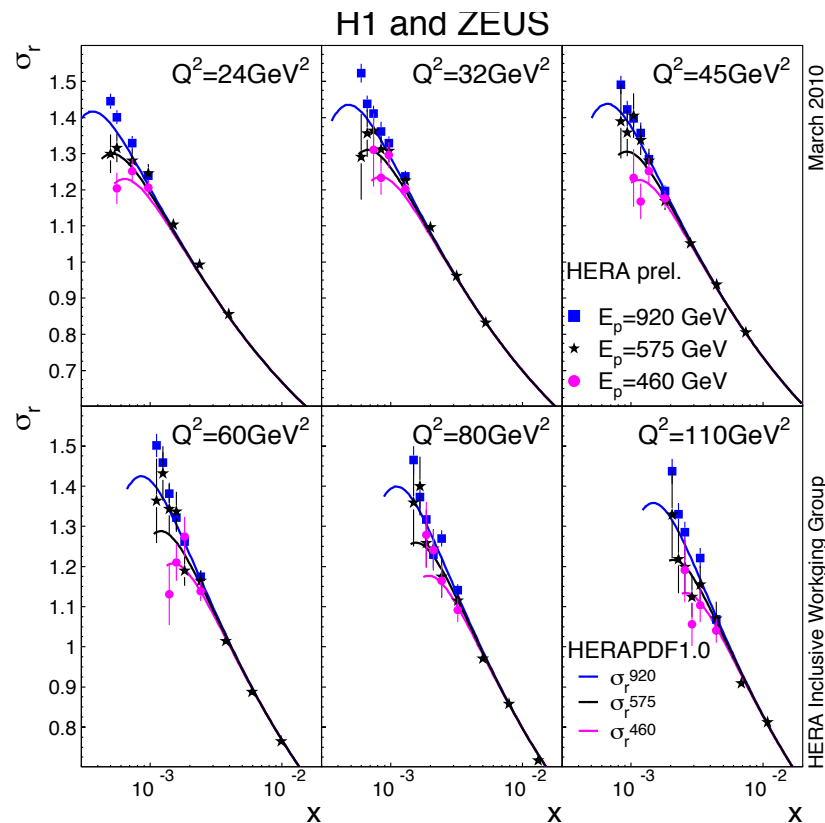
Different “optimal” effective masses
for different GM-VFNS yield very similar fits



If a fixed “optimal” mass value is considered
then the spread is still considerable ($\sim 7\%$)
but if each prediction is taken at its own
optimal value the spread among predictions
is reduced to 1% (2% considering ZM-VFNS)

Adding low energy data

Add to HERA-I combined results
measurements @ $E_p = 920, 575, 470$ GeV

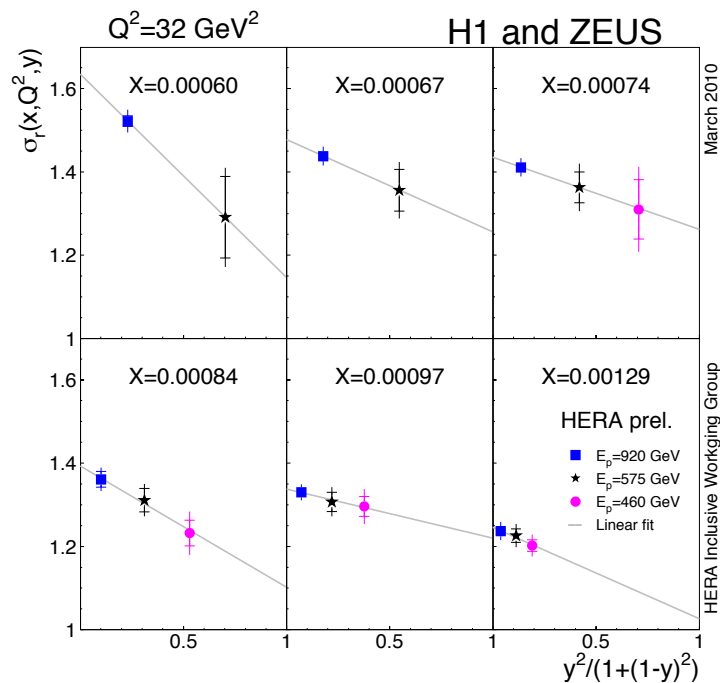


PDFs from new fit agree well with
HERAPDF1.0

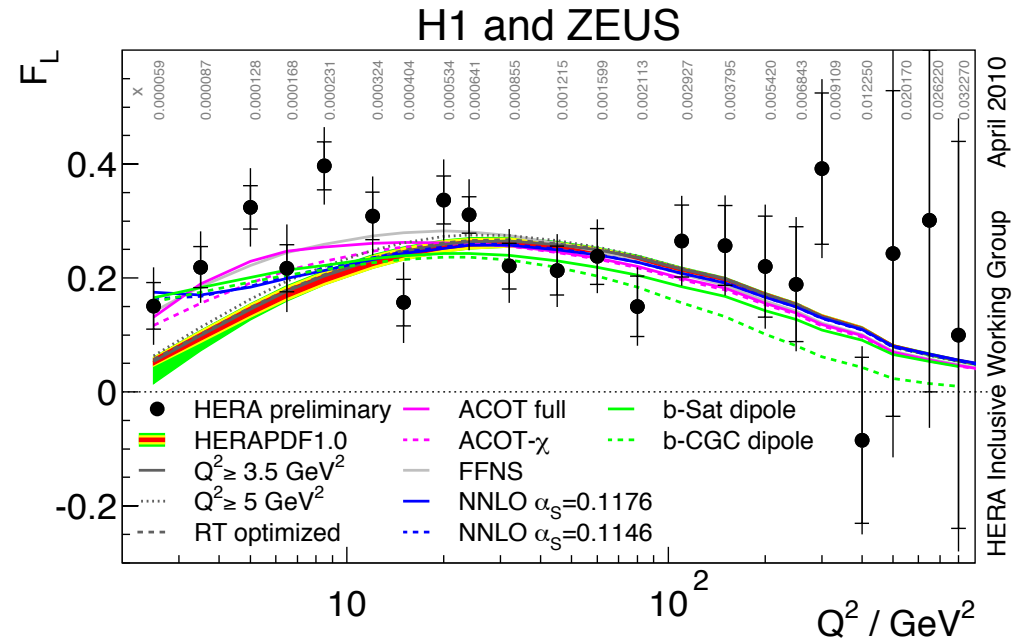
..but worse χ^2/ndof at low Q^2 and x

Longitudinal Structure Function

$$\sigma_r = F_2(x, Q^2) - \frac{y^2}{1 + (1 - y)^2} F_L(x, Q^2)$$



Determine F_2 and F_L simultaneously from a simple linear fit



Combined F_L in general consistent with HERAPDF1.0 but at low Q^2 , the QCD prediction tends to underestimate the measurements.

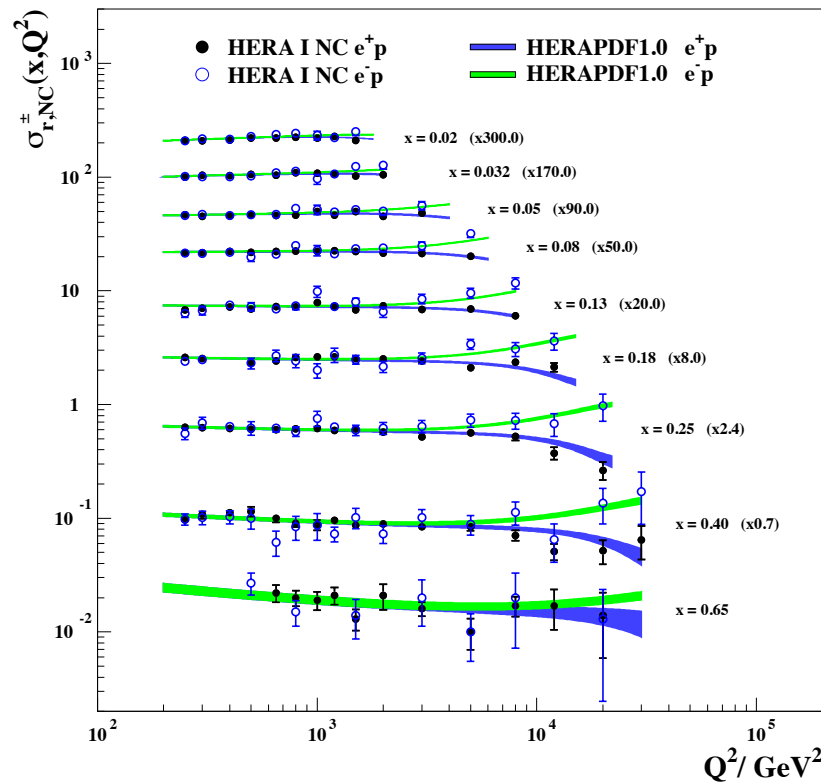
Using NNLO or different heavy flavour schemes may help to improve description

HERA-II High- Q^2 Data: NC $e^\pm p$

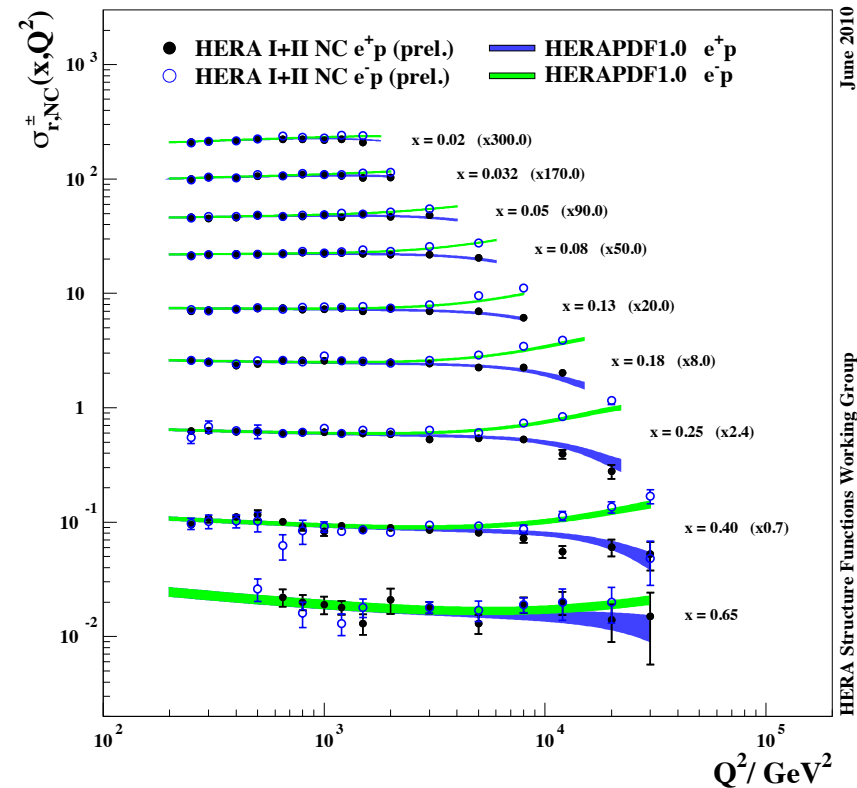
HERA-I combined results

HERA-I + HERA-II combined results

H1 and ZEUS



H1 and ZEUS



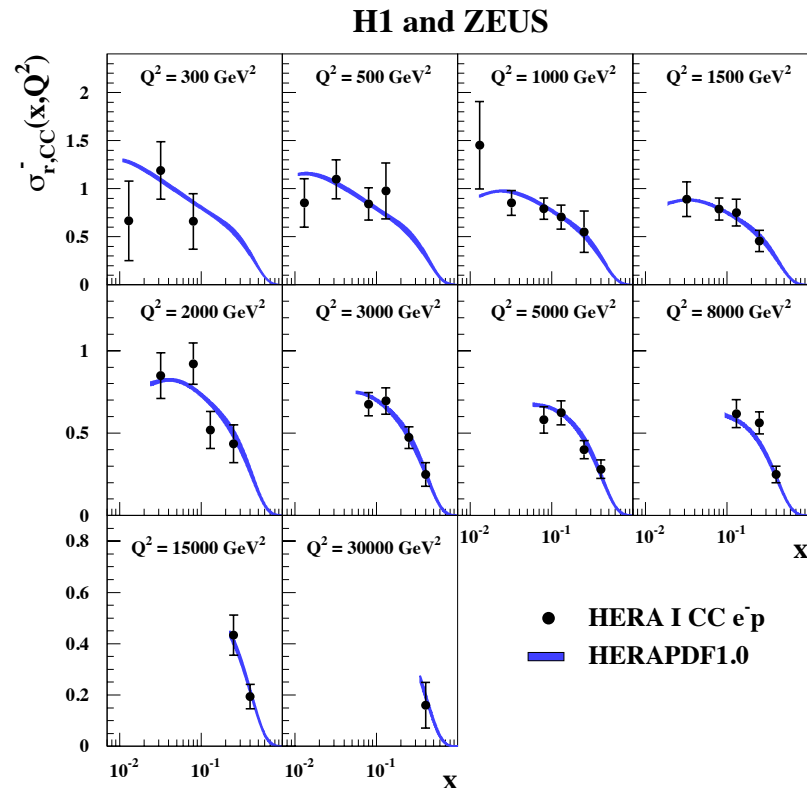
June 2010

HERA Structure Functions Working Group

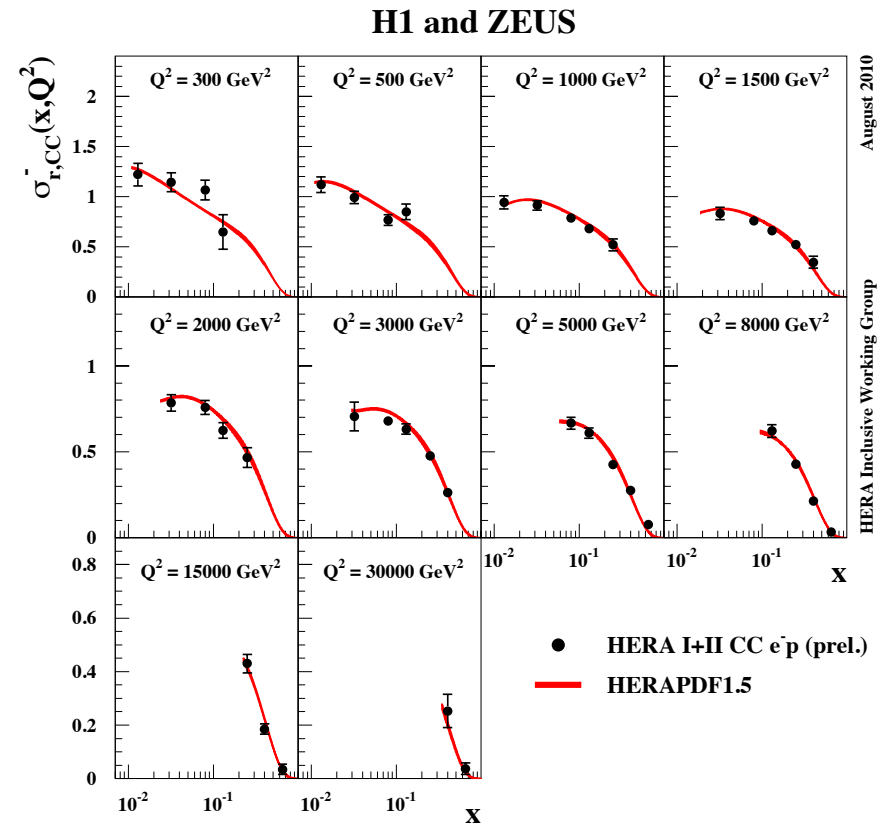
New HERA-II measurements: increased precision at high- Q^2

HERA-II High- Q^2 data: CC e^-p

HERA-I combined results



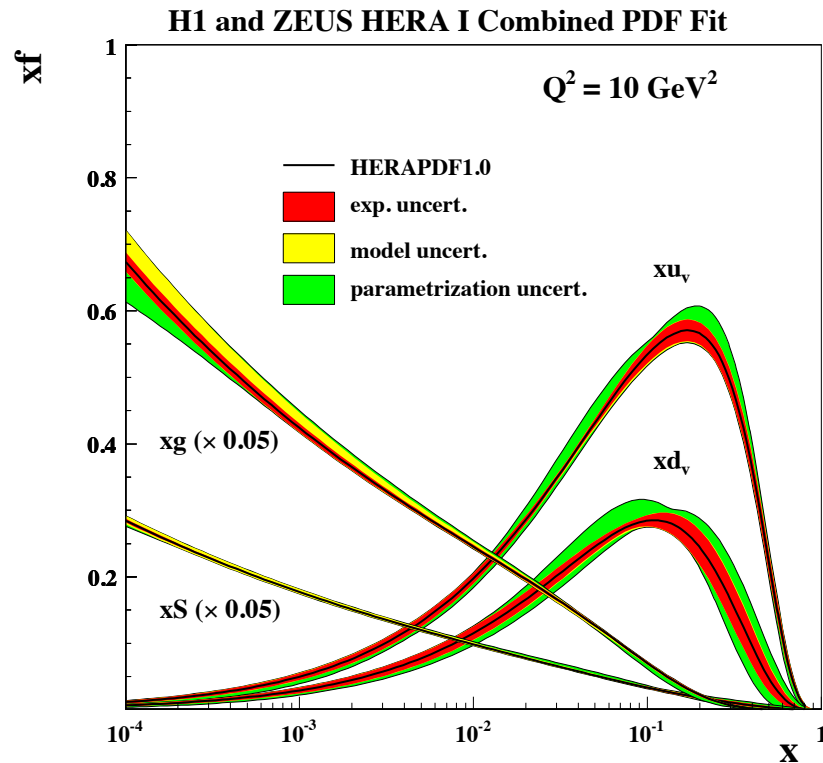
HERA-I + HERA-II combined results



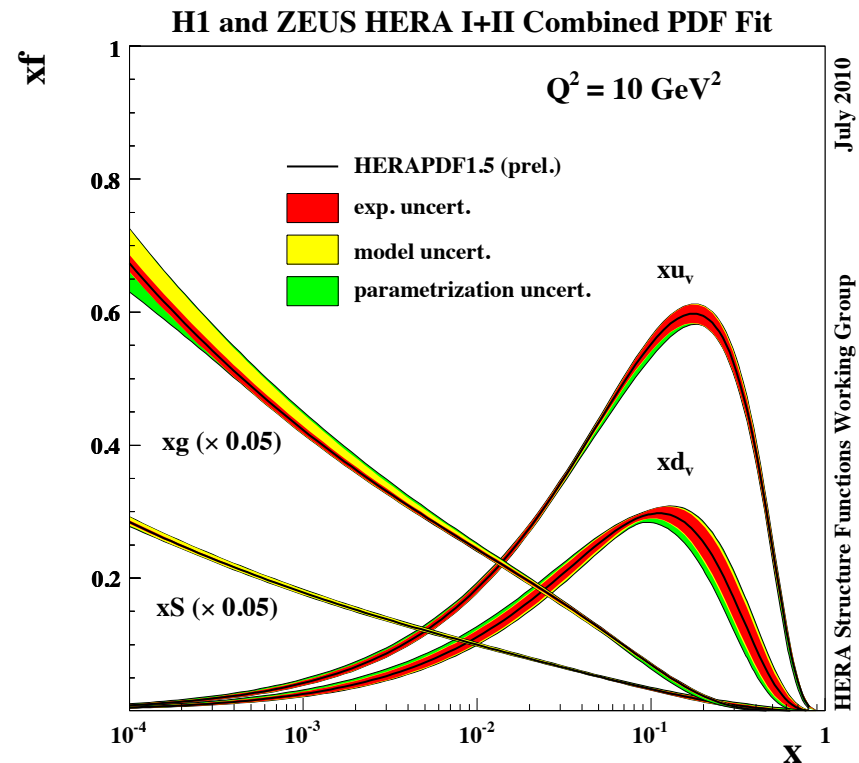
New HERA-II measurements: increased precision at high- Q^2

HERAPDF1.0 vs HERAPDF1.5

HERA-I / HERAPDF1.0



HERA-I+II / HERAPDF1.5



Impact on valence quarks: much better constrained at mid and high-x

Summary

HERA remains our main source of information on proton structure

Recent combined results of the H1 and ZEUS Collaborations have allowed to determine proton's PDFs with an unprecedented precision

Most of the improvements in the understanding of the PDFs, described here, are very relevant for the physics program of the LHC

Many results still to come (NNLO PDFs, new DGLAP analyses based on the full HERA-II data samples and new heavy flavour results).
Stay tuned!

For additional information and results please refer to:
https://www.desy.de/h1zeus/combined_results/