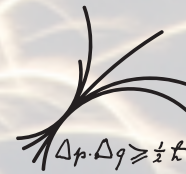
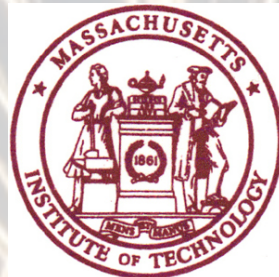


PDFs & $\alpha_s(M_Z)$ from Inclusive and Jet Measurements in DIS @ HERA

Günter Grindhammer, MPI für Physik, München



PANIC,



Cambridge, MA, July 24-29, 2011

Rutherford Centennial & MIT Sesquicentennial



on behalf of the H1 and ZEUS collaborations

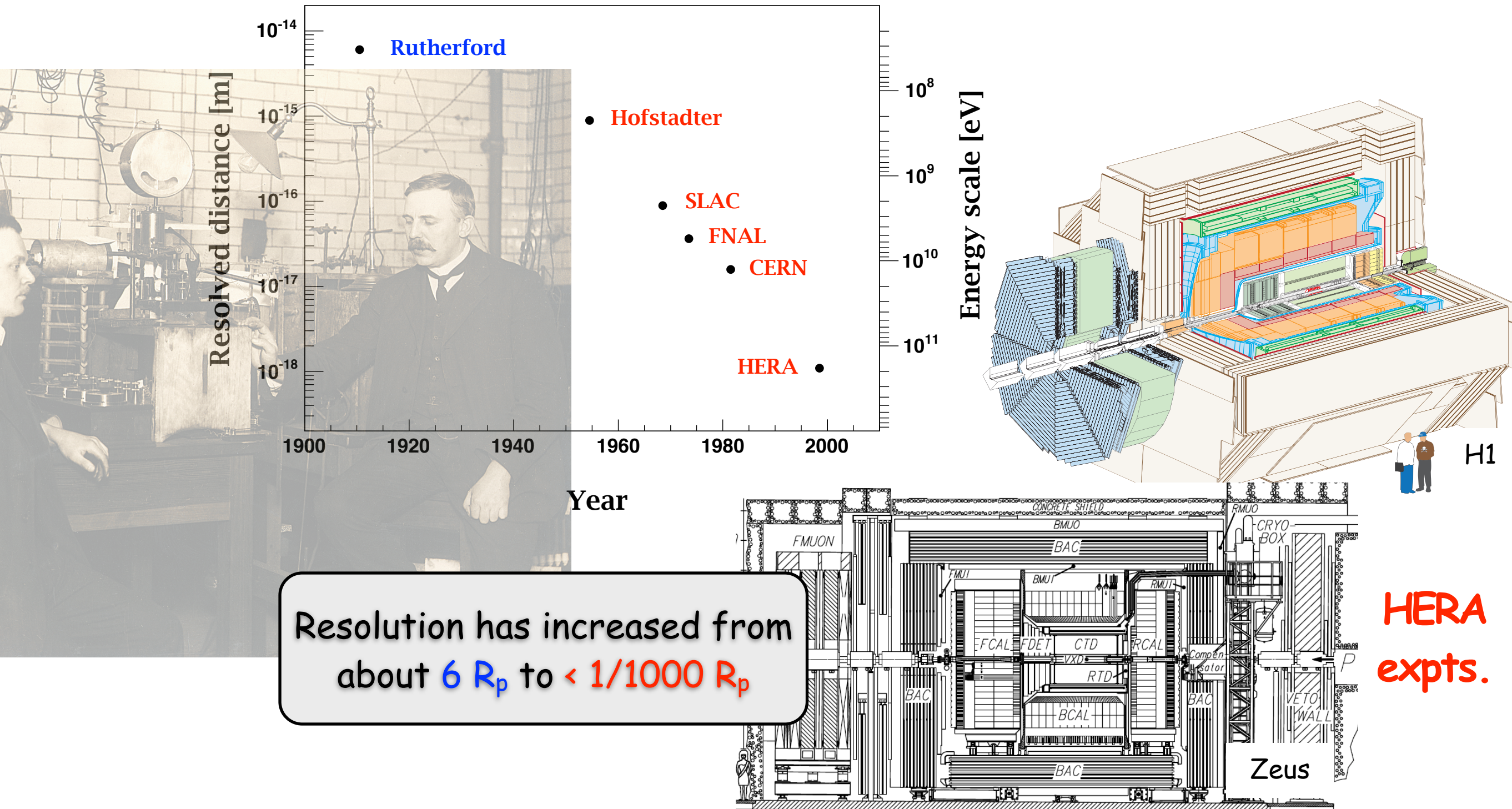


- introduction
- HERAPDFs
- data: inclusive & jet cross sections
- results

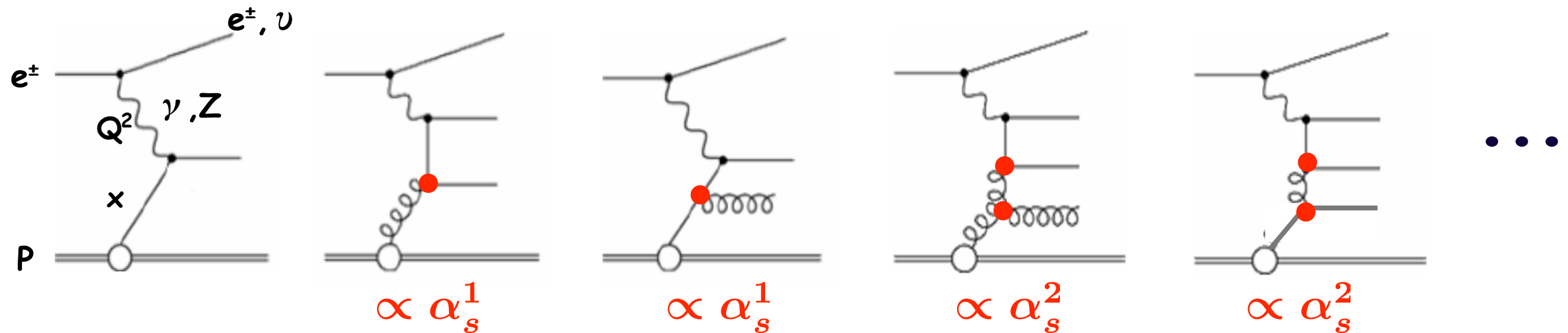


From Rutherford to HERA

Celebrating the Rutherford centennial



Physics of inclusive DIS & jets



inclusive DIS: $\sigma \propto q(x, \mu_f)$

in LO

jets in DIS in the Breit frame: $\sigma_{\text{jet}} \propto \alpha_s(\mu_r)(c_g g(x, \mu_f) + c_q q(x, \mu_f))$

α_s and gluon are strongly correlated in fits to inclusive data alone, because sensitivity to the gluon only enters in NLO (scaling violations).

jet data are sensitive to α_s and gluon already in LO and together with inclusive data can reduce the strong correlation.

HERAPDFs

- idea: use only HERA data (combined H1 & ZEUS) in the PDF fits
 - precise data set with total uncertainties between 1-2% over most of the phase space
 - systematic correlated and uncorr. uncertainties well controlled, allowing for $\Delta \chi^2 = 1$ uncertainty criterion
 - $e^\pm p$ data only, i.e. no need for deuterium corrections and heavy target corrections
 - for central fit use parametrizations with minimum number of parameters
 - param. uncertainty \Rightarrow vary number of parameters (and parametrization) and Q_0^2 , the starting scale of the parametrizations (default = 1.9 GeV^2)
 - model uncertainty \Rightarrow vary m_c , m_b , f_s , Q_{\min}^2 (defaults: 1.4 GeV , 4.75 GeV , 0.31 , 3.5 GeV^2)

HERAPDF parametrizations I

- $x \cdot uv$, $x \cdot dv$, $x \cdot Ubar$, $x \cdot Dbar$ and $x \cdot g$ are parametrized according to:

$$xf(x, Q_0^2) = Ax^B (1-x)^C (1 + Dx + Ex^2 + \epsilon\sqrt{x})$$

- starting scale $Q_0^2 = 1.9 \text{ GeV}^2$ (below m_c), NLO DGLAP evolution (RT-VFNS)
- constraints:
 - momentum sum rules, quark sum rules
 - $x \cdot sbar = f_s x \cdot Dbar$ strange sea is a fixed fraction f_s of $Dbar$ at Q_0^2
 - $B_{Ubar} = B_{Dbar}$ and $B_{uv} = B_{dv}$
 - $Sea = 2x \cdot (Ubar + Dbar)$
 - $Ubar = Dbar$ at $x=0$
- 10 free parameters are used up to HERAPDF1.5 fitting HERA-1 data:
 - $B_g, C_g, B_{uv}, C_{uv}, C_{dv}, A_{Dbar}, B_{Dbar}, C_{Dbar}, C_{Ubar}, E_{uv}$
- 14 free parameters are used for HERAPDF1.5f, HERAPDF1.6 fitting HERA-1 and HERA-2 data (more data require a more flexible parametrization):
 - $A'_g \cdot x^{B'_g} \cdot (1-x)^{C_g}$ term for low- x gluon and $B_{uv} \neq B_{dv}$ to free low- x uv from dv

HERAPDF parametrizations II

$$xf(x, Q_0^2) = Ax^B (1-x)^C (1 + Dx + Ex^2 + \epsilon\sqrt{x})$$

extended gluon parametrization: $A_g \cdot x^{B_g} \cdot (1-x)^{C_g} \cdot (1+Dx+Ex^2) - A'_g \cdot x^{B'_g} \cdot (1-x)^{C_g}$

	A	B	C	D	E	ϵ
uv	Sum rule	free	free	free	free	var
dv	Sum rule	free	free	var	var	var
UBar	=(1-fs)ADbar	=BDbar	free	var	var	var
DBar	free	free	free	var	var	var
glue	Sum rule	free	free	var	var	var

A'_g	B'_g
free	free

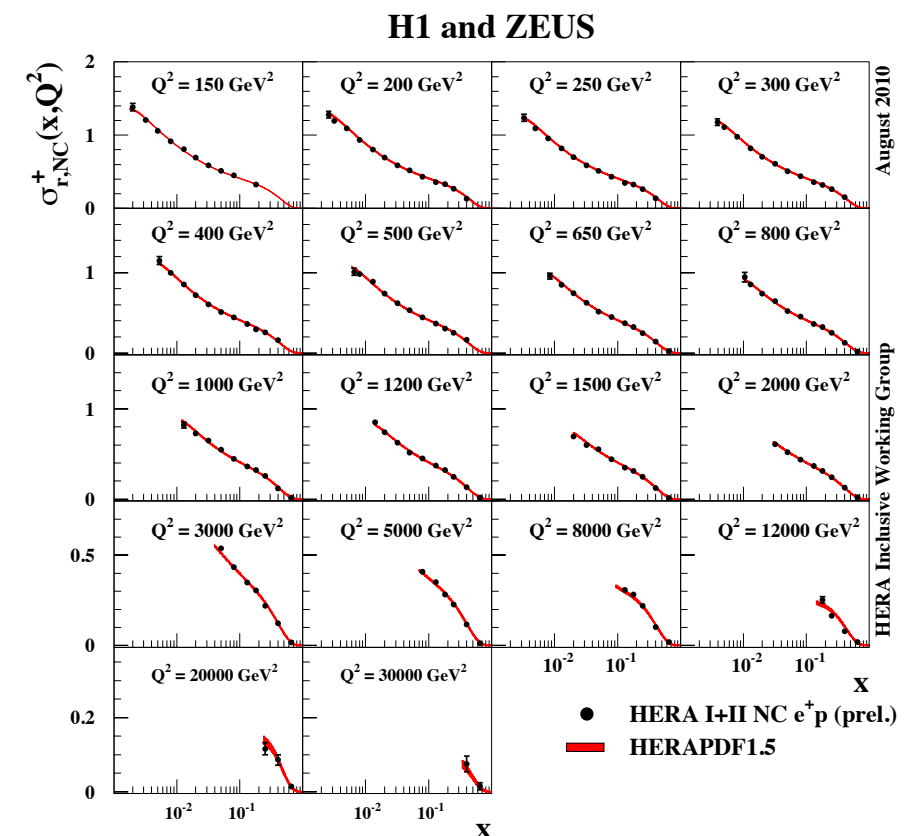
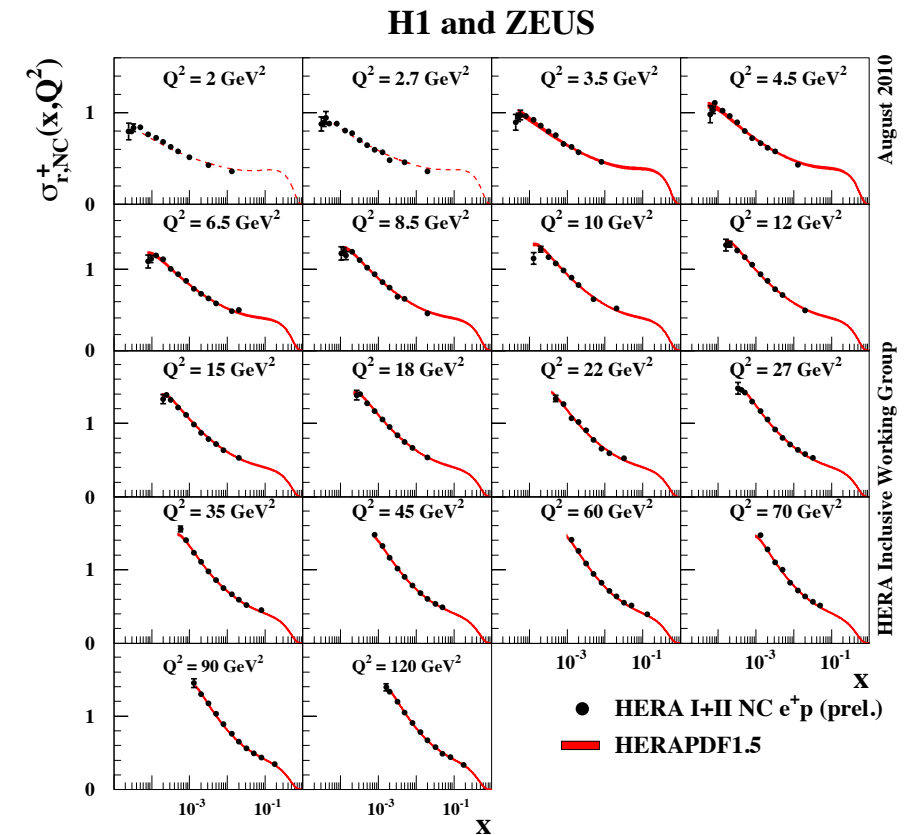
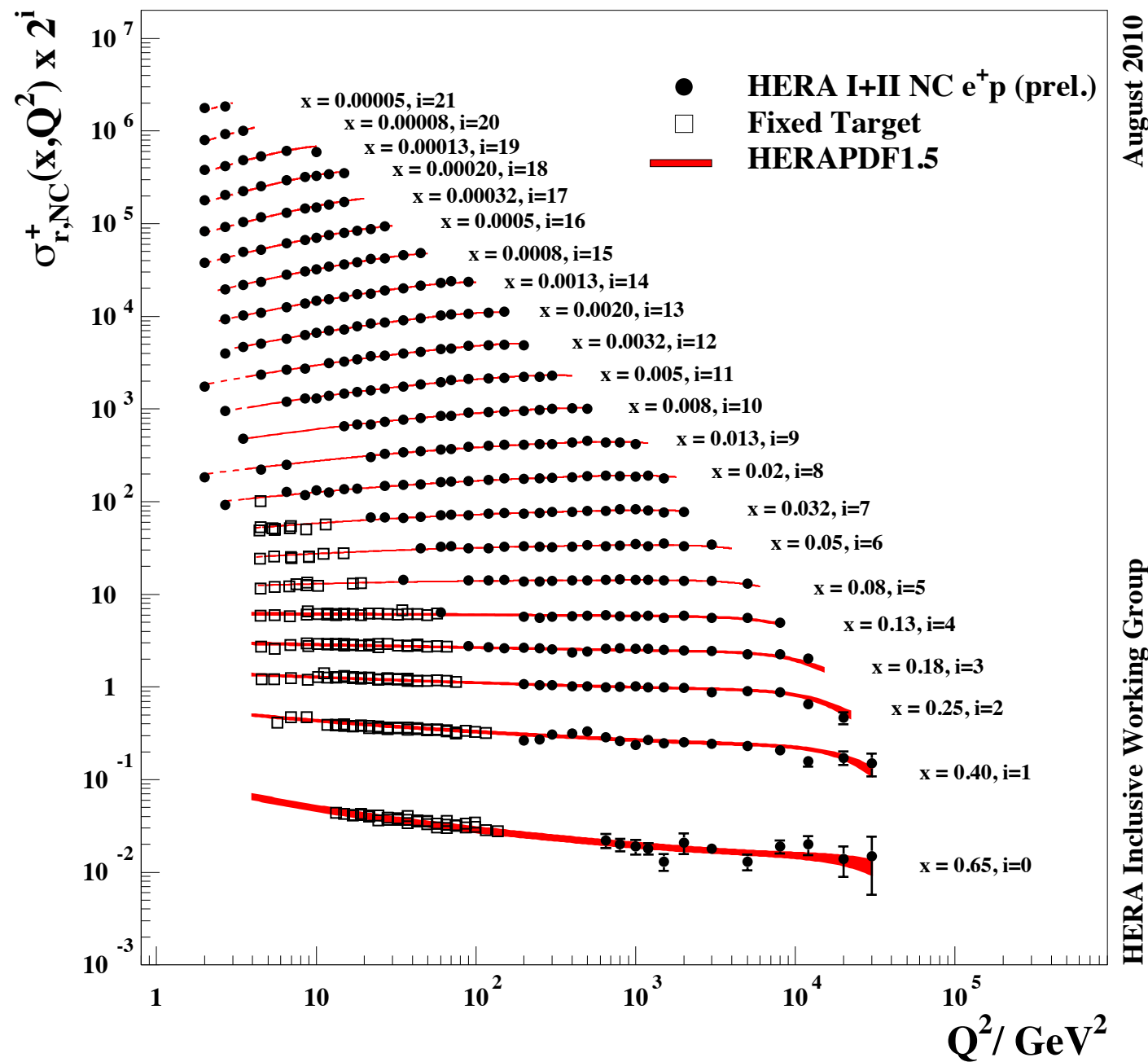
HERAPDF1.5f & HERAPDF1.6:

- additional parameters: B_{dv} , D_{uv} , A'_g , B'_g
- estimate of parametrization uncertainty: indicated parametrization variations, Q_0^2
- estimate of model uncertainties: m_c , m_b , f_s , Q_{\min}^2 are varied

Incl. HERA NC e+p cross sections

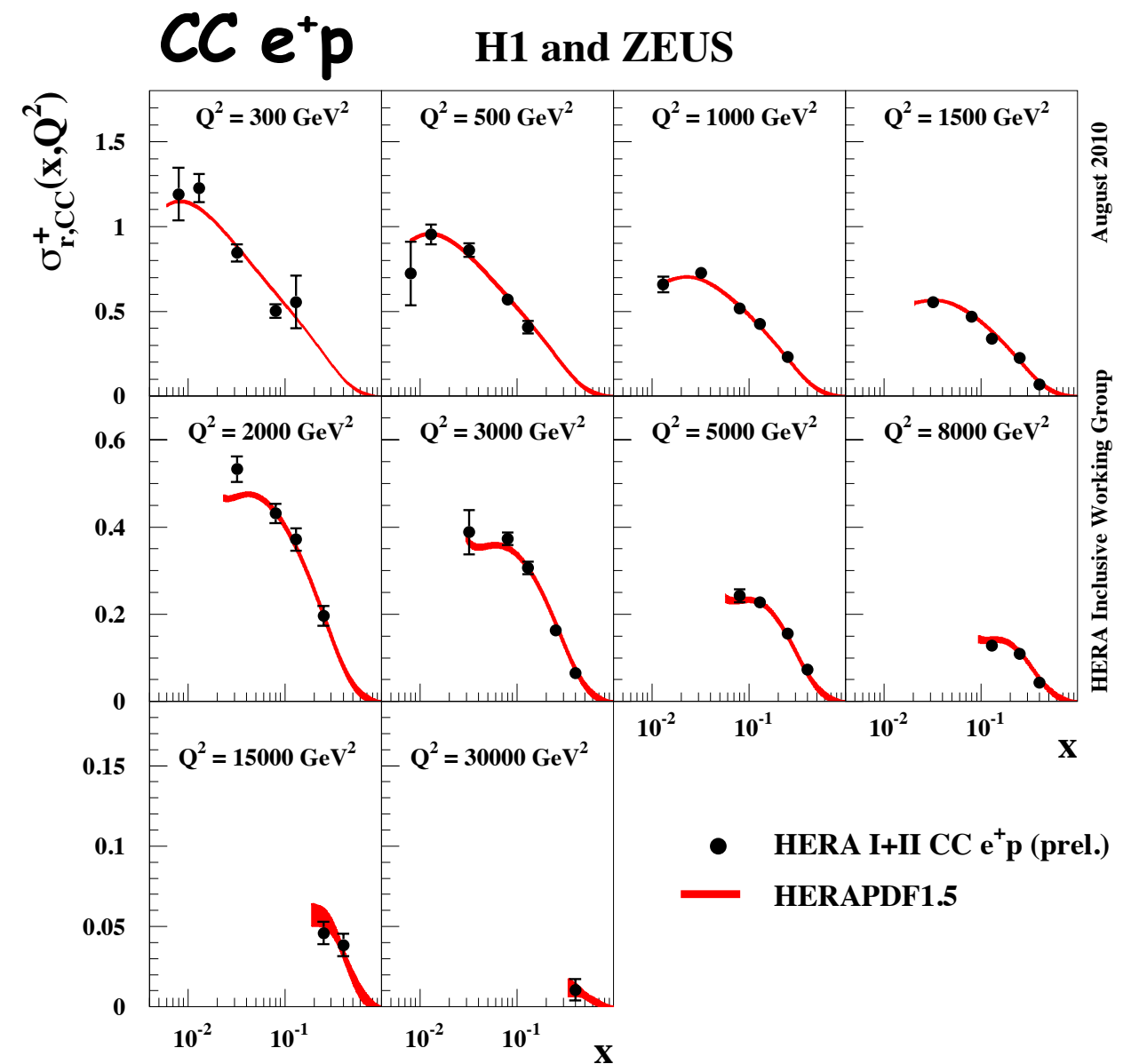
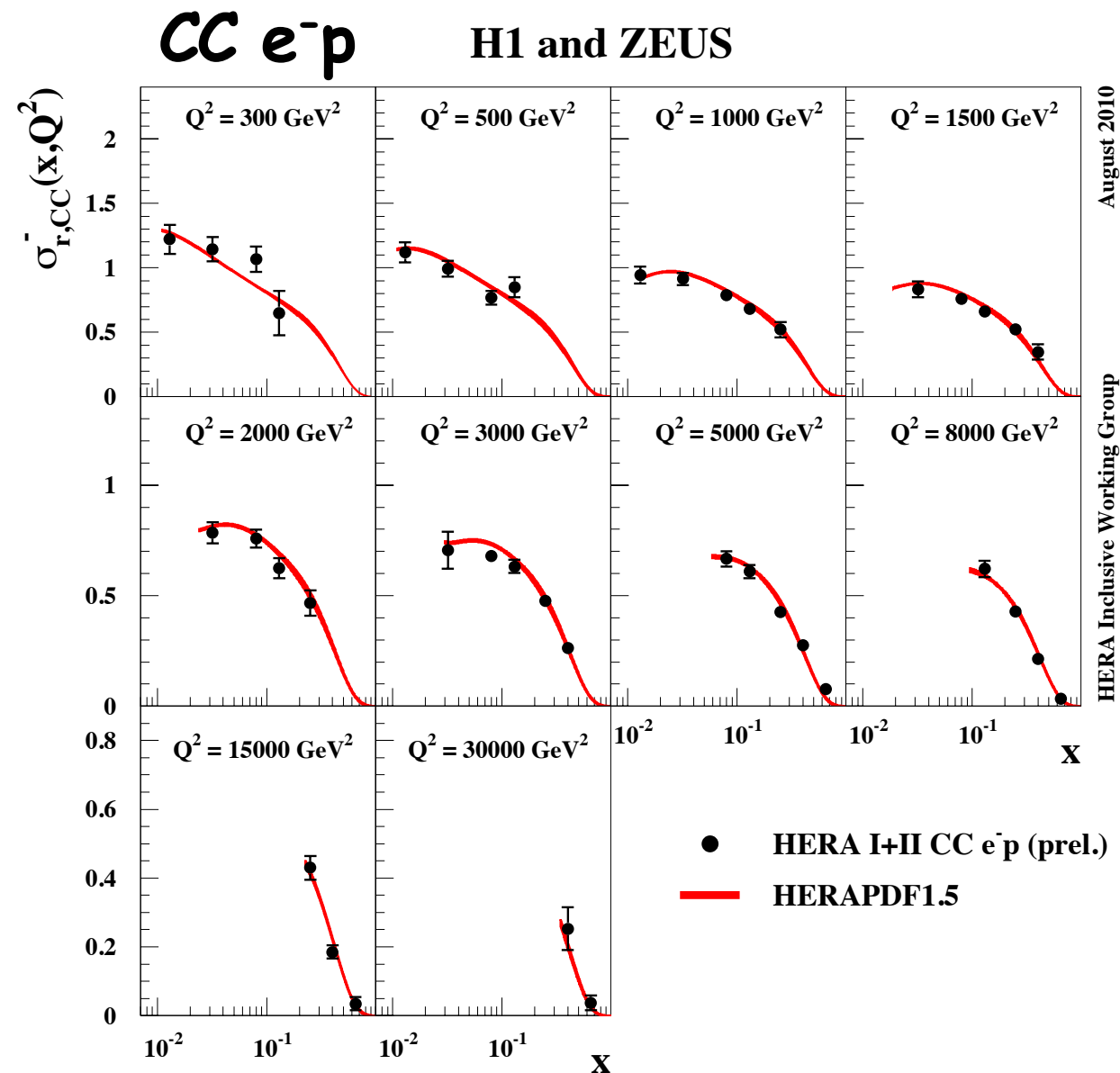
- HERA PS: $0.045 < Q^2 < 3 \cdot 10^4 \text{ GeV}^2$, $5 \cdot 10^{-5} < x < 0.65$
- combine H1 & ZEUS data

H1 and ZEUS



see talk by Rik Yoshida on combined (H1&ZEUS) NC and CC measurements, and H1 & ZEUS, JHEP 1001 109 (2010) + updates

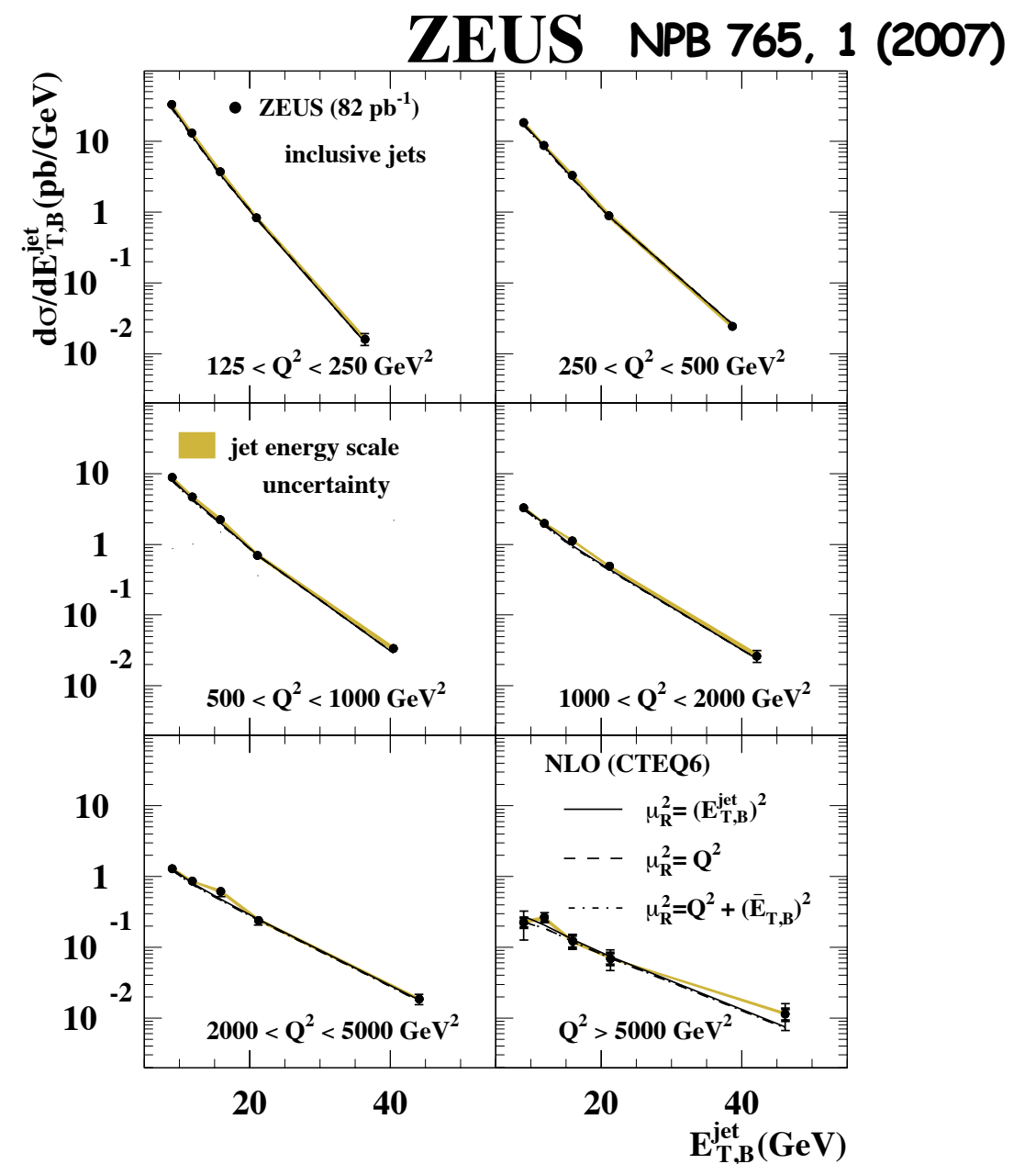
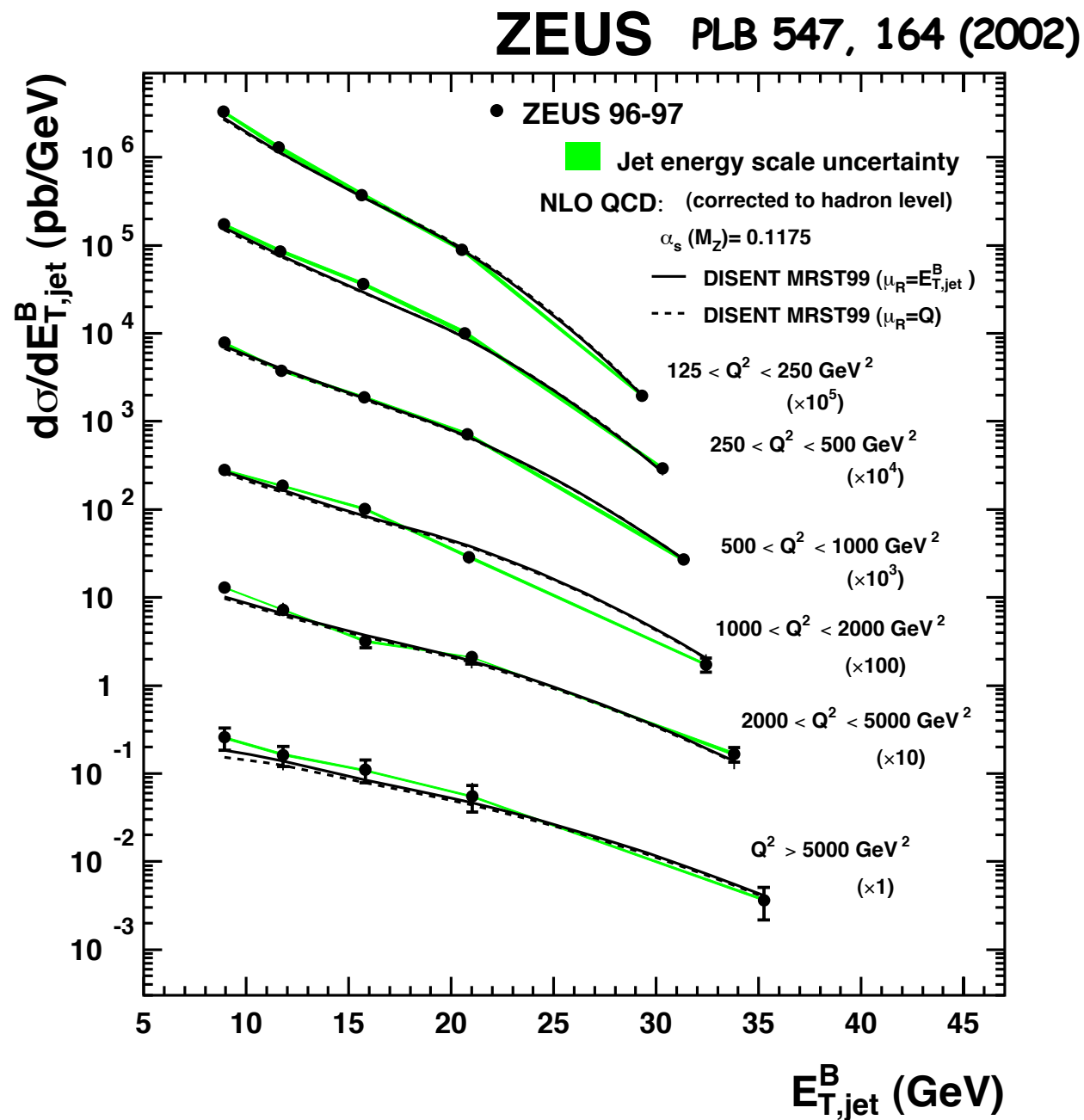
Incl. HERA CC $e^\pm p$ cross sections



$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) \left[u + c + (1-y)^2 (\bar{d} + \bar{s}) \right]$$

$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) \left[\bar{u} + \bar{c} + (1-y)^2 (d + s) \right]$$

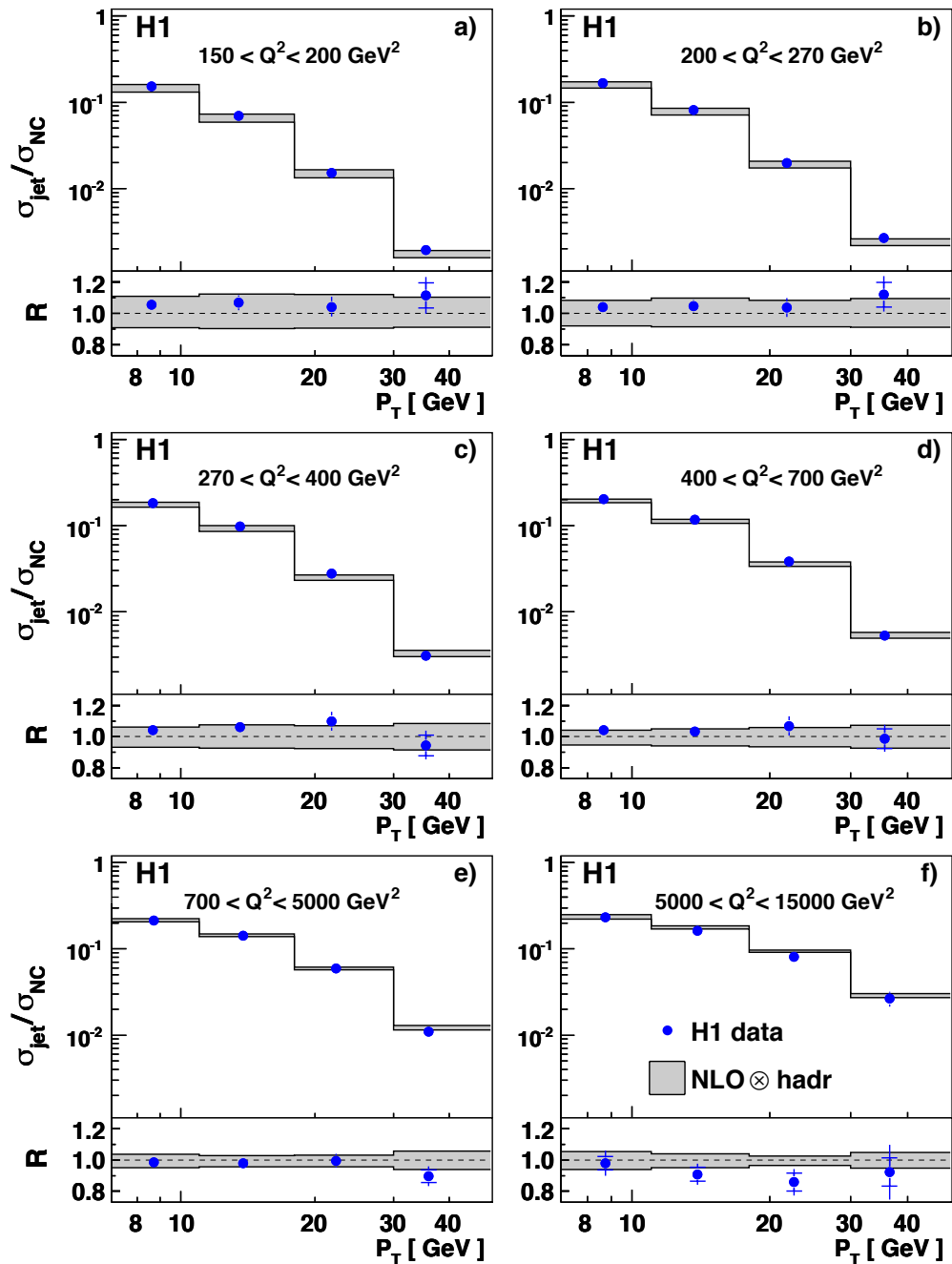
Incl. jet cross sections (ZEUS)



exp. uncertainty for inclusive jets at high Q^2 : ~ 15% uncorrelated, 4% correlated

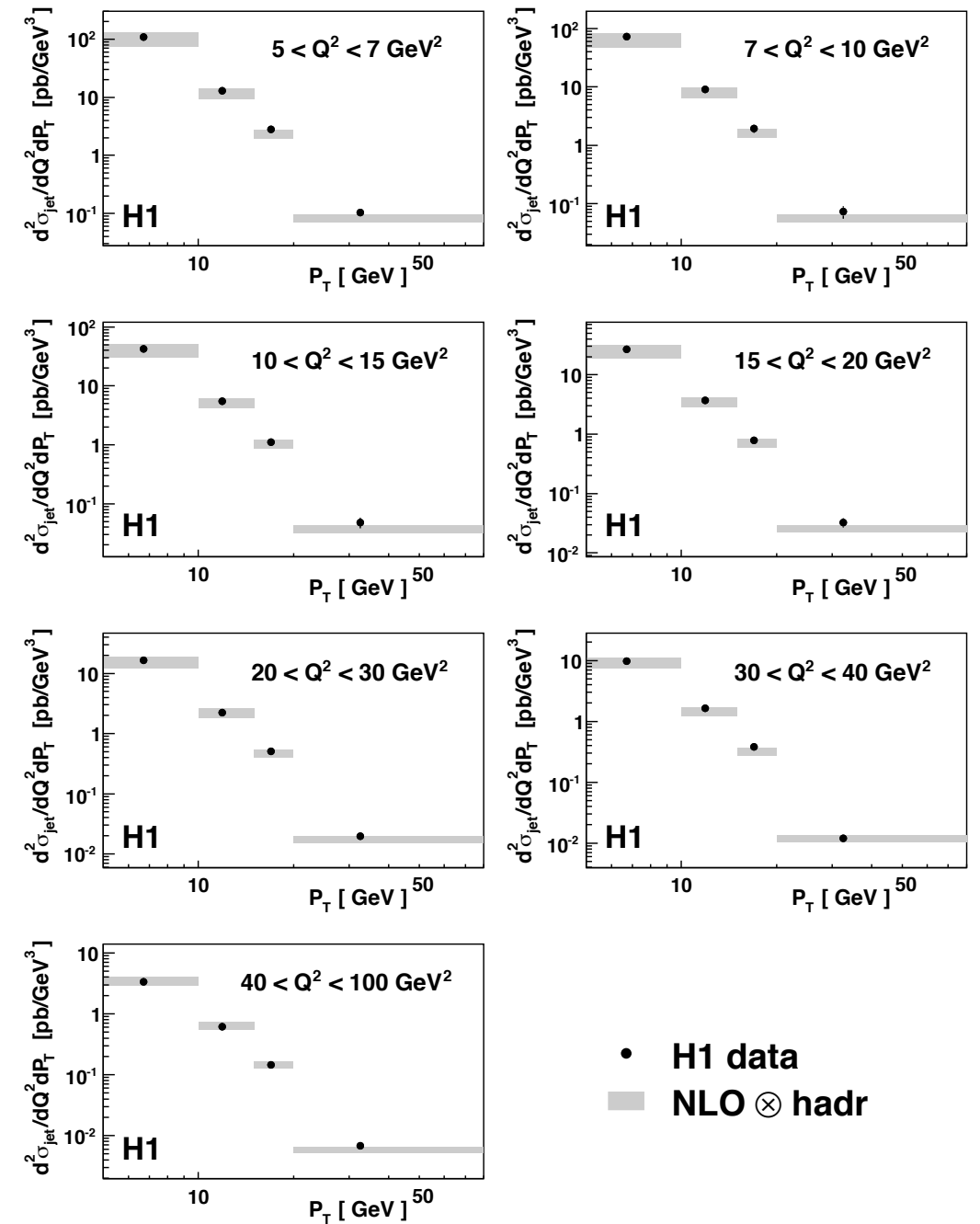
Incl. jet cross sections (H1)

Normalised Inclusive Jet Cross Section



EPJC 65, 363 (2010)

Inclusive Jet Cross Section



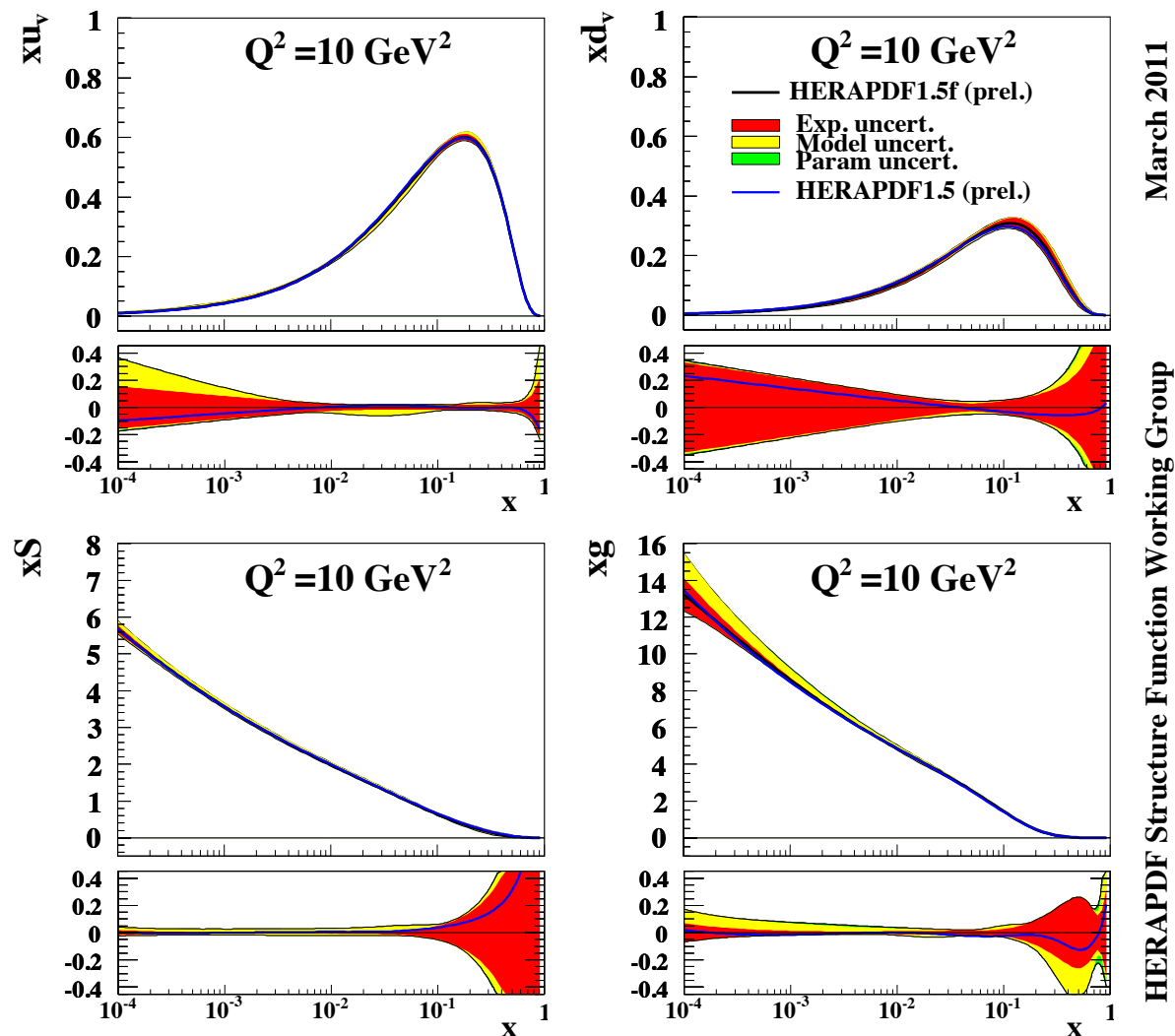
EPJC 67, 1 (2010)

exp. uncertainty for **normalized** inclusive jets
at **high** Q^2 : ~ 6% uncorrelated, 3% correlated

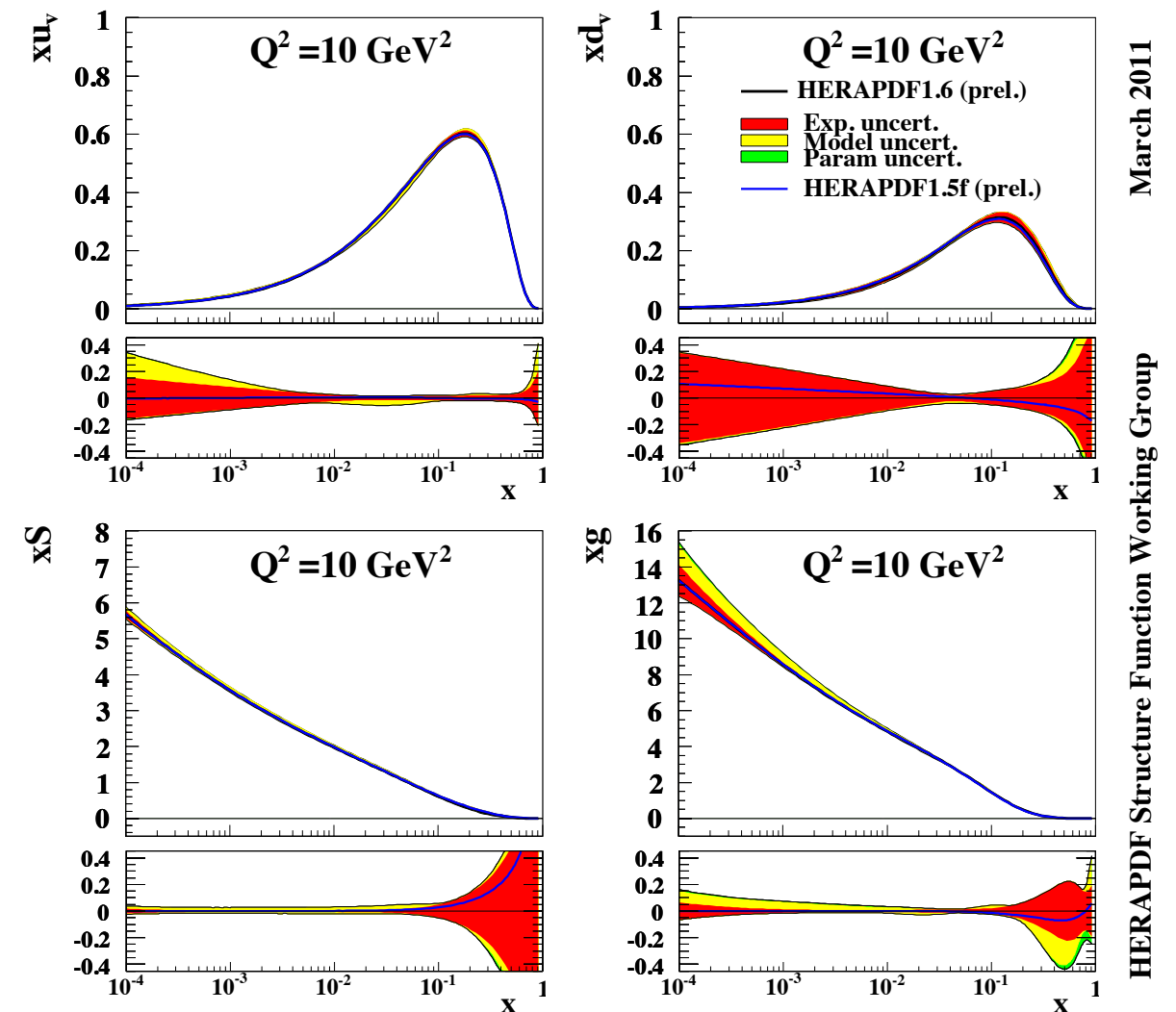
for inclusive jets at **low** Q^2 :
~ 9% uncorrelated, 8% correlated

HERAPDF1.5f (no jets) vs HERAPDF1.6 (+jets)

H1 and ZEUS HERA I+II 14 parameter PDF Fit **no jets**



H1 and ZEUS HERA I+II PDF Fit **with jets**



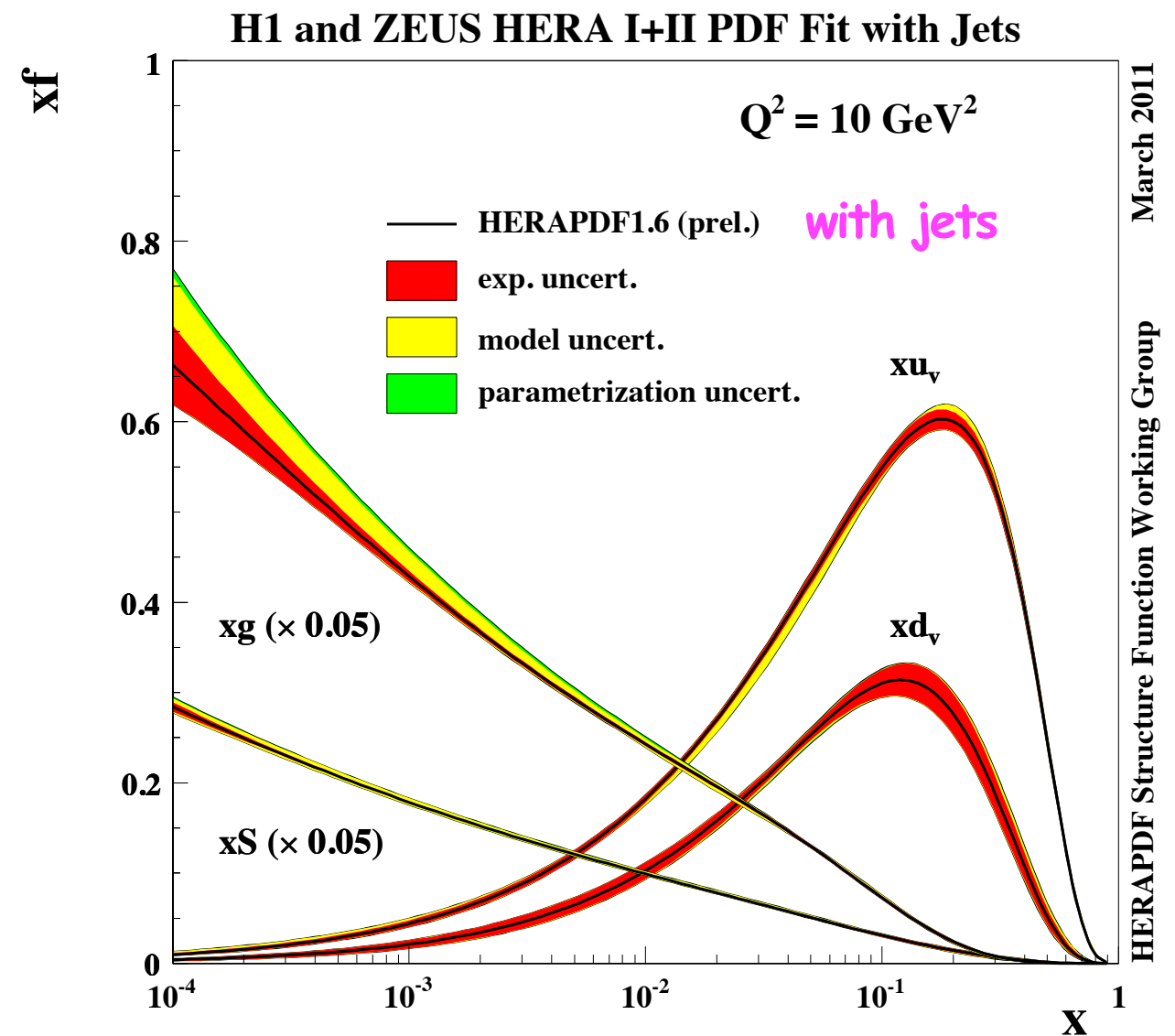
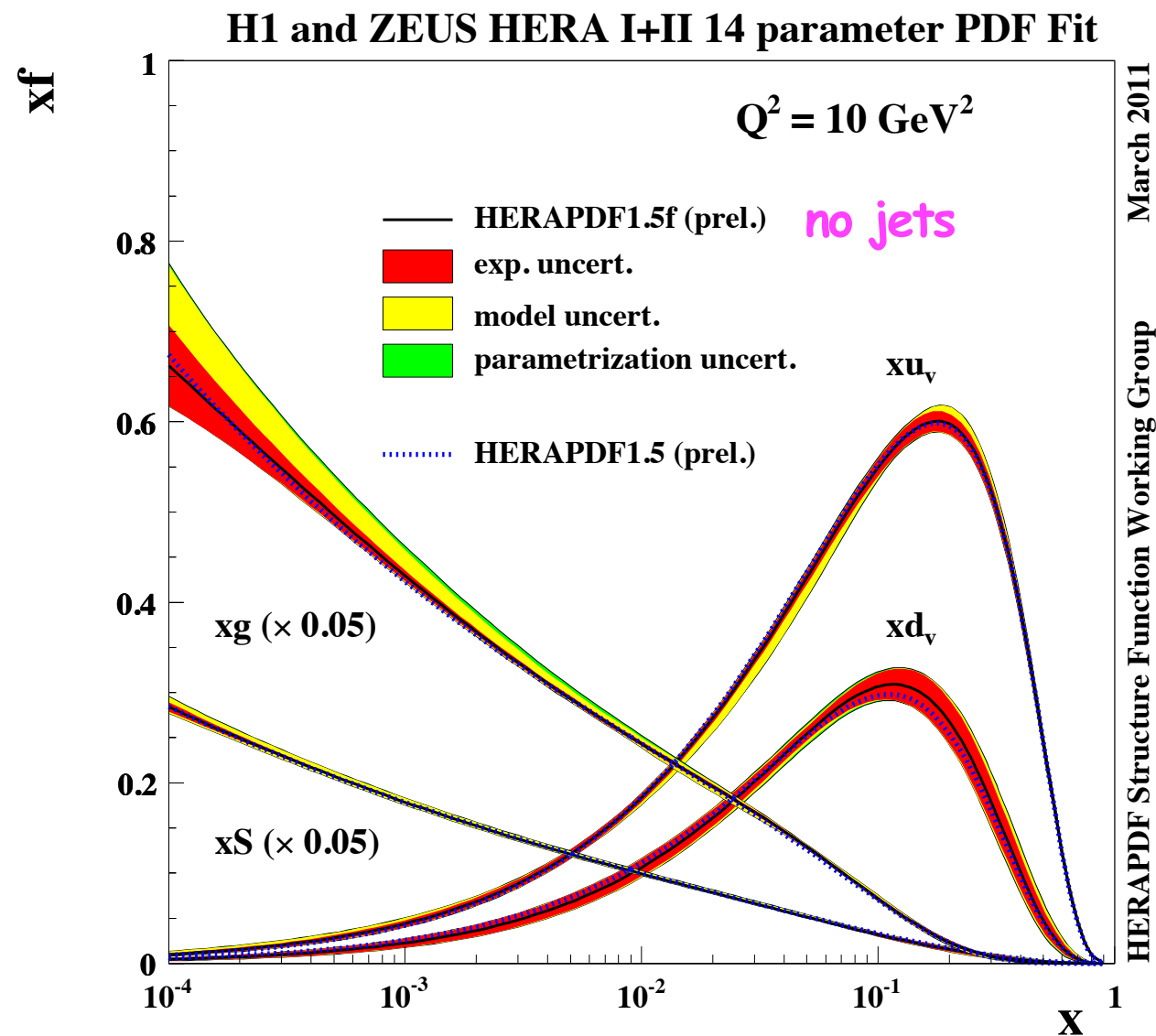
fixed $\alpha_s(M_Z) = 0.1176$

➡ adding jet data results in almost no differences, besides a softer high- x Sea and a marginal reduction in the high- x gluon uncertainty

H1prelim-11-034
ZEUS-prel-11-001

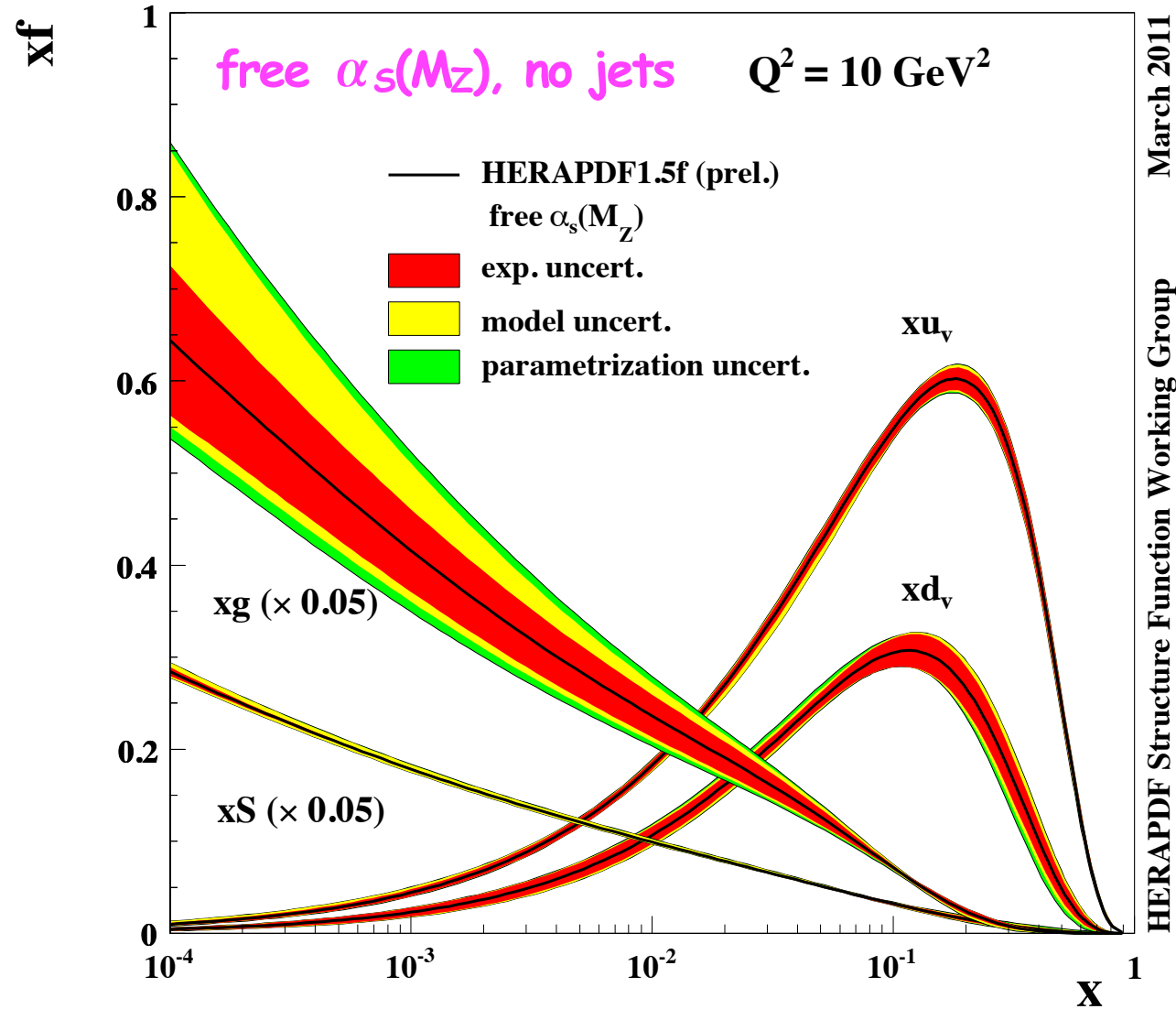
HERAPDF1.5f (no jets) vs HERAPDF1.6 (+jets)

fixed $\alpha_s(M_Z) = 0.1176$

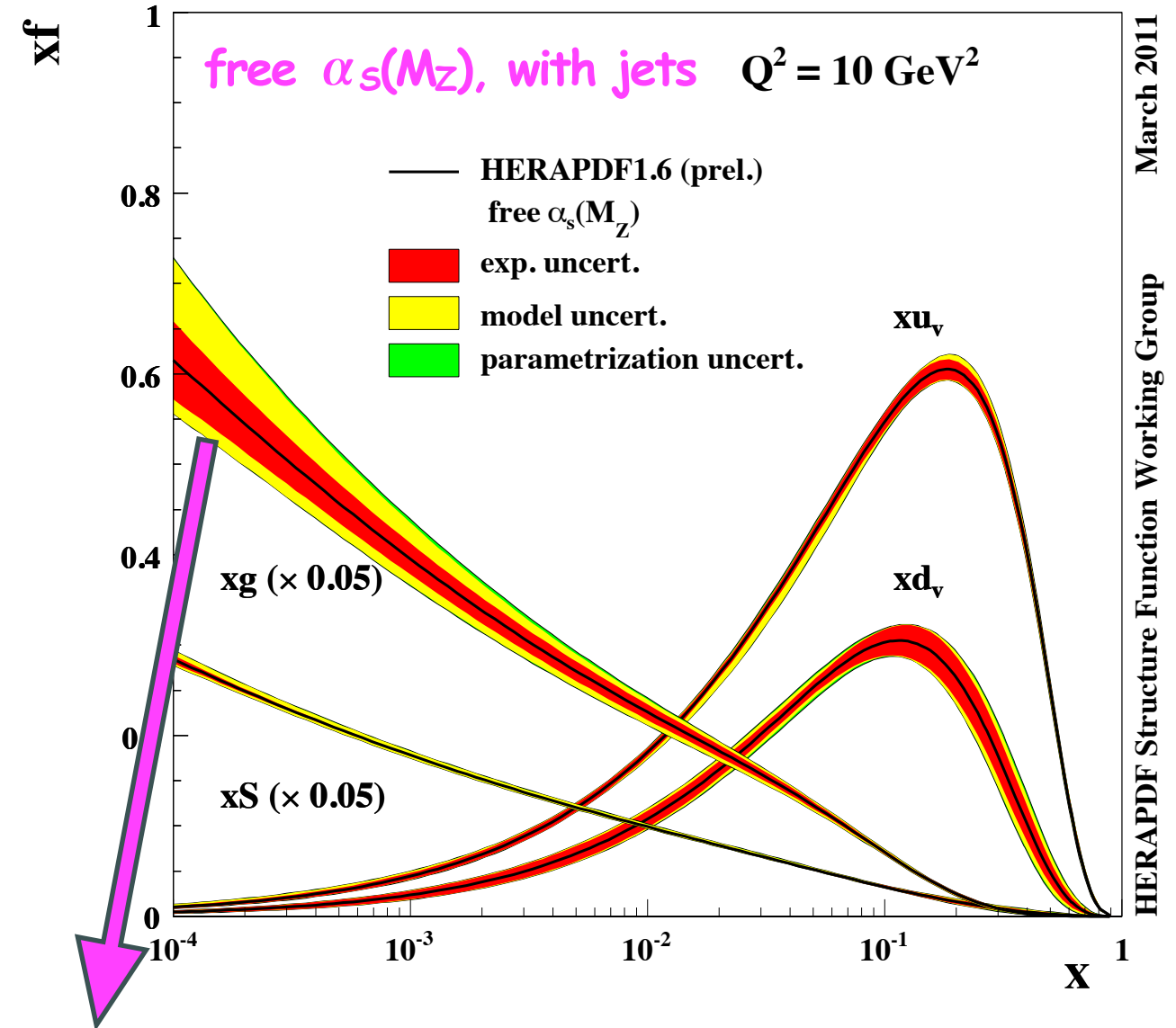


HERAPDF1.5f (no jets) vs HERAPDF1.6 (+jets)

H1 and ZEUS HERA I+II PDF Fit

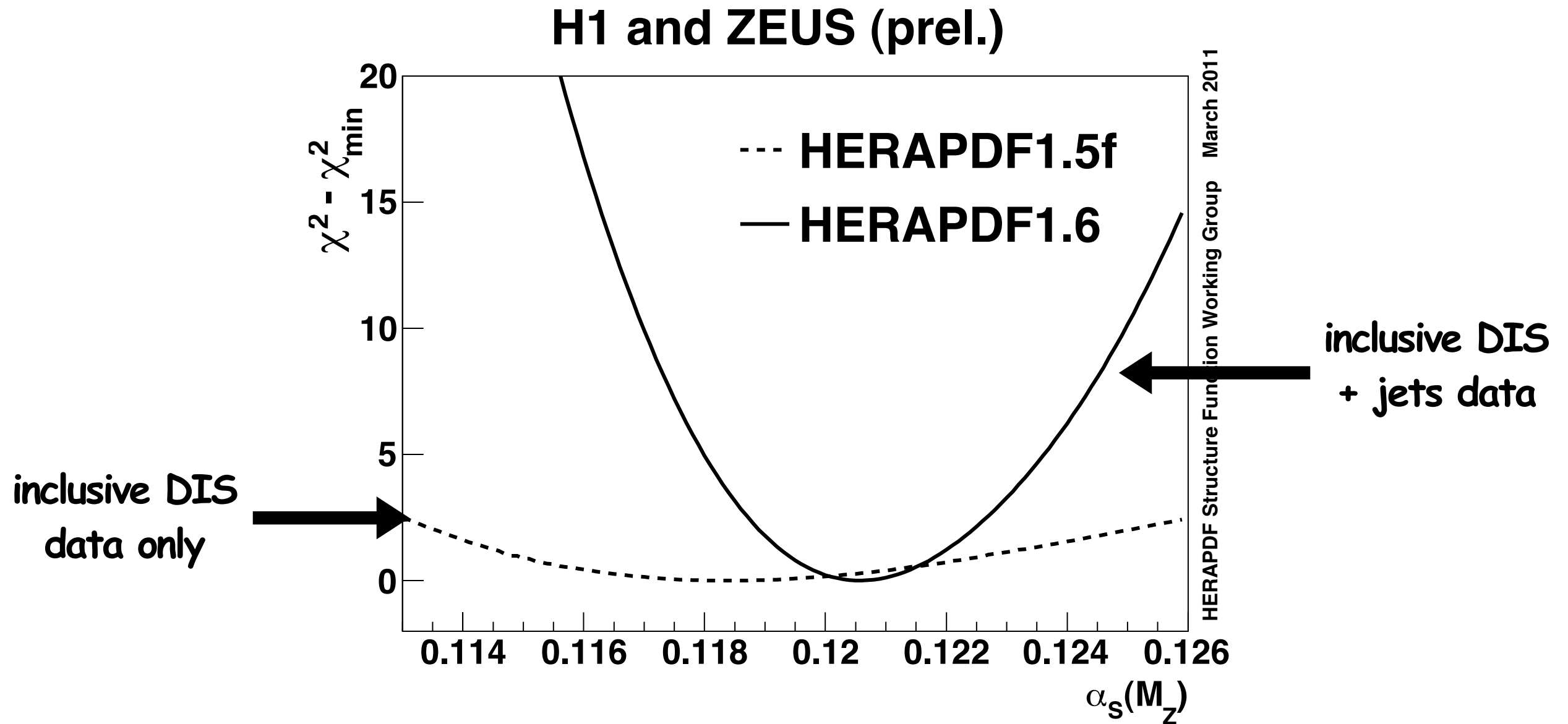


H1 and ZEUS HERA I+II PDF Fit with Jets



adding jet data dramatically decreases the low- x gluon uncertainty, not only the **exp.** but also the **model** and **parametrization** uncertainties

HERAPDF1.5f & 1.6 and $\alpha_s(M_Z)$ scan



⇒ adding jet data successfully reduces the correlation of α_s and the gluon

$\alpha_s(M_Z)$ from incl. DIS & jets in DIS

$$\alpha_s(M_Z) = 0.1202 \pm 0.0013(\text{exp}) \pm 0.0007(\text{model/param}) \pm 0.0012(\text{hadronization}) {}^{+0.0045}_{-0.0036}(\text{scale})$$

$$\alpha_s(M_Z) = 0.1202 \pm 0.0019(\text{exp/model/param/hadronization}) {}^{+0.0045}_{-0.0036}(\text{scale})$$

scale uncertainty from variation of renormalization
& factorization scale by a factor of $\frac{1}{2}$ and 2

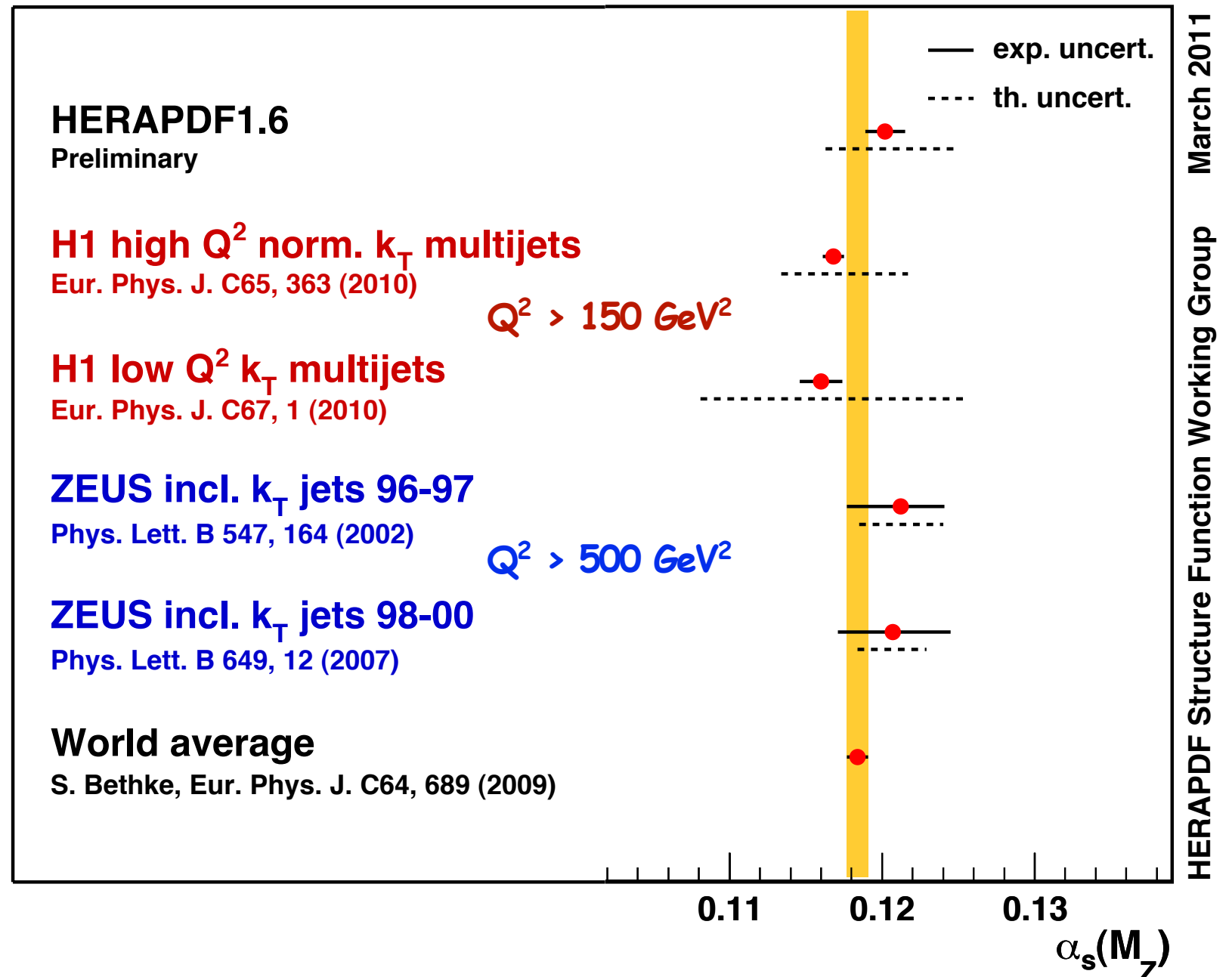
HERAPDF1.6 $\alpha_s(M_Z)=0.1176$	χ^2	N _{data}
all data	811.5	780
inclusive data	730.2	674
jet data	81.3	106

HERAPDF1.6 $\alpha_s(M_Z)$ free	χ^2	N _{data}
all data	807.6	780
inclusive data	730.0	674
jet data	77.6	106

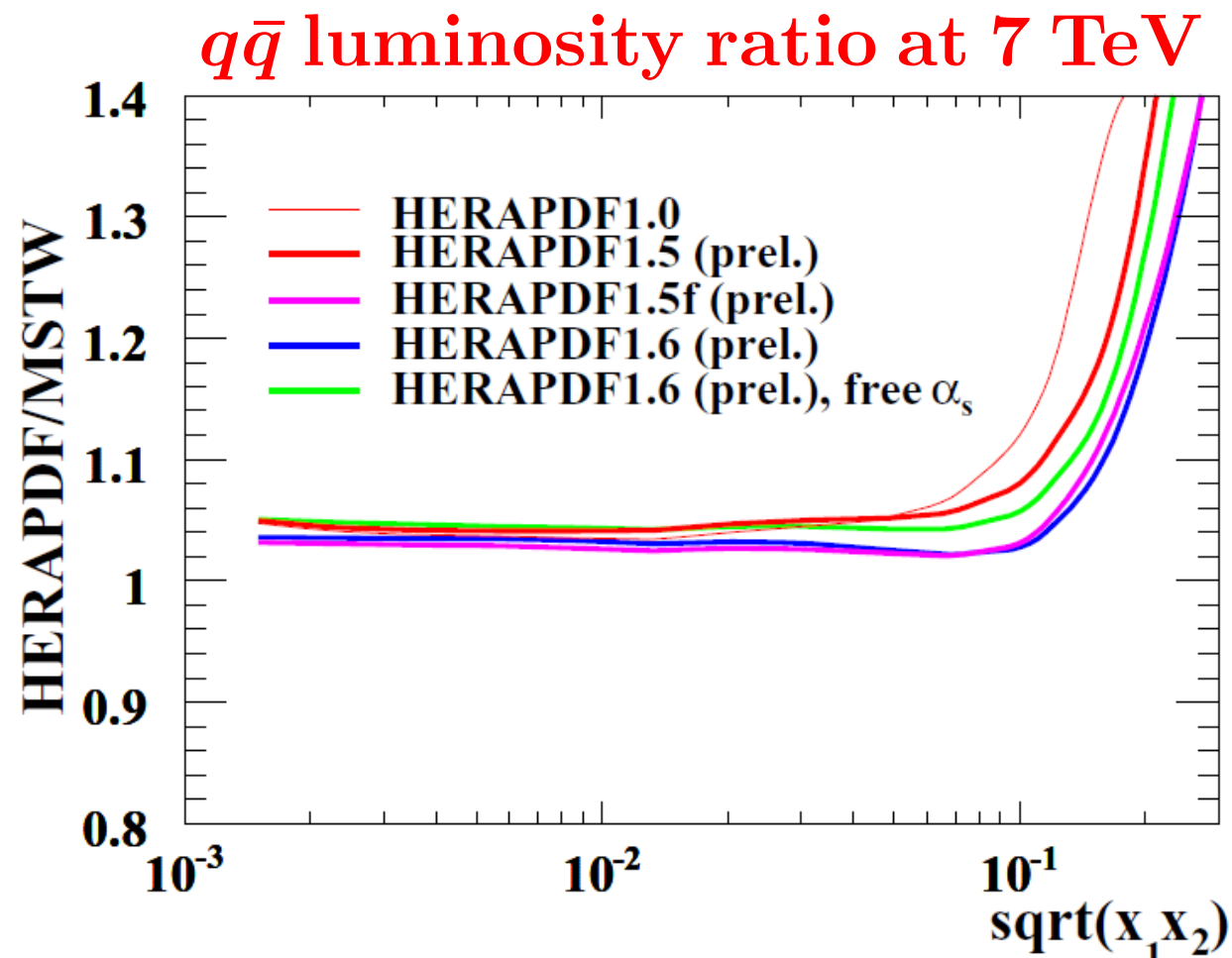
$\alpha_s(M_Z)$ summary

- for HERAPDF1.6 the PDF uncertainty is part of the exp. uncertainty
- for the **H1** and **ZEUS** results from jets only, it is part of the theory uncertainty

H1 and ZEUS (prel.)

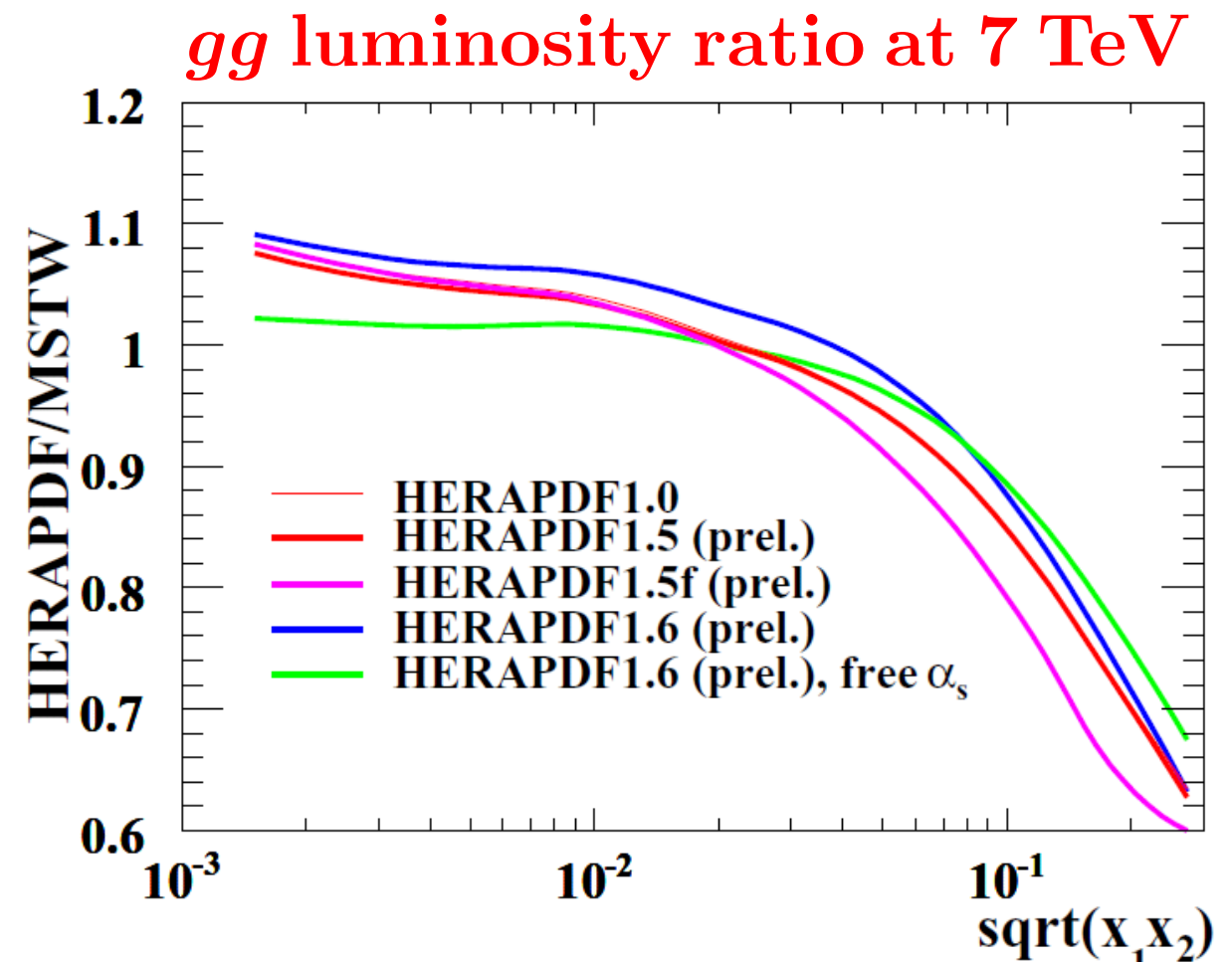


LHC parton lumis: HERAPDFs/MSTW2008



from HERAPDF1.5f (no jets) to
HERAPDF1.6 (+jets) “no” difference,

HERAPDF1.6 (+jets & free α_s) leads
to a small increase at high- x



from HERAPDF1.5f (no jets) to
HERAPDF1.6 (+jets) increases the
gluon, particularly at high- x ,

HERAPDF1.6 (+jets & free α_s) leads
in addition to a decrease at low- x

Summary

- An NLO QCD fit with simultaneous determination of the PDFs & $\alpha_s(M_Z)$ was performed using HERA data only.
- Combined H1 and ZEUS inclusive DIS cross sections together with inclusive jet cross sections from H1 and ZEUS are used.
- Including jet data in the fit and letting $\alpha_s(M_Z)$ free
 - dramatically reduces the correlation between the gluon PDF and $\alpha_s(M_Z)$ compared to fits without jets
 - the precision of the gluon PDF is improved and an accurate and unbiased determination of $\alpha_s(M_Z)$ is achieved, with a value consistent with the world average.



HERA Combined results




[HERA results](#)

[H1 home page](#)

[ZEUS home page](#)

HERAPDF table

https://www.desy.de/h1zeus/combined_results/herapdf/table/

NAME	NC and CC DIS	NC, lower E(p_beam)	Jets	Charm	Docu	Grids	Data comparison	Date
HERAPDF1.7 NLO	HERAI + partial HERAI	H1+ZEUS	H1 and ZEUS(1)	H1+ZEUS	Figures	N.A.		June 2011
HERAPDF1.6 NLO	HERAI + partial HERAI	---	H1 and ZEUS(1)	---	Writeup and figures	N.A.		March 2011
HERAPDF1.5 NNLO	HERAI + partial HERAI	---	---	---	Figures	LHAPDF 5.8.6 beta		March 2011
HERAPDF1.5 NLO	HERAI + partial HERAI	---	---	---	Figures	LHAPDF 5.8.6 beta		July 2010
Charm mass scan	HERAI	---	---	H1+ZEUS	Writeup and figures	---		August 2010
HERAPDF1.0 NNLO	HERAI	---	---	---	ICHEP2010 writeup and figures	Docu for LHAPDF		April 2010
	HERAI	H1+ZEUS	---	---	Writeup and figures	N.A.		April 2010
	HERAI	---	---	H1+ZEUS	DIS2010 writeup and figures	N.A.		April 2010
HERAPDF1.0 NLO PUBLISHED	HERAI	---	---	---	 Paper HERAPDF1.0 page	LHAPDF	Benchmarking HERAPDF1.0	Nov. 2009

(1) H1 jets data: [1](#) and [2](#), ZEUS jets data: [1](#) and [2](#).

More information on the results can be obtained from the [contact persons](#) and/or from the [H1 and ZEUS management](#).

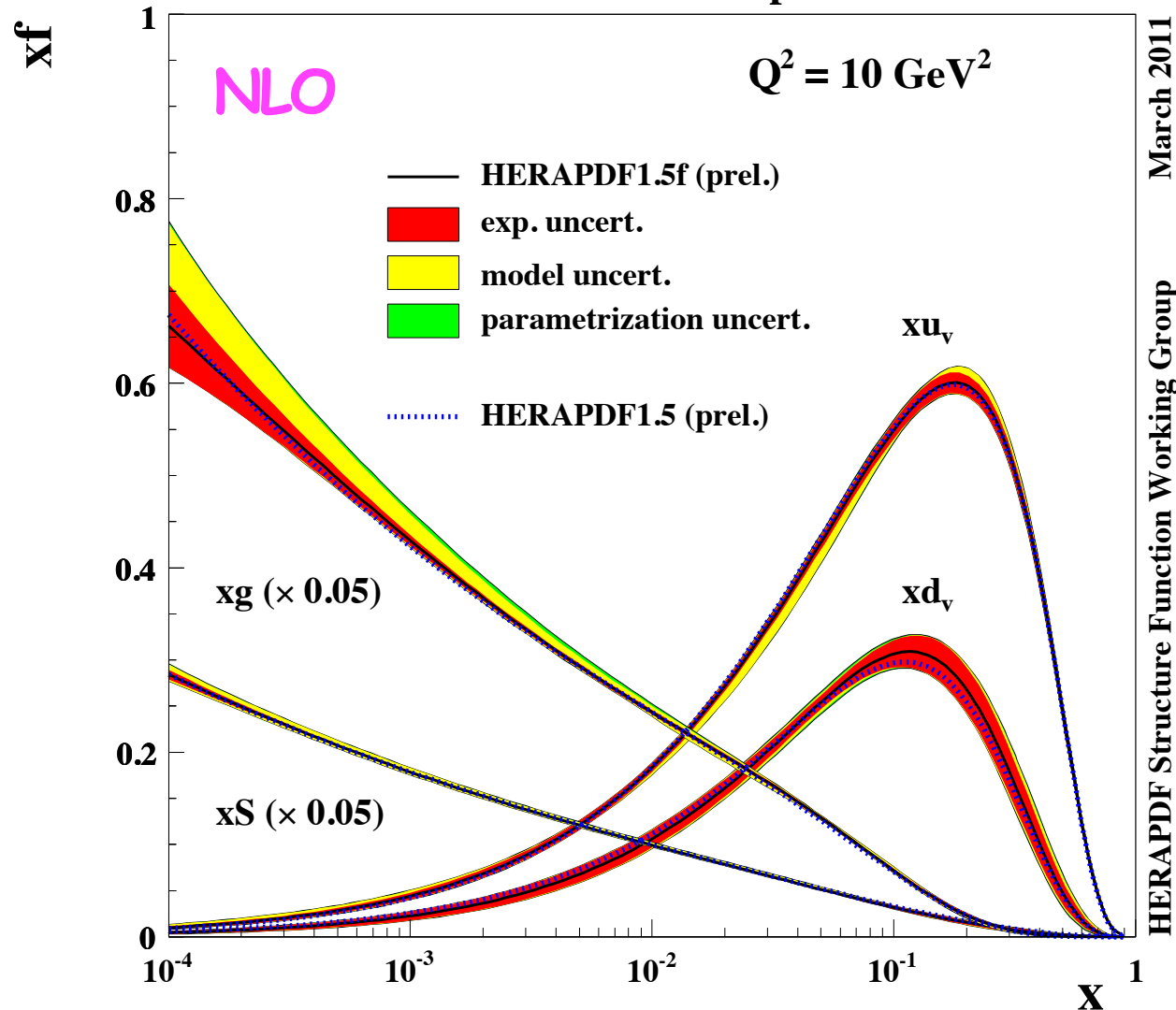
Last modified: Wed Jul 13 16:32:06 CEST 2011

Extras

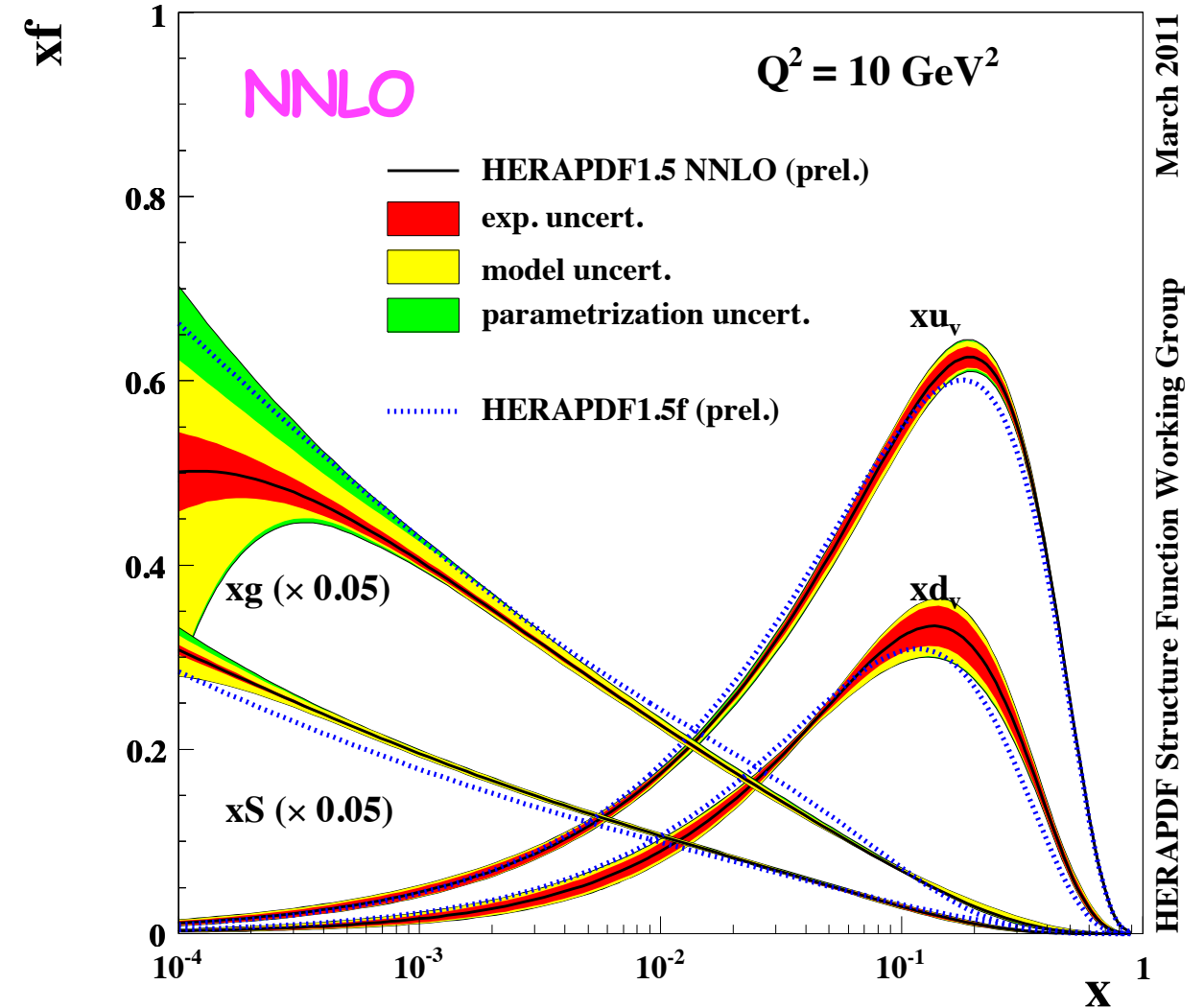
HERAPDF1.5 NLO & NNLO

fixed $\alpha_s(M_Z) = 0.1176$

H1 and ZEUS HERA I+II 14 parameter PDF Fit



H1 and ZEUS HERA I+II PDF Fit



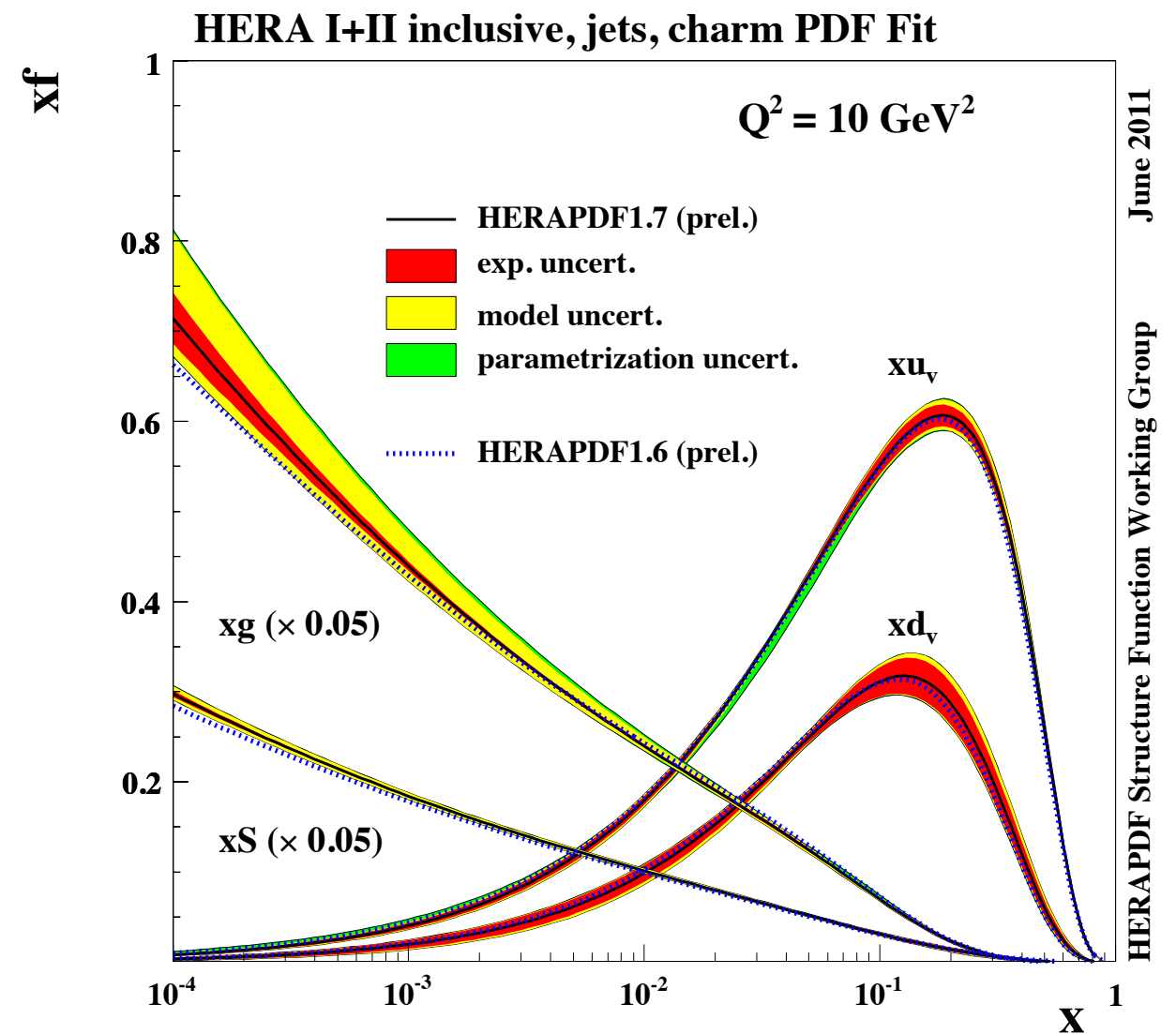
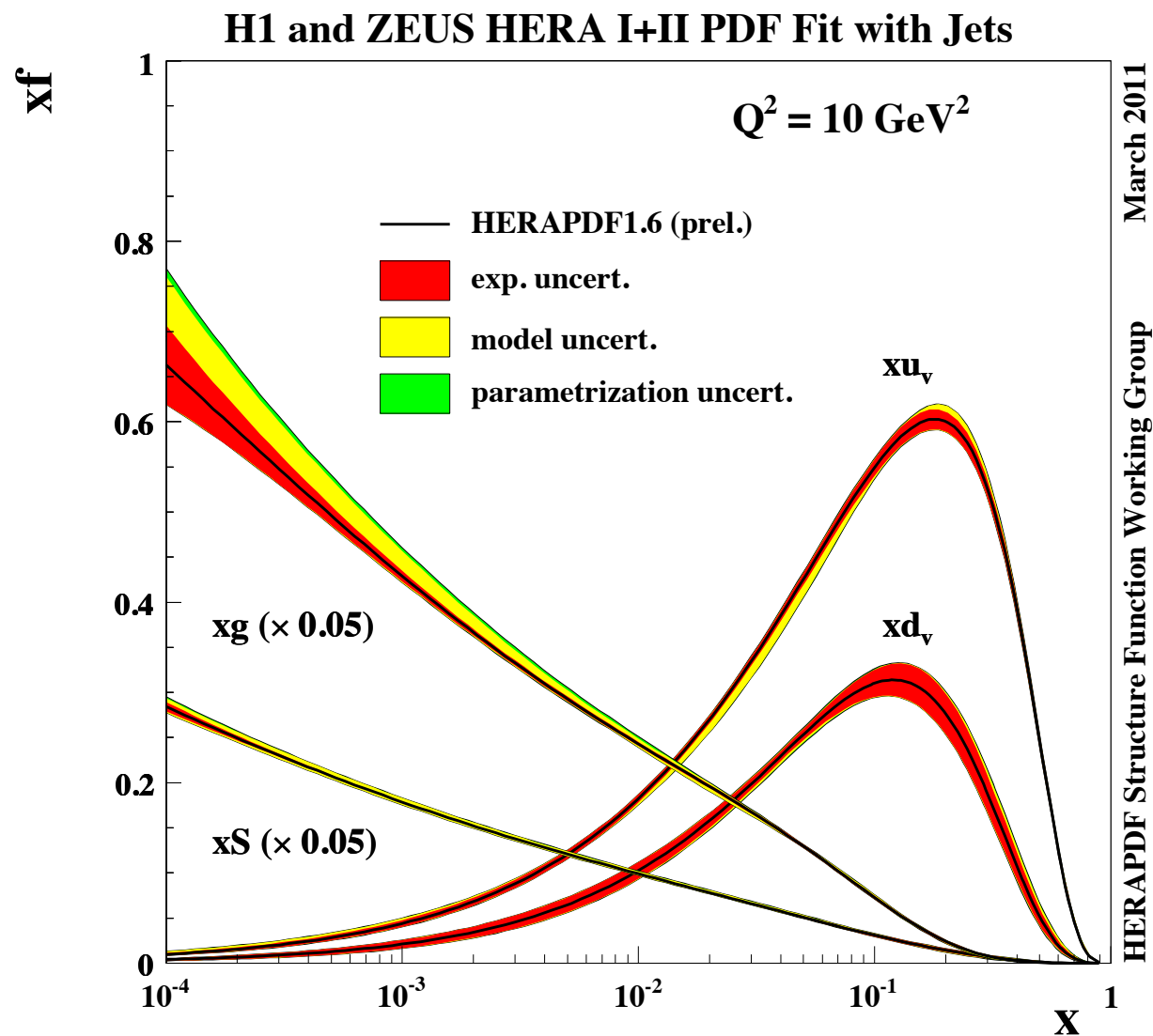
in NNLO:

- larger gluon uncertainty at low- x
- softer (more valence-like) gluon
- slightly steeper Sea at low- x
- small shift in valence to high- x

NNLO does not provide a better fit than NLO at low- x and Q^2

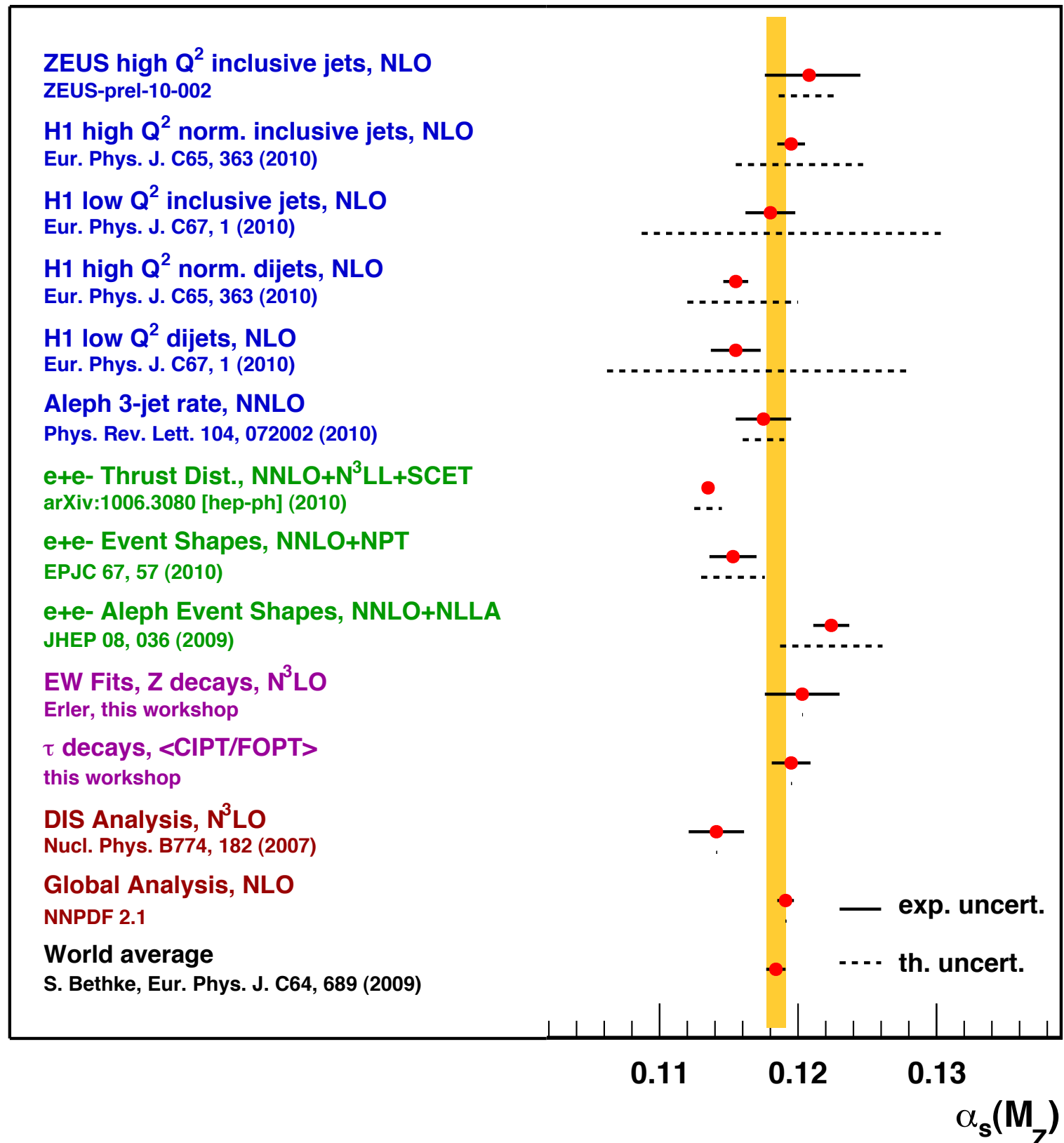
HERAPDF1.6 & 1.7

HERAPDF1.7 has fixed $\alpha_s(M_Z) = 0.1190$ & includes additional low energy & charm data



$\alpha_s(M_Z)$ from different processes

$\alpha_s(M_Z)$ values shown in
discussion session at
 α_s -workshop at MPI
Munich in February '11



What is measured in inclusive DIS ?

➤ Neutral Current: $e^\pm p \rightarrow e^\pm X$

$$\frac{d^2\sigma^{e^\pm p}}{dx dQ^2} \propto \frac{2\pi\alpha^2}{xQ^4} \left[Y_+ \underline{F_2(x, Q^2)} \mp Y_- \underline{xF_3(x, Q^2)} - y^2 \underline{F_L(x, Q^2)} \right] \quad Y_\pm \equiv 1 \pm (1-y)^2$$

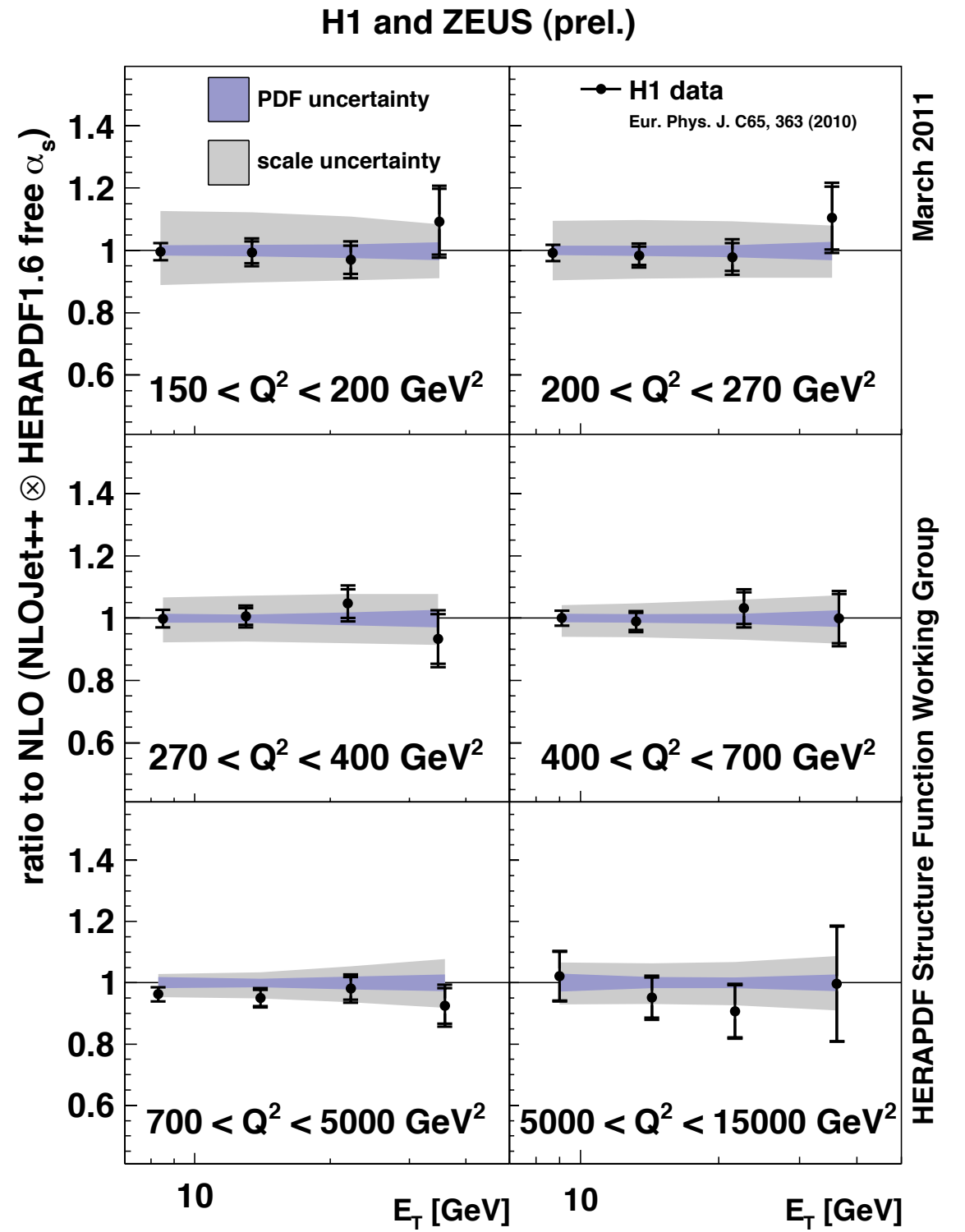
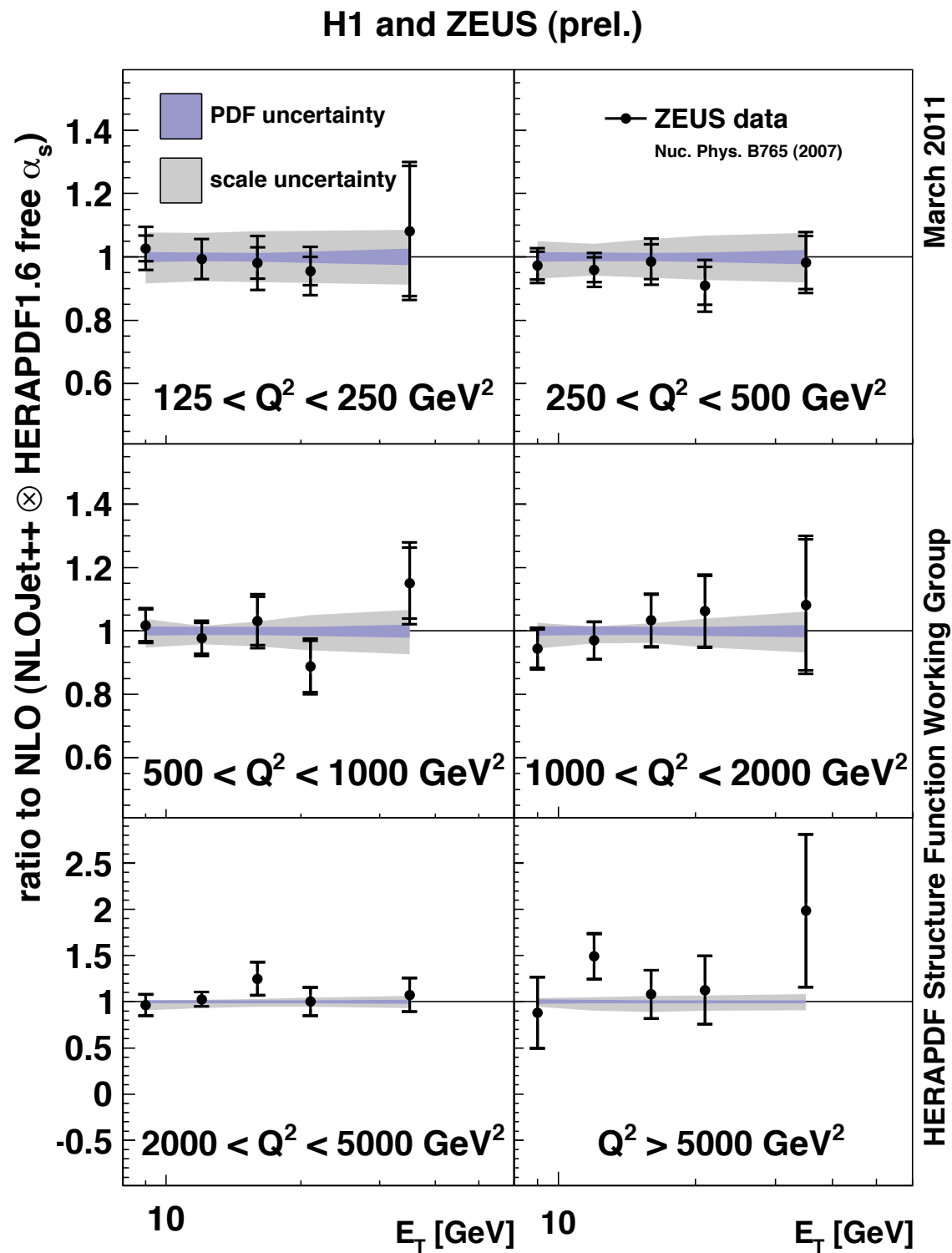
$$\text{QPM: } \begin{cases} F_2(x, Q^2) \propto x \sum_f q_f(x, Q^2) + \bar{q}_f(x, Q^2) & \text{Dominant contribution} \\ xF_3(x, Q^2) \propto x \sum_f q_f(x, Q^2) - \bar{q}_f(x, Q^2) & \text{Z/\gamma interference} \end{cases}$$

$$\text{QCD: } F_L(x, Q^2) \propto x\alpha_s g(x, Q^2) \quad \text{Directly sensitive to the gluon \& } \alpha_s$$

➤ Charged Current: $e^\pm p \rightarrow \nu X$

$$\begin{aligned} \sigma_{CC}^{e^+p} &\propto x \{ (\bar{u} + \bar{c}) + (1-y)^2 (d + s) \} && \text{sensitive to mainly d-valence quarks at high } x \\ \sigma_{CC}^{e^-p} &\propto x \{ (u + c) + (1-y)^2 (\bar{d} + \bar{s}) \} && \text{sensitive to mainly u-valence quarks at high } x \end{aligned}$$

HERAPDF1.6 and DIS jets



excellent description of the jet data sets used, shown here for 2 out of 4

systematic error sources for jets

Source of correlated uncertainty	Correlation fraction	Data set
H1 LAr electron energy scale (99-07)	25%	[4]
H1 LAr electron angle (99-07)	100%	[4]
H1 Jet energy scale (99-07)	50%	[4]
H1 Luminosity (99-00)	100%	[5]
H1 Spacal electron energy scale (99-00)	50%	[5]
H1 Spacal electron angle (99-00)	50%	[5]
H1 Jet energy scale (99-00)	50%	[5]
H1 low Q^2 jet measurement model dependence	50%	[5]
ZEUS luminosity measurement (96-97)	100%	[6]
ZEUS jet energy scale (96-97)	100%	[6]
ZEUS luminosity measurement (98-00)	100%	[7]
ZEUS jet energy scale (98-00)	100%	[7]
Theoretical luminosity measurement uncertainty	100%	[4], [5], [6], [7]

model uncertainties

Model parameter	Standard value	Lower Limit	Upper Limit
Strange fraction f_s	0.31	0.23	0.38
Charm mass m_c [GeV]	1.4	1.35	1.65
Beauty mass m_b [GeV]	4.75	4.3	5.0
Minimum Q^2 [GeV ²]	3.5	2.5	5.0

+ hadronization uncertainty for jets is included in the model uncertainty