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High Energy Physics**

**July 16 - 22, 2009**

**Krakow, Poland**



## Jets and subjects at HERA

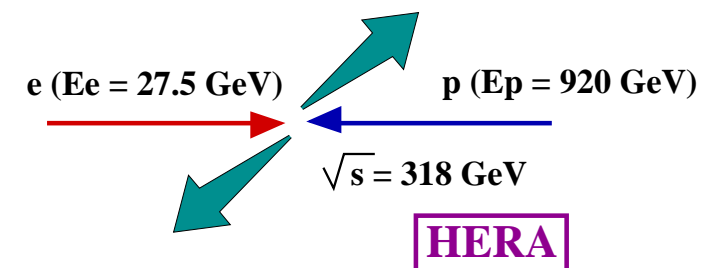
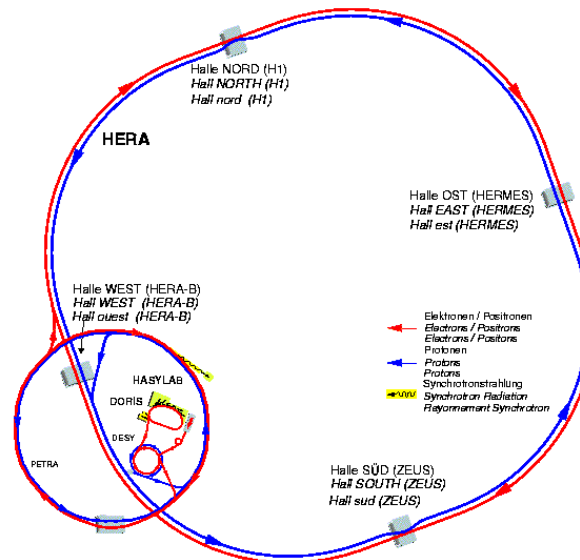
**Claudia Glasman**  
**Universidad Autónoma de Madrid**



from



**ZEUS Collaboration**

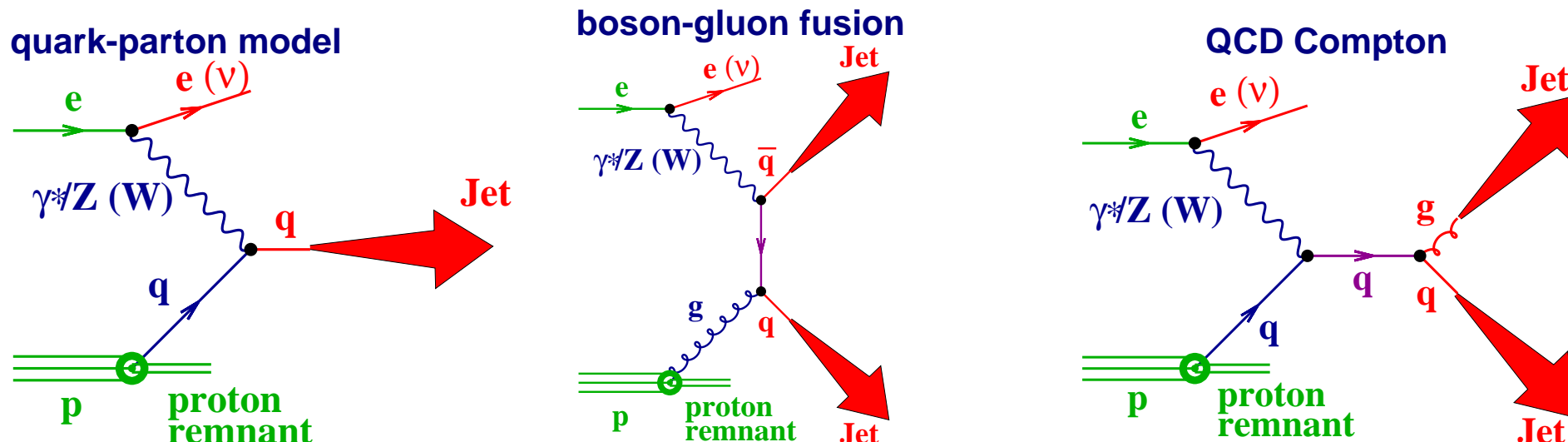


# Jets and subjects at HERA

- **Jet production and jet substructure has been extensively studied at HERA**
- **Jet cross sections have proven to be a powerful tool**
  - to test pQCD and the SM
    - **Multi-jet cross sections in CC DIS (ZEUS Collab, PRD 78 (2008) 032004)**
  - to constrain the gluon pPDFs
    - **see Juan Terrón's talk**
  - to determine  $\alpha_s$ 
    - **see Joerg Behr's talk**
  - to test the underlying colour dynamics
    - **Angular correlations in three-jet events (ZEUS Collab, DESY-08-100)**
- **Jet substructure has been proven to be a powerful tool**
  - to test the pattern of parton radiation
  - to test splitting functions
  - to study colour-coherence effects
  - to test underlying colour dynamics
    - **Subjet distributions in DIS (ZEUS Collab, DESY-08-178)**
    - **Three-subjet distributions in DIS (ZEUS Collab, ZEUS-prel-09-007)**

# Jet production in DIS at HERA

- Jet production in NC and CC deep inelastic  $ep$  scattering up to  $\mathcal{O}(\alpha_s)$ :



- Jet production cross section for DIS is given in QCD by:

$$d\sigma_{\text{jet}} = \sum_{a=q,\bar{q},g} \int dx f_a(x, \mu_F) d\hat{\sigma}_a(x, \alpha_s(\mu_R), \mu_R, \mu_F)$$

- $f_a$ : parton  $a$  density, determined from experiment  
→ **long-distance structure of the target**
- $\hat{\sigma}_a$ : subprocess cross section, calculable in pQCD  
→ **short-distance structure of the interaction**

## Kinematics:

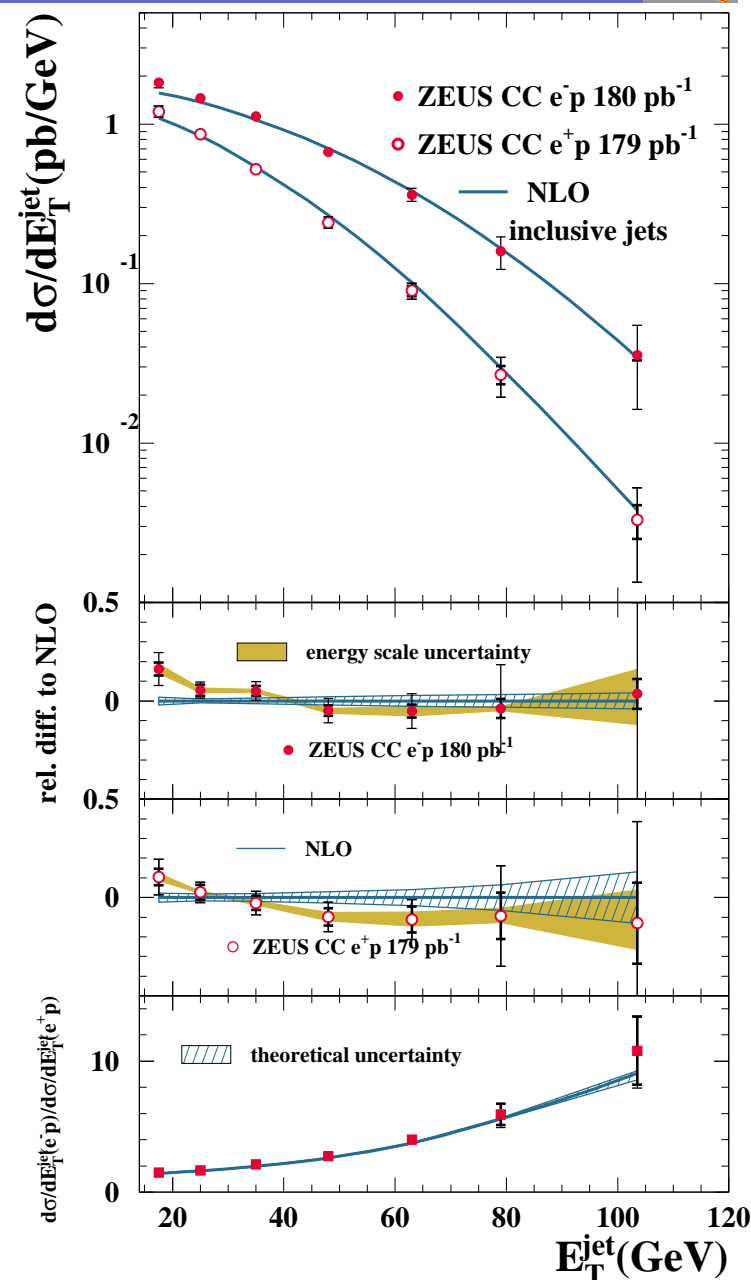
- momentum transfer:  
 $Q^2 = -q^2 = -(k - k')^2$
- Bjorken  $x$ :  $x = \frac{Q^2}{2P \cdot q}$
- inelasticity:  
 $y = \frac{P \cdot q}{P \cdot k} = 1 - \frac{E'_e(1 - \cos \theta_e)}{2E_e}$

## CC DIS and QCD



$$e^{\pm}p \rightarrow \nu + \text{jet} + X \text{ (inclusive jets)}$$

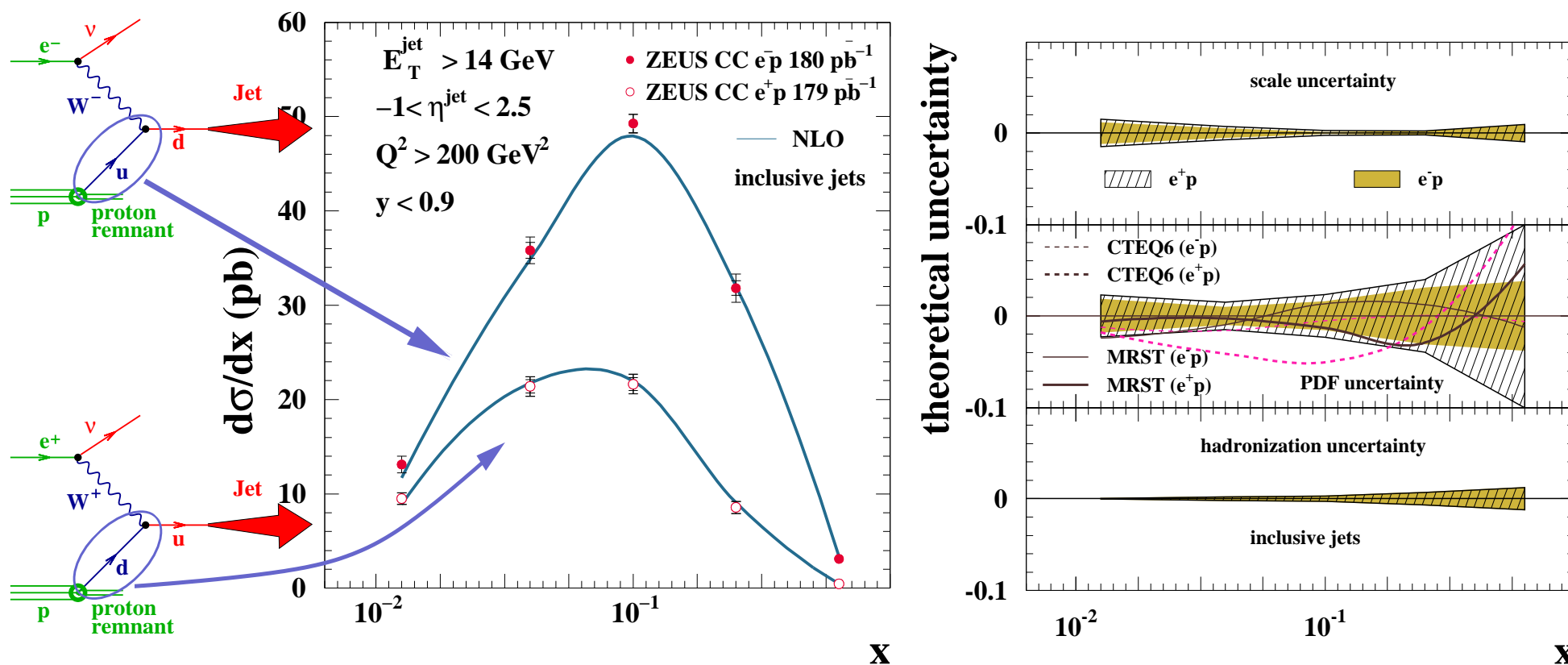
- Jets searched using the  $k_T$  cluster algorithm in LAB frame
- Kinematic region:  $Q^2 > 200 \text{ GeV}^2$  and  $y < 0.9$
- At least one jet with  $E_T^{\text{jet}} > 14 \text{ GeV}$  and  $-1 < \eta^{\text{jet}} < 2.5$
- $\mathcal{L} = 359 \text{ pb}^{-1}$  !!!
- The measured cross section for the  $e^+p$  sample decreases more rapidly than for the  $e^-p$  sample
- Comparison to NLO QCD predictions:
  - the shape and magnitude of the measured cross sections are reasonably well described by the predictions
- Ratio of  $e^-p$  to  $e^+p$  cross sections expected to be  $\approx 2$ 
  - increase at high  $E_T^{\text{jet}}$  values expected due to increasing contribution from valence-quark densities at high  $x$
  - both reactions are sensitive to different quark flavours



# CC DIS and the proton PDFs



- Inclusive-jet cross sections in charged-current deep inelastic  $e^\pm p$  scattering:



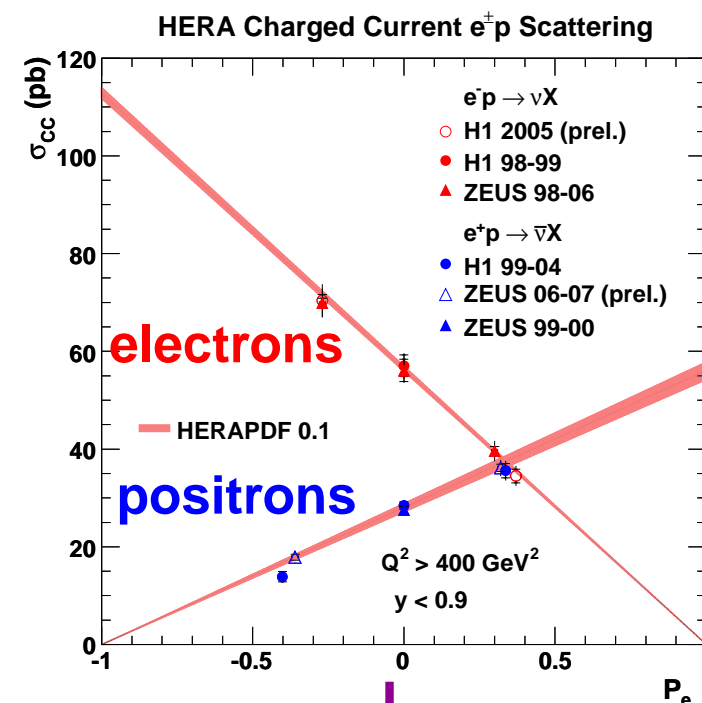
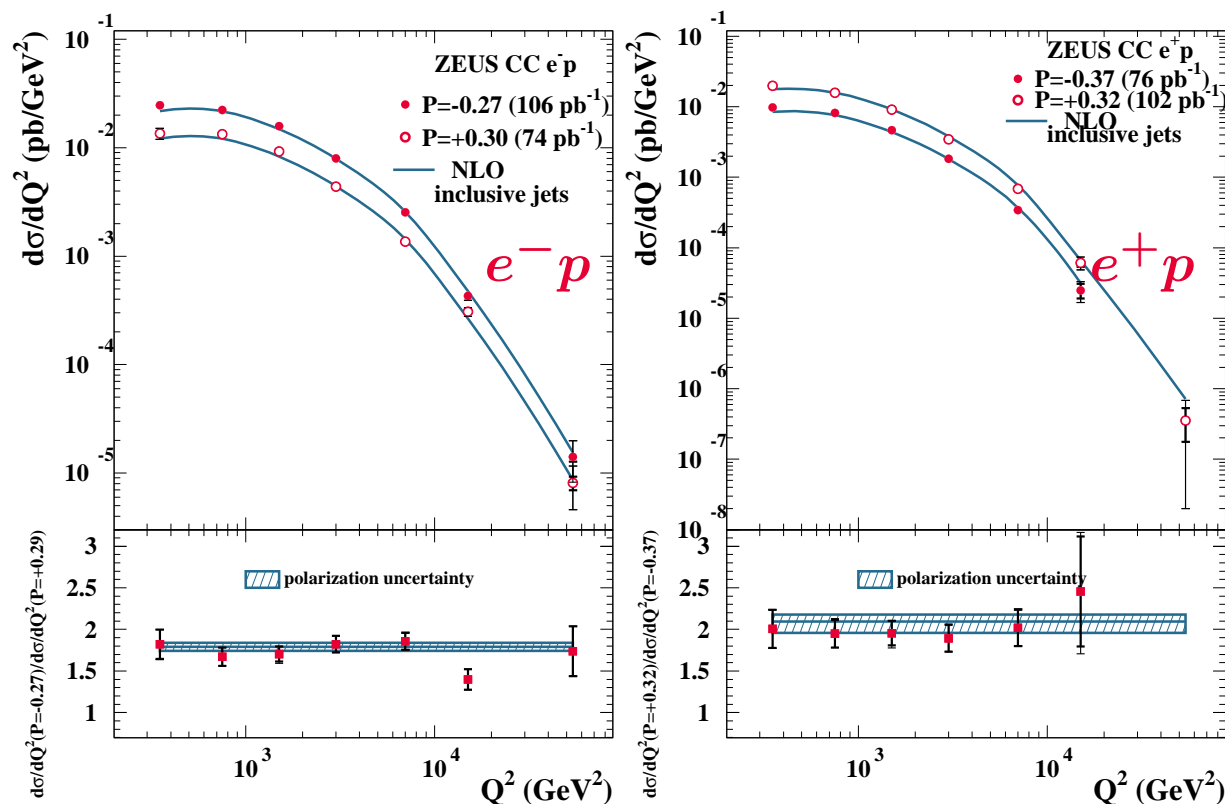
- Good description of data by NLO QCD calculations
- Theoretical uncertainties dominated by PDF uncertainty
- measured cross sections can help to constrain further  $u$  and  $d$  PDFs

# CC DIS and polarisation



- Inclusive-jet cross sections in charged current DIS with longitudinally-polarised  $e^\pm$  beams
- SM prediction for polarisation dependence:

$$\sigma_{CC}^\pm(P_e) = (1 \pm P_e)\sigma_{CC}^0$$



“total” CC  $e^\pm$  cross section vs  $P_e$

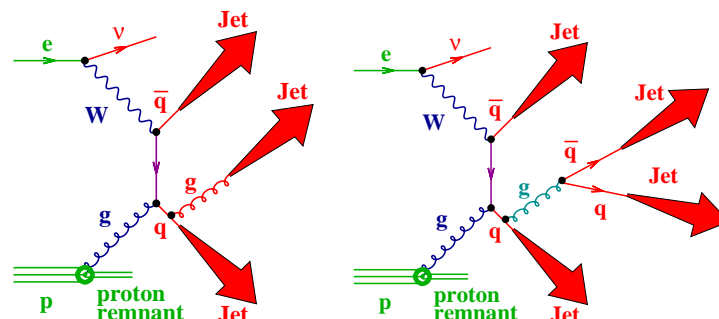
→ jet cross sections in CC  $e^\pm$  for different  $P_e$

⇒ Good agreement with SM predictions

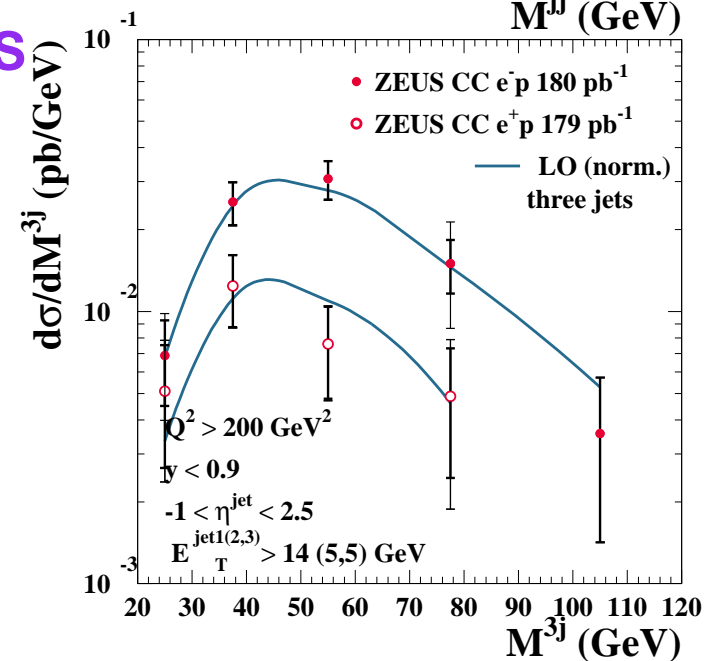
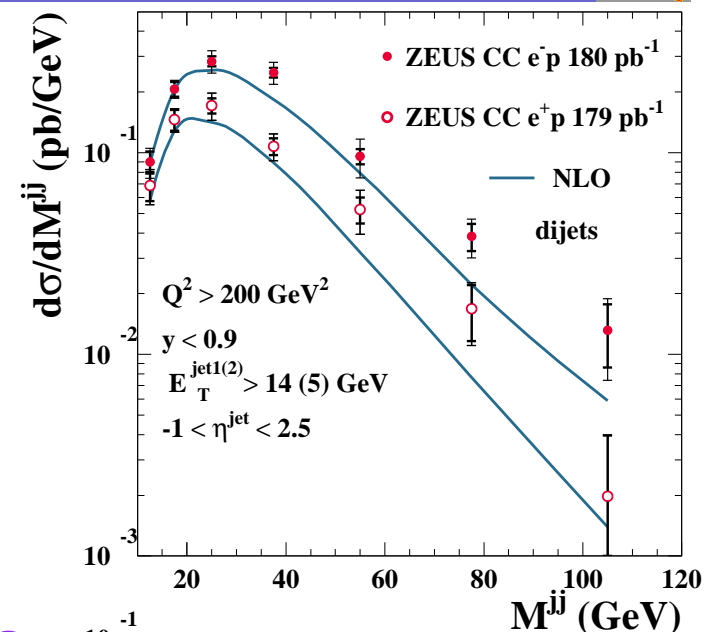
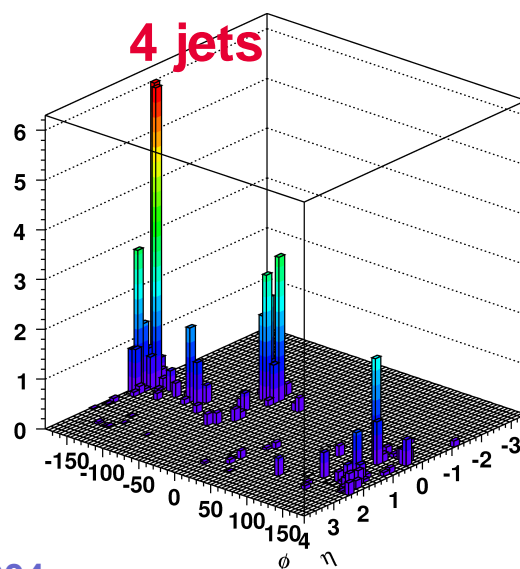
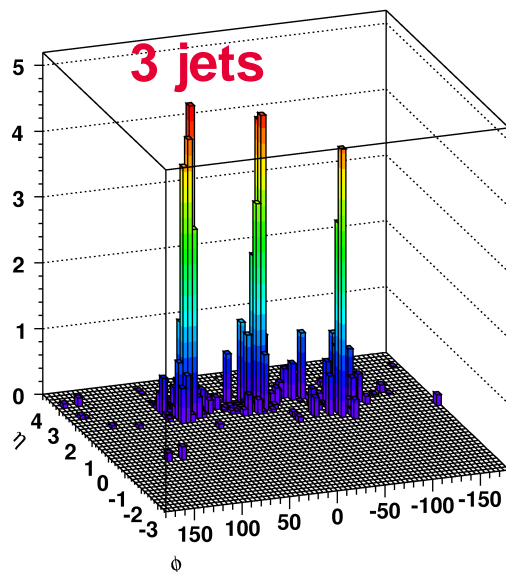
# Multi-jet production in CC DIS and QCD



- Additional jets with  $E_T^{\text{jet}} > 5 \text{ GeV}$



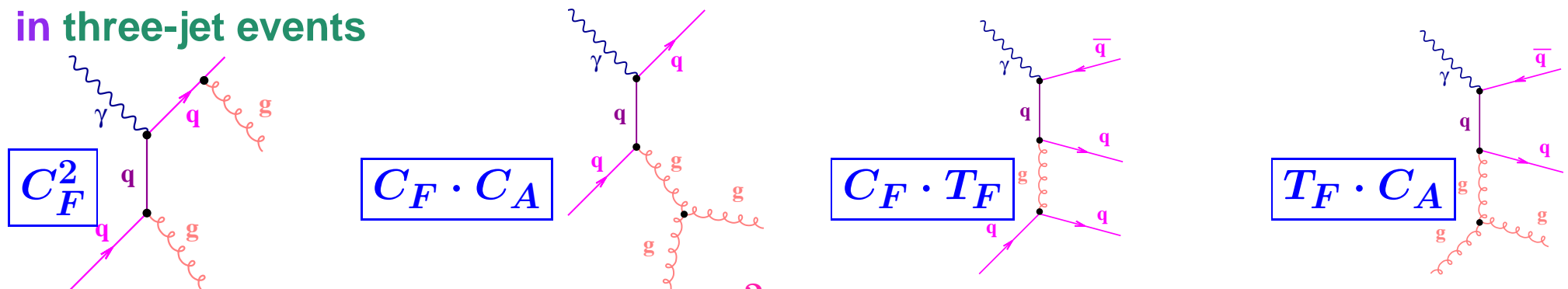
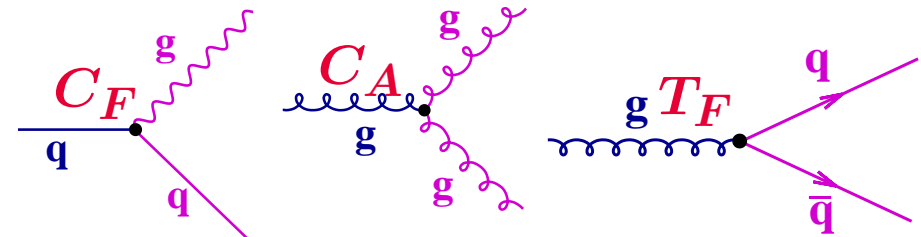
- The measured dijet cross sections are **not** well described by NLO
- The shape of the measured three-jet cross sections are well described by LO
- First observation of 3- and 4-jet production in CC DIS





# Underlying group symmetry and colour factors

- The colour factors represent the relative strength of the processes and their relative contributions
- Their values are predicted by the underlying gauge-group structure  
 $\rightarrow$  for  $SU(N)$ :  $C_F = (N^2 - 1)/2N$ ,  $C_A = N$ ,  $T_F = 1/2$
- Since the couplings  $qqg$  and  $ggg$  have different spin structures, the colour factors give rise to a specific pattern of angular correlations between the final-state jets
- Colour factors extensively studied at LEP by measuring angular correlations between final-state jets in  $e^+e^- \rightarrow 4$  jets and  $C_A/C_F$  and  $T_F/C_F$  determined
- In  $ep$  collisions at HERA, colour factors are studied using angular correlations in three-jet events



- The predicted cross section at  $\mathcal{O}(\alpha\alpha_s^2)$  can be written as

$$\sigma_{ep \rightarrow 3\text{jets}} = C_F^2 \cdot \sigma_A + C_F C_A \cdot \sigma_B + C_F T_F \cdot \sigma_C + T_F C_A \cdot \sigma_D$$



# Angular correlations in three-jet events



- Variables to highlight the contributions from the different colour configurations  
→ angular correlations between the three jets

→  $\theta_H$ : the angle between the plane determined by the highest  $E_T^{\text{jet}}$  and the beam and the plane determined by the two lowest  $E_T^{\text{jet}}$  jets (Muñoz-Tapia, Stirling)

→  $\alpha_{23}$ : the angle between the two lowest  $E_T^{\text{jet}}$  jets (inspired by the variable  $\alpha_{34}^{e^+e^-}$  for  $e^+e^- \rightarrow 4\text{jets}$ )

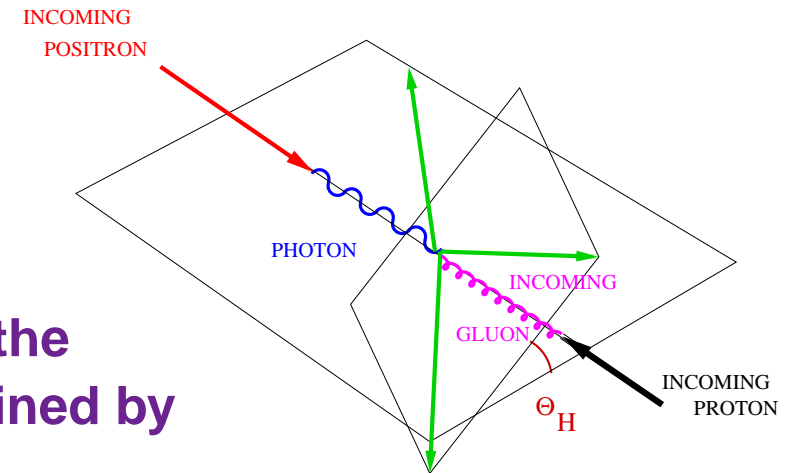
→  $\beta_{KSW}$ : defined by

$$\cos \beta_{KSW} = \cos \frac{1}{2} [\angle[(\vec{p}_1 \times \vec{p}_3), (\vec{p}_2 \times \vec{p}_B)] + \angle[(\vec{p}_1 \times \vec{p}_B), (\vec{p}_2 \times \vec{p}_3)]],$$

where  $\vec{p}_i$  is the momentum of jet  $i$  (ordered according to decreasing  $E_T^{\text{jet}}$ ) and  $\vec{p}_B$  is a unit vector in the direction of the proton beam

(inspired by the Körner-Schierholz-Willrodt angle  $\Phi_{KSW}^{e^+e^-}$  for  $e^+e^- \rightarrow 4\text{jets}$ )

→  $\eta_{\text{max}}^{\text{jet}}$ : pseudorapidity of the most forward jet

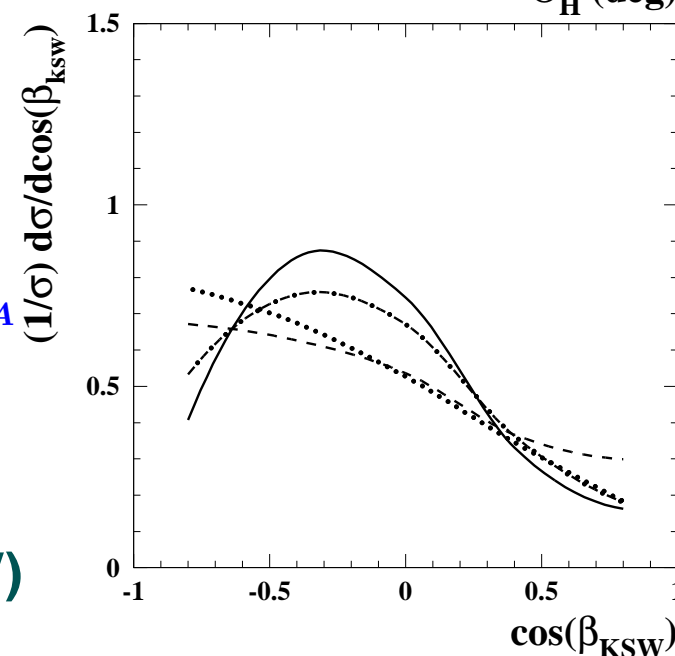
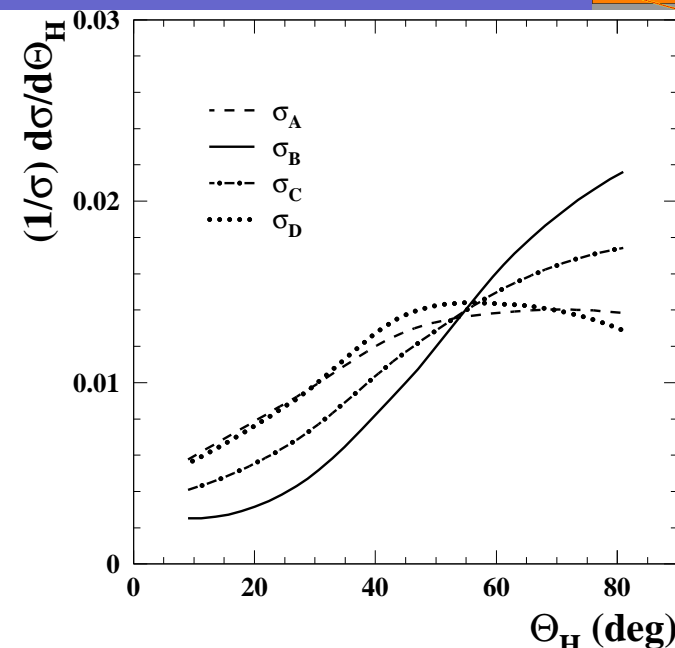
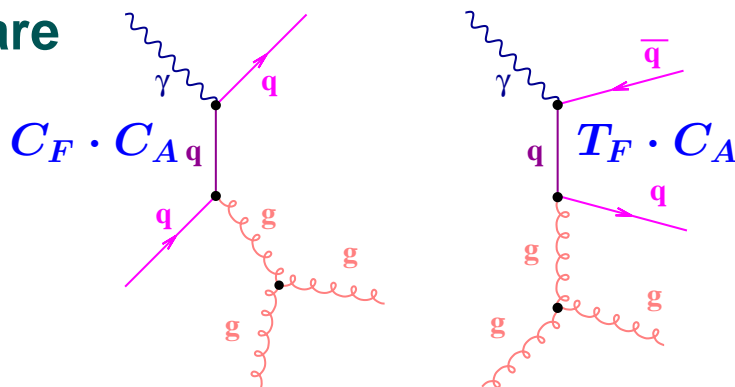


# Three-jet events in NC DIS and colour configurations



$$ep \rightarrow e + 3\text{jet} + X$$

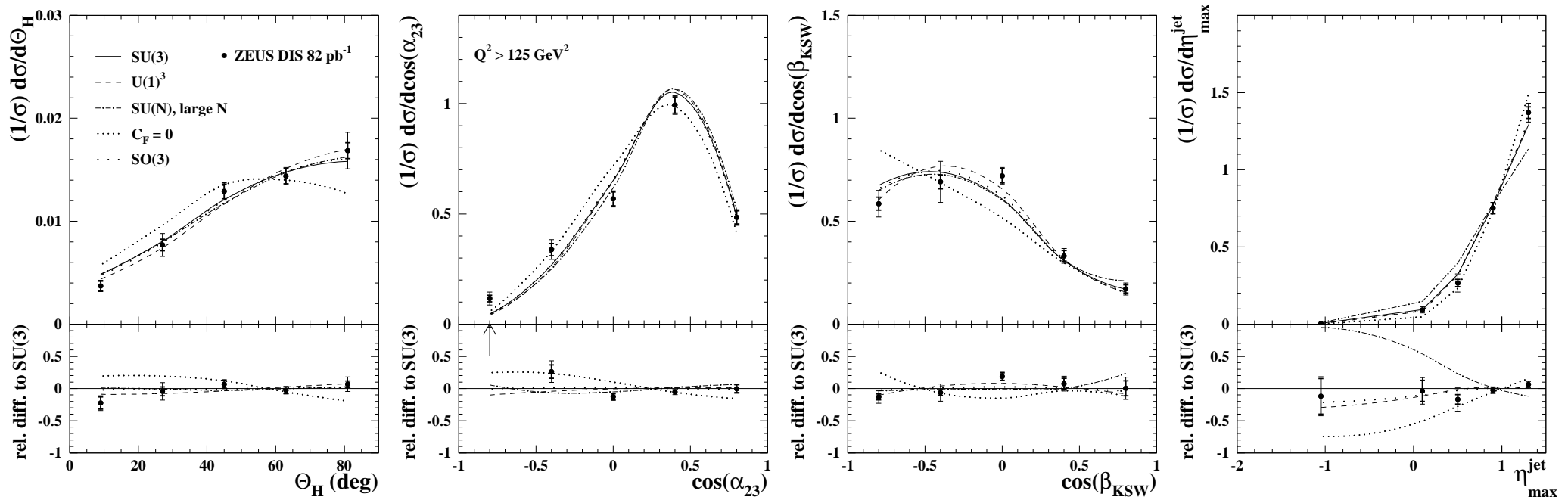
- Jets searched using the  $k_T$  cluster algorithm in Breit frame
- Kinematic region:  $Q^2 > 125 \text{ GeV}^2$  and  $|\cos \gamma_h| < 0.65$
- Three jets with  $E_{T,B}^{\text{jet}} > 8(5) \text{ GeV}$  and  $-2 < \eta_B^{\text{jet}} < 1.5$
- Predictions for the angular correlations show sensitivity to the different colour configurations
- The distribution for  $\sigma_B$  has a very different shape than the others in all variables
- The distribution for  $\sigma_D$  has a different shape than the others in  $\eta_{\text{max}}^{\text{jet}}$
- The predicted relative contributions of each colour configuration in SU(3) are
  - $\sigma_A (C_F^2)$ : 23%
  - $\sigma_B (C_F C_A)$ : 13%
  - $\sigma_C (C_F T_F)$ : 39%
  - $\sigma_D (T_F C_A)$ : 25%
- A total of 38% for diagrams which involve  $C_A$  (TGV)



# Angular correlations and underlying gauge symmetry



- Measured normalised three-jet cross sections in NC DIS vs  $\mathcal{O}(\alpha_s^2)$  predictions based on different symmetry groups

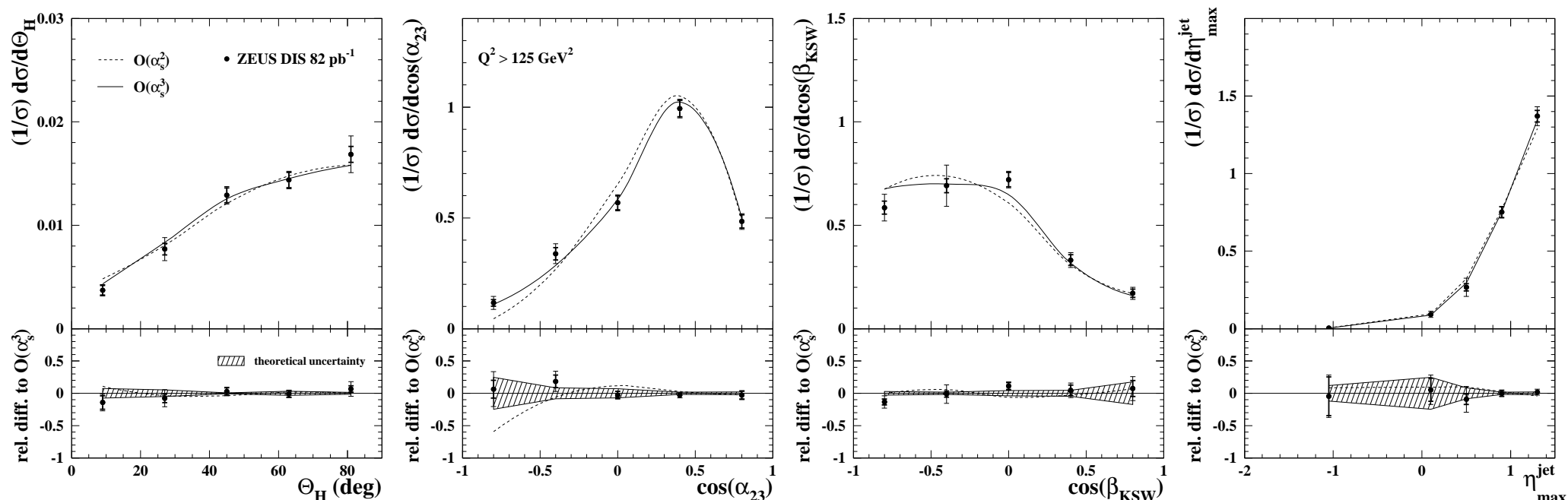


- The data disfavour SU(N) in the limit of large N and  $C_F = 0$  symmetry groups
- The measurements are consistent with the admixture of colour configurations as predicted by SU(3)
- the discrepancies observed can be attributed to higher orders →

# Angular correlations and underlying gauge symmetry



- Measured normalised three-jet cross sections in NC DIS vs  $\mathcal{O}(\alpha_s^3)$  predictions based on SU(3) symmetry group



- Very good description of data by SU(3) at  $\mathcal{O}(\alpha_s^3)$
- Potential to extract the colour factors from these measurements
  - NLO analysis and more statistics to be able to distinguish SU(3) and U(1)<sup>3</sup> are required

# Two-subject distributions



- **Subjects:** jet-like substructures identified by reapplying the  $k_T$  algorithm at smaller values of the resolution parameter  $y_{\text{cut}}$

- Subject distributions can be used to study:

→ pattern of parton radiation from a primary parton

→ direct test of splitting functions  $P_{ab}(z, \mu)$  and their scale dependence

→ colour coherence

→ soft gluon radiation tends to be emitted towards proton direction

- Measurements of normalised cross sections as functions of

$$E_T^{\text{sbj}} / E_T^{\text{jet}}, \eta^{\text{sbj}} - \eta^{\text{jet}}, |\phi^{\text{sbj}} - \phi^{\text{jet}}| \text{ and } \alpha^{\text{sbj}}$$

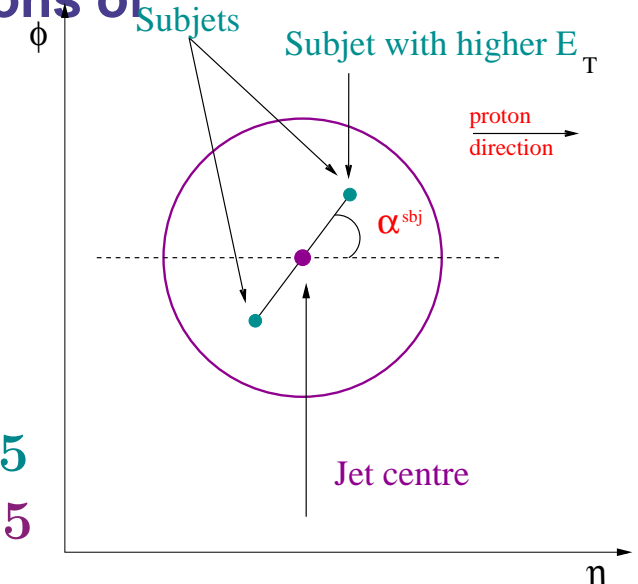
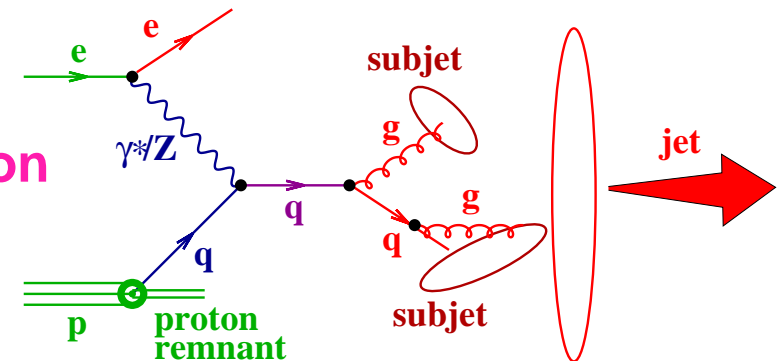
and their dependence with  $E_T^{\text{jet}}$ ,  $Q^2$  and  $x$

- Jets searched using the  $k_T$  cluster algorithm in LAB frame

- Kinematic region:  $Q^2 > 125 \text{ GeV}^2$

- At least one jet with  $E_T^{\text{jet}} > 14 \text{ GeV}$  and  $-1 < \eta^{\text{jet}} < 2.5$

- Final sample: jets that have two subjects for  $y_{\text{cut}} = 0.05$



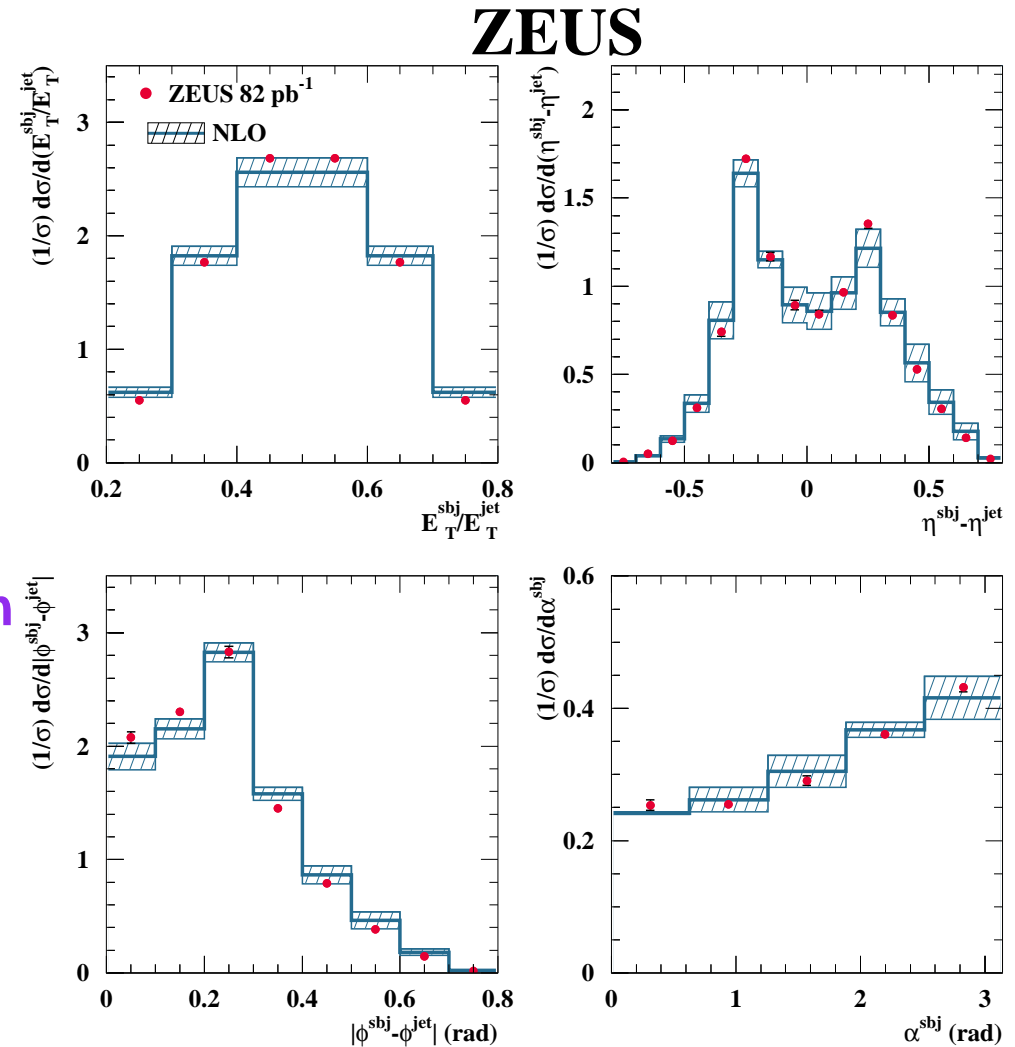
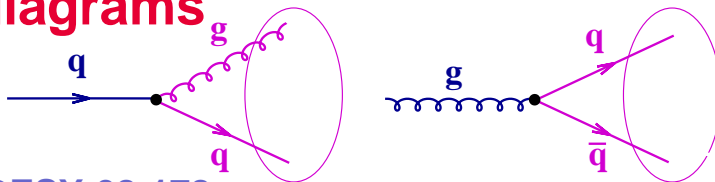
# Two-subjet distributions and pattern of parton radiation



## ● Normalised subjet cross sections compared with NLO calculations:

- $E_T^{\text{sbj}} / E_T^{\text{jet}}$ : the two subjets tend to have similar  $E_T^{\text{sbj}}$
- $\eta^{\text{sbj}} - \eta^{\text{jet}}$ : asymmetric two-peak structure
- $|\phi^{\text{sbj}} - \phi^{\text{jet}}|$ : suppression around 0 because the two subjets cannot be resolved when close
- $\alpha^{\text{sbj}}$ : higher  $E_T^{\text{sbj}}$  subjet tends to be in rear direction  
→ consistent with asymmetric peaks of  $\eta^{\text{sbj}} - \eta^{\text{jet}}$

→ The NLO predictions, which contain these diagrams

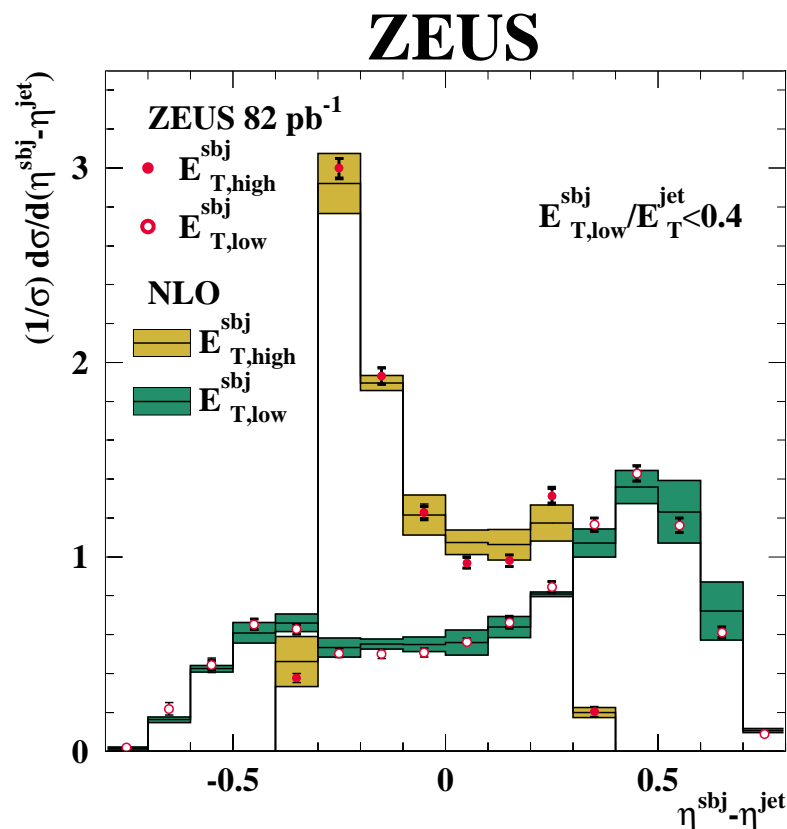


describe the data adequately

# Two-subjet distributions and colour coherence



- $\eta^{\text{sbj}} - \eta^{\text{jet}}$  normalised cross section for  $E_{T,\text{low}}^{\text{sbj}}/E_T^{\text{jet}} < 0.4$



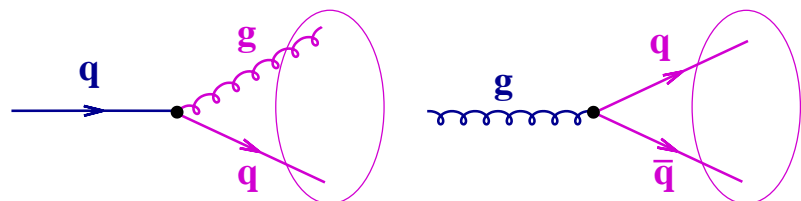
- The higher (lower)  $E_T^{\text{sbj}}$  subjet tends to be in the rear (forward) direction
- colour-coherence effects between the initial and final states



# Two-subjet distributions and parton splitting



## ● Comparison with predictions for quark- and gluon-induced processes



### → NLO prediction:

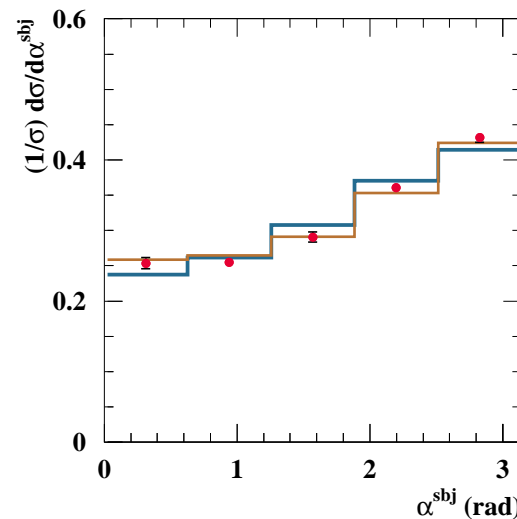
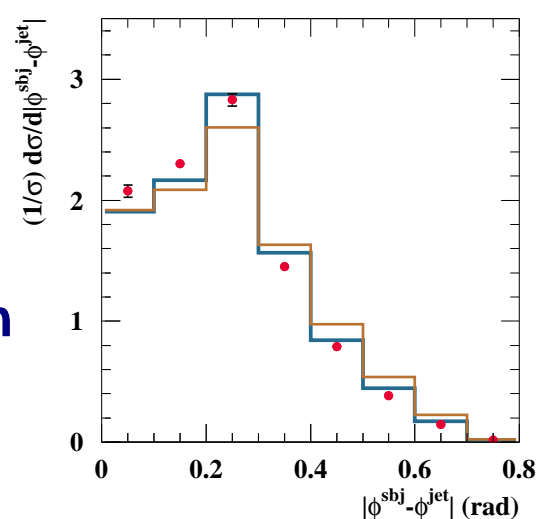
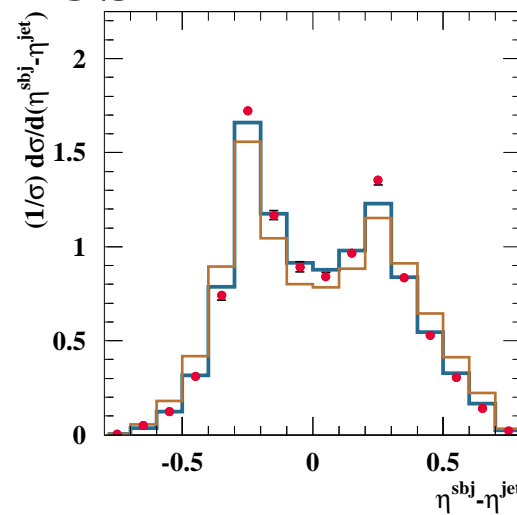
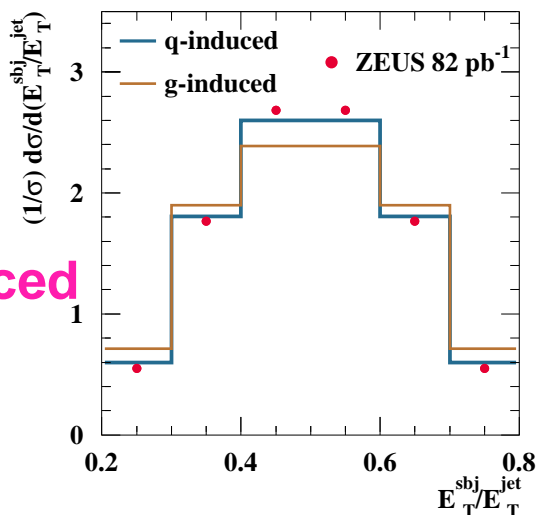
81% of q-induced and 19% of g-induced

## ● Predictions for these two types of processes are different:

- the two subjects in q-induced have more similar  $E_T^{sbj}$  and are closer to each other than in g-induced

## → The data are better described by the calculations for jets arising from the splitting of a quark into a quark-gluon pair

# ZEUS

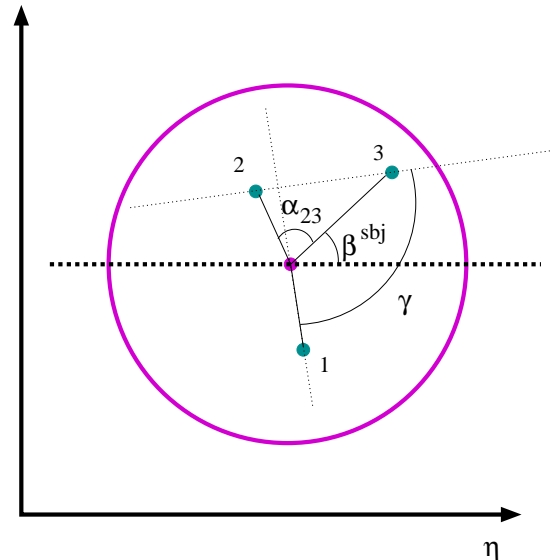


# Three-subjet distributions



- Subjet distributions can be used to study:
  - pattern of parton radiation from a primary parton
    - direct test of splitting functions  $P_{ab}(z, \mu)$  and their scale dependence
  - colour coherence
    - soft gluon radiation tends to be emitted towards proton direction
  - underlying group symmetry
    - angular correlations between three subjets should show sensitivity to the colour configurations
- Measurements of normalised cross sections as functions of
 
$$E_T^{\text{sbj}} / E_T^{\text{jet}}, \eta^{\text{sbj}} - \eta^{\text{jet}}, |\phi^{\text{sbj}} - \phi^{\text{jet}}|, \beta^{\text{sbj}},$$

$$\theta_H, \alpha_{23} \text{ and } \gamma$$
  - Jets searched using the  $k_T$  cluster algorithm in LAB frame
  - Kinematic region:  $Q^2 > 125 \text{ GeV}^2$
  - At least one jet with  $E_T^{\text{jet}} > 14 \text{ GeV}$  and  $-1 < \eta^{\text{jet}} < 2.5$
  - Final sample: jets that have three subjets for  $y_{\text{cut}} = 0.03$

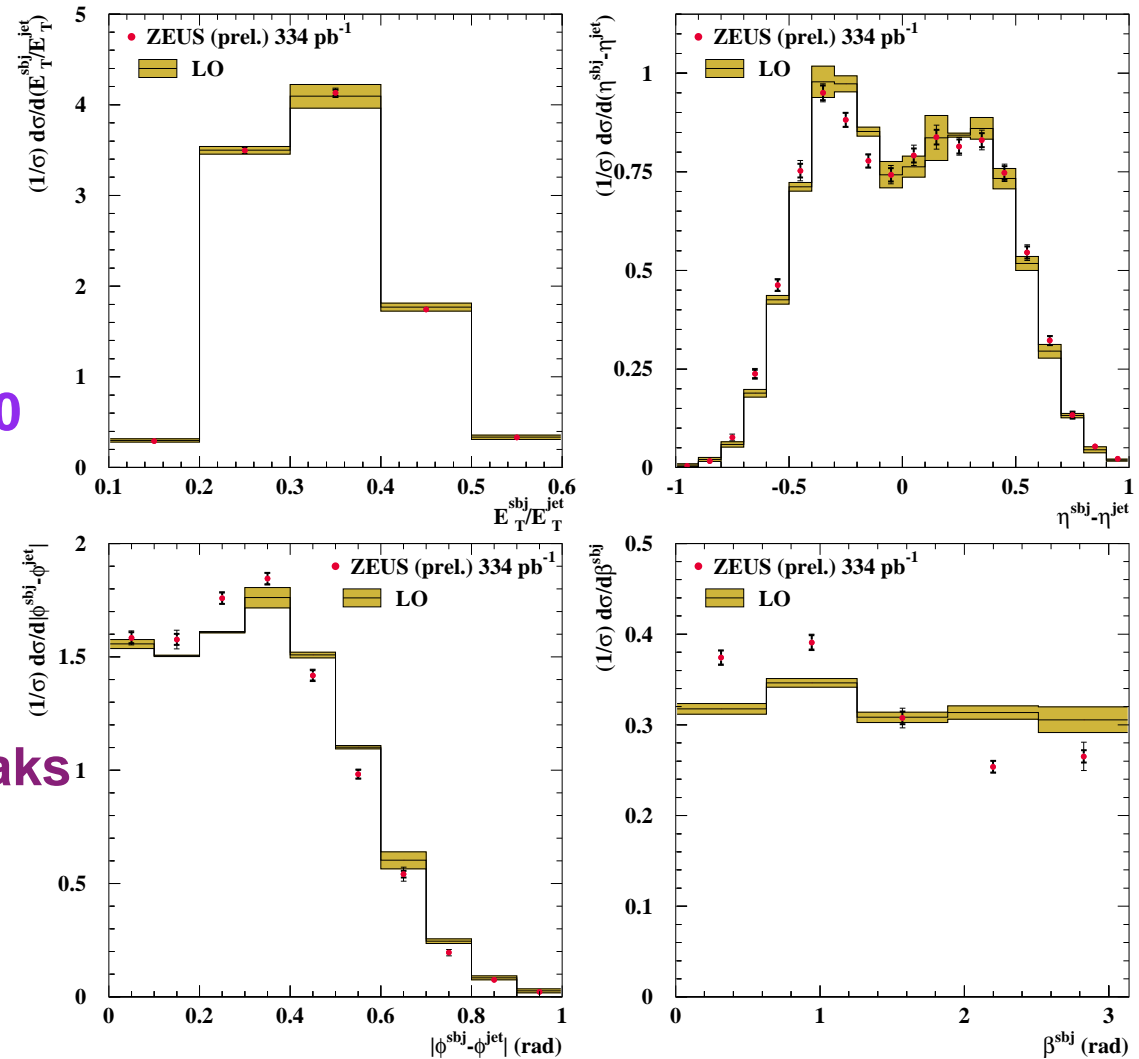


# Three-subjet distributions and pattern of parton radiation



## ● Normalised subjet cross sections compared with LO calculations:

- $E_T^{\text{sbj}} / E_T^{\text{jet}}$ : the three subjects tend to have similar  $E_T^{\text{sbj}}$
  - $\eta^{\text{sbj}} - \eta^{\text{jet}}$ : asymmetric two-peak structure
  - $|\phi^{\text{sbj}} - \phi^{\text{jet}}|$ : suppression around 0 because the subjects cannot be resolved when close
  - $\beta^{\text{sbj}}$ : lowest  $E_T^{\text{sbj}}$  subjet tends to be in forward direction
    - consistent with asymmetric peaks of  $\eta^{\text{sbj}} - \eta^{\text{jet}}$
- The LO predictions describe the data adequately, except for  $\beta^{\text{sbj}}$  (higher orders?)

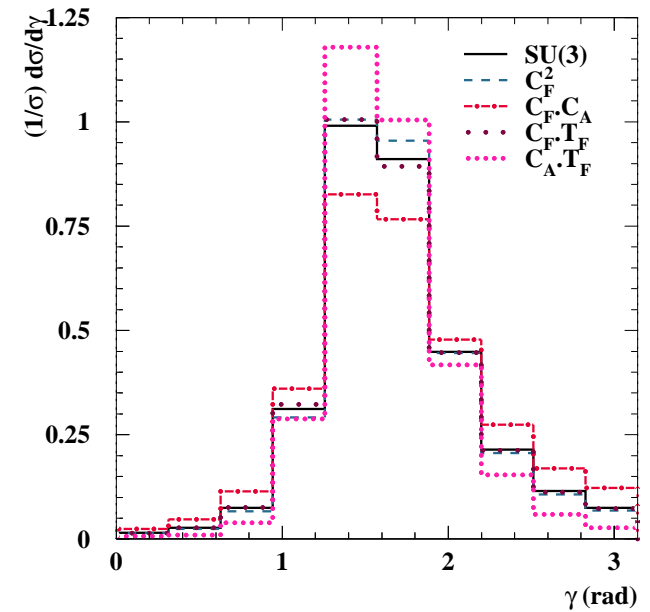
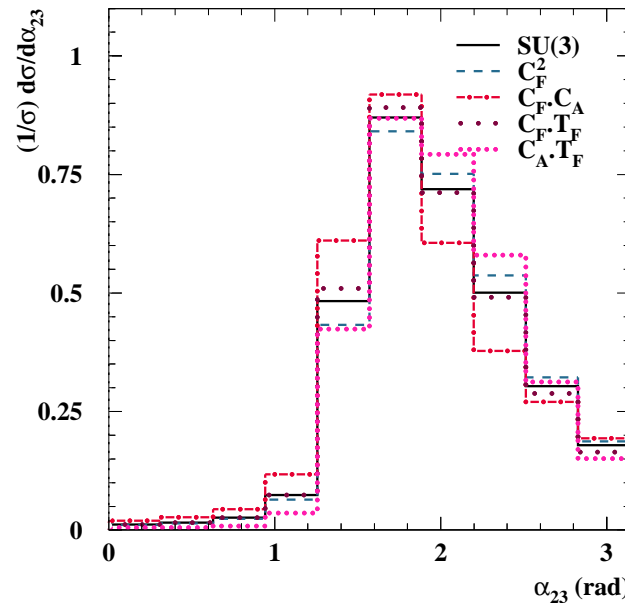
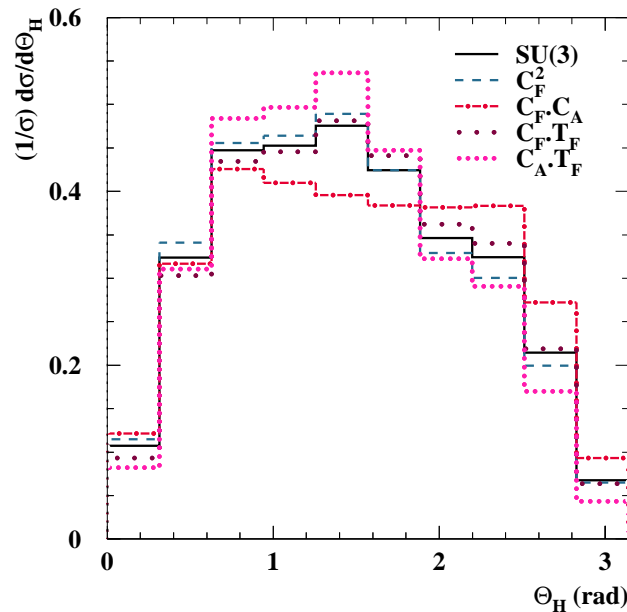
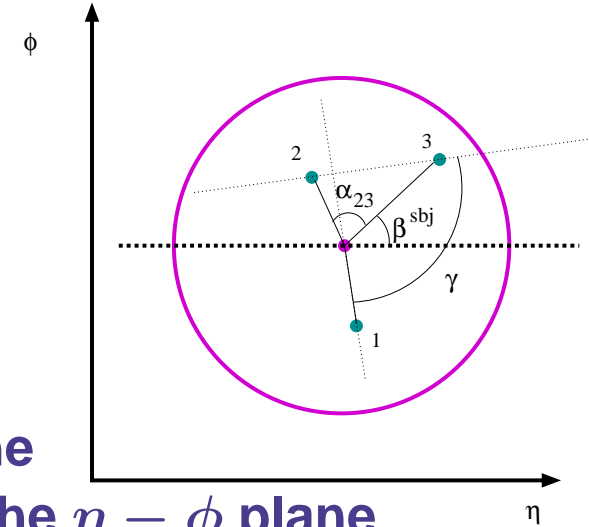


# Angular correlations in three-subjet events



## ● Three-subjet angular correlations

- $\theta_H$ : the angle between the planes determined by the highest- $E_T$  subjet and the beam and the two lowest- $E_T$  subjets
- $\alpha_{23}$ : the angle between the two lowest- $E_T$  subjets in the  $\eta - \phi$  plane
- $\gamma$ : the angle between the highest- $E_T$  subjet and the vector difference of the two lowest- $E_T$  subjets in the  $\eta - \phi$  plane

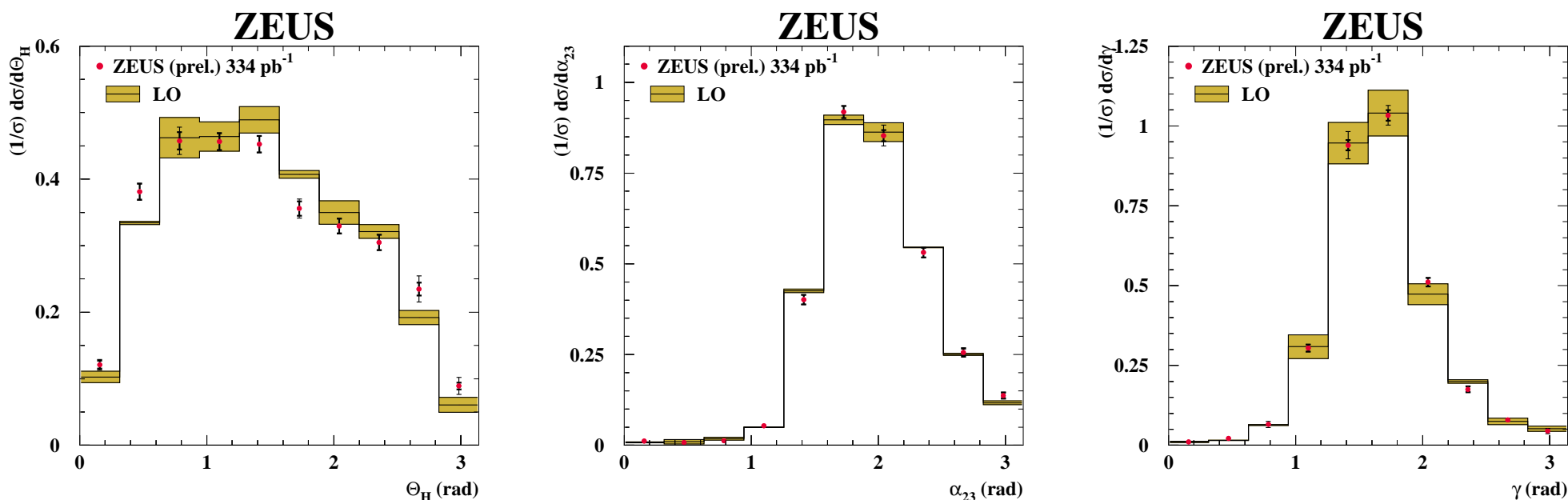


→ The  $C_F \cdot C_A$  and  $C_A \cdot T_F$  configurations display distinct behaviour

# Angular correlations and underlying gauge symmetry



- Measured normalised three-subjet cross sections in NC DIS vs  $\mathcal{O}(\alpha_s^2)$  predictions based on SU(3)



- The measurements are consistent with the admixture of colour configurations as predicted by SU(3)
- SU(3) predicts: 47% ( $C_F^2$ ), 17% ( $C_F \cdot C_A$ ), 27% ( $C_F \cdot T_F$ ) and 9% ( $T_F \cdot C_A$ )  
 → a total of 26% for the components which involve  $C_A$  (TGV)
- Potential to extract the colour factors from these measurements

# Conclusions



- Jet production and jet substructure are still being extensively studied at HERA
  - Results shown:
    - \* Multi-jet cross sections in CC DIS
    - \* Angular correlations in three-jet events
    - \* Two-subjet distributions
    - \* Three-subjet distributions
  - Measurements allow
    - ~> stringent tests of pQCD and the SM
    - ~> constraints on the proton PDFs
    - ~> test of the underlying gauge symmetry
    - ~> study of pattern of parton radiation
    - ~> study of colour coherence
- ↪ **Jet analysis at HERA:** a powerful tool that provides stringent tests of pQCD