

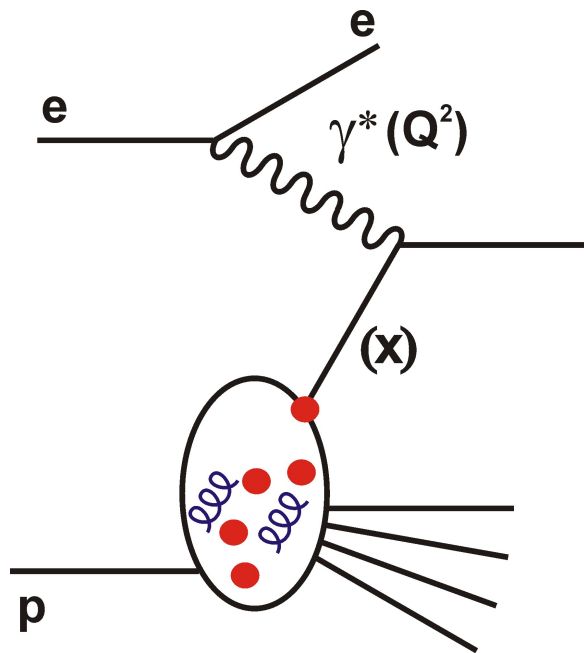
# Inclusive Deep Inelastic Scattering at HERA

Paul Newman  
(Birmingham)



... for the H1 & ZEUS collaborations

Supported in part by  
IPPP, Durham



Diffraction'10  
Otranto  
11 September 2010



# Proton "Structure"?

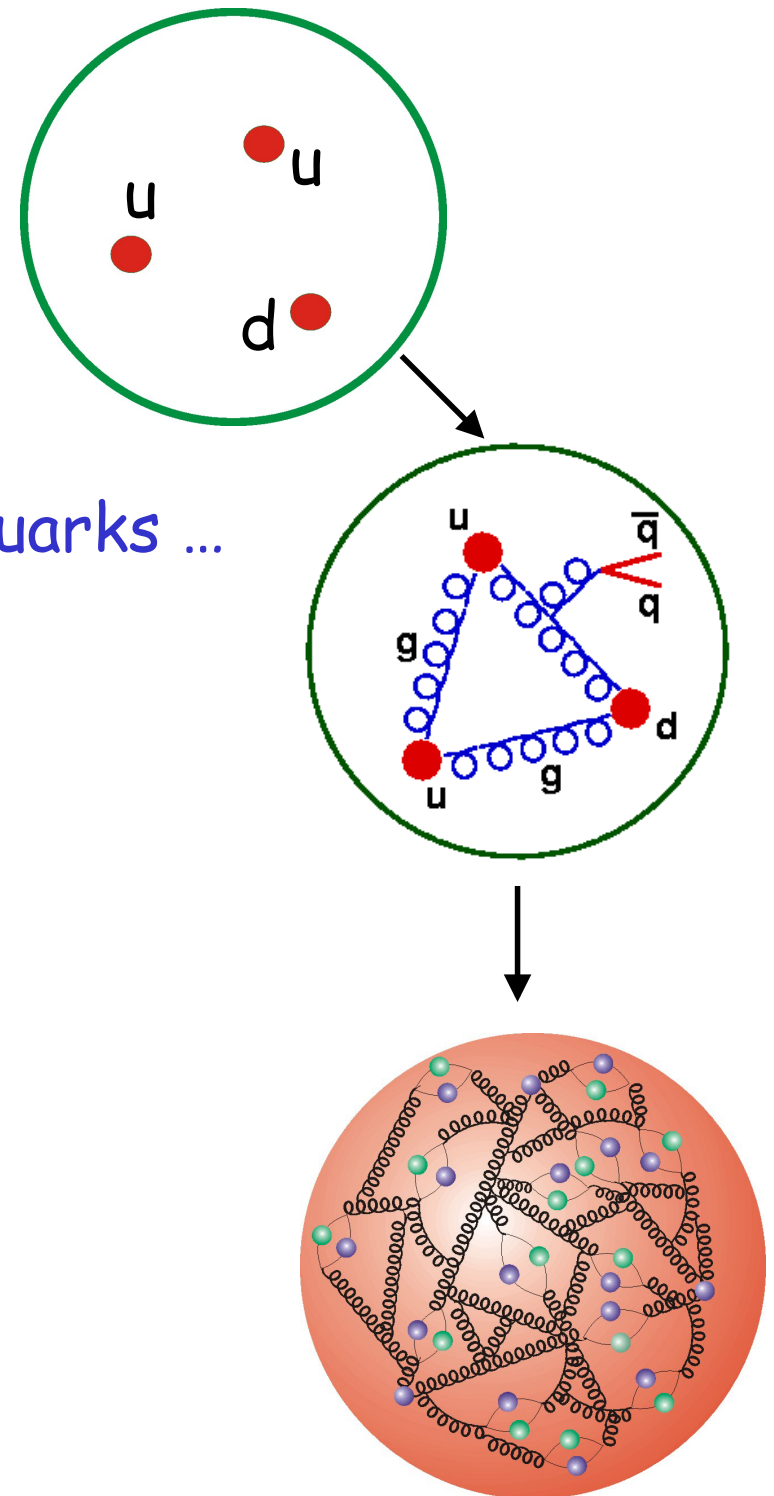
Proton constituents ...

2 up and 1 down **valence quarks**

... and some **gluons**

... and some **sea quarks**

... and lots more gluons and sea quarks ...





# Proton "Structure"?

Proton constituents ...

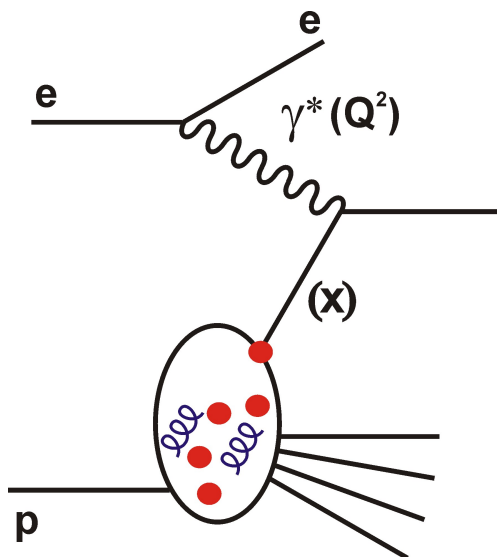
2 up and 1 down **valence quarks**

... and some **gluons**

... and some **sea quarks**

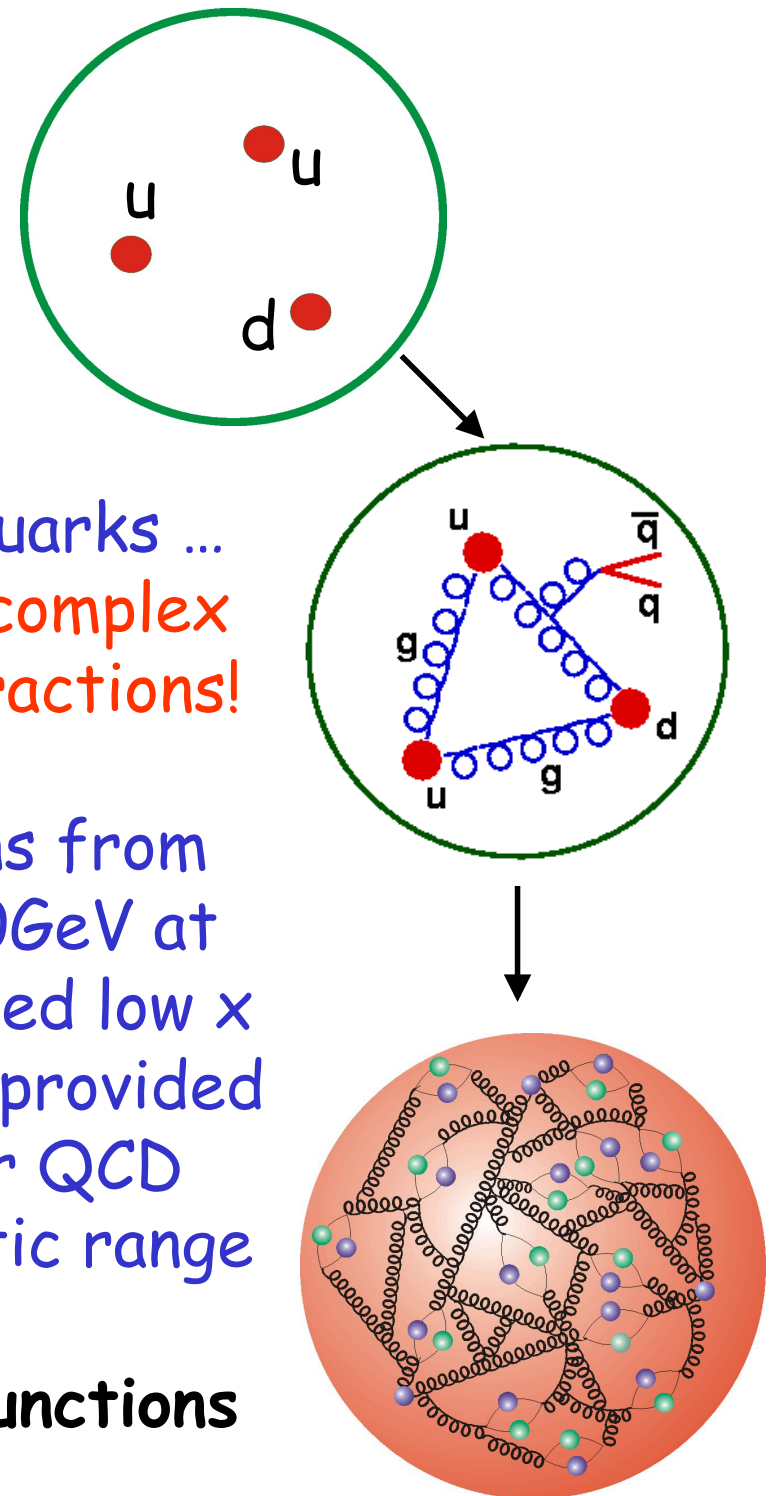
... and lots more gluons and sea quarks ...

→ strong interactions induce rich and complex  
'structure' of high energy proton interactions!



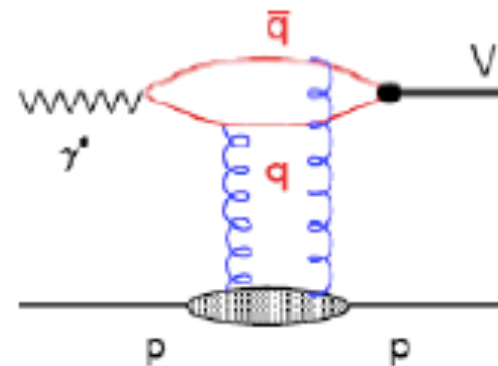
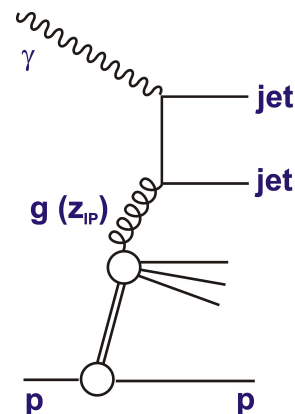
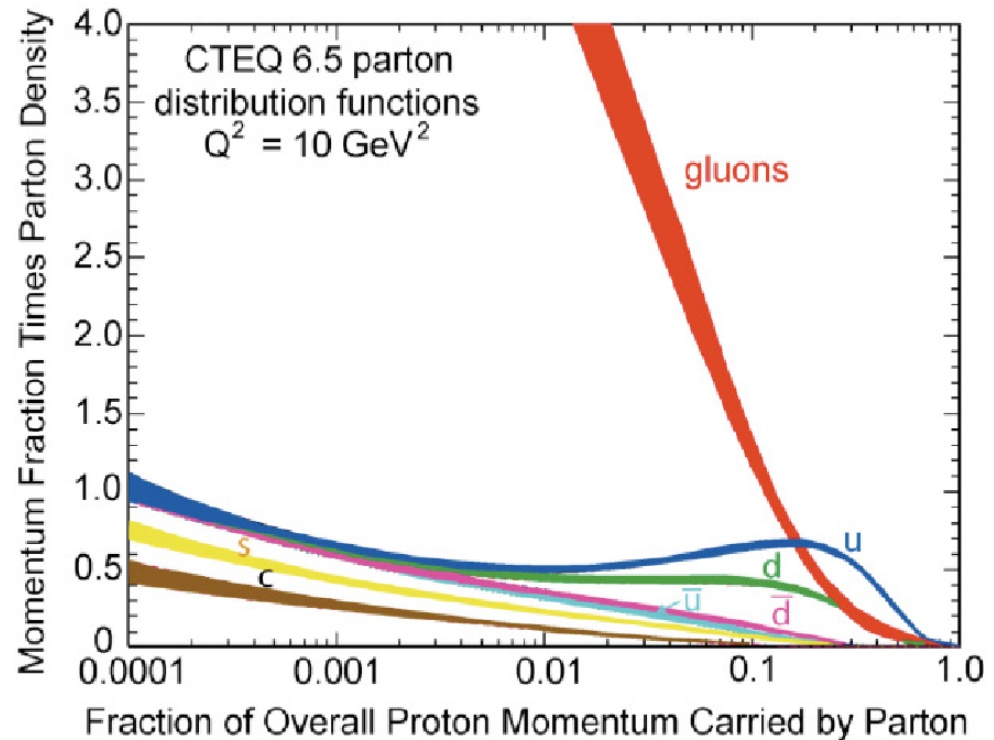
Scattering electrons from  
protons at  $\sqrt{s} > 300\text{GeV}$  at  
HERA has established low  $x$   
proton structure & provided  
a testing ground for QCD  
over a huge kinematic range

... **parton density functions**



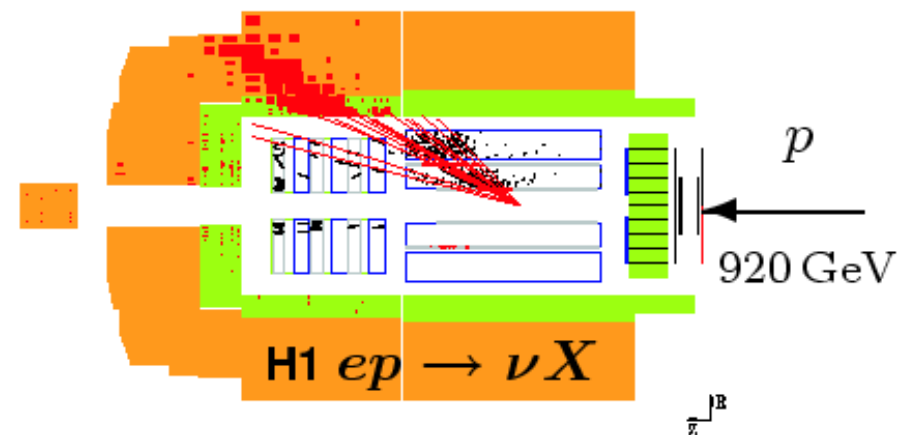
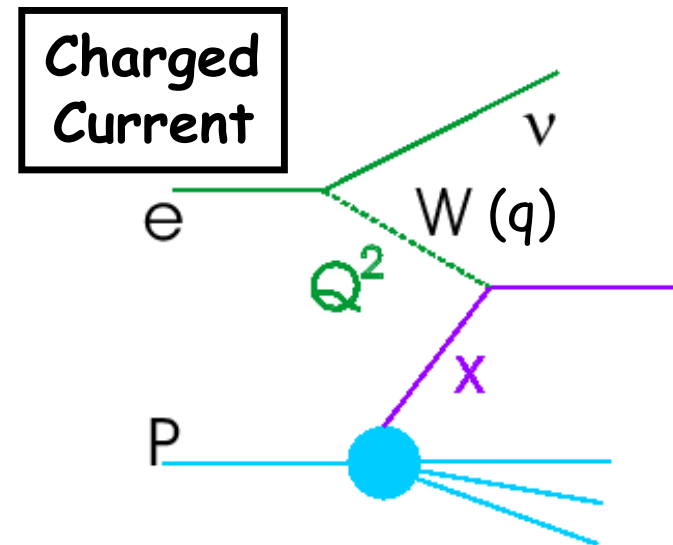
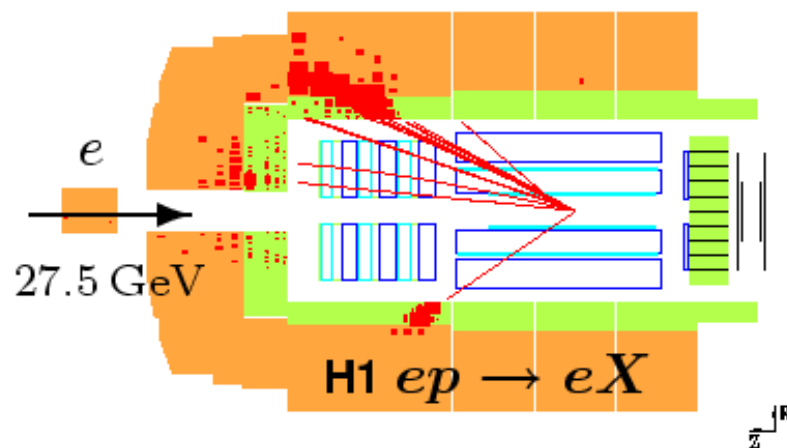
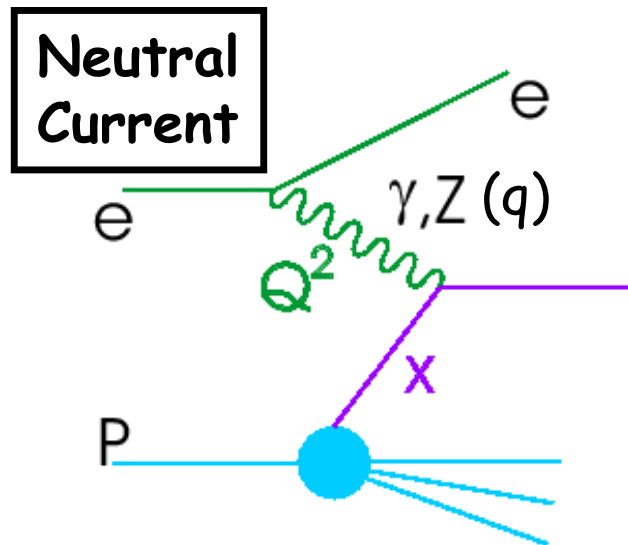
# Main Relation to Diffraction ... the Low $x$ Gluon

- Low  $x$  physics, as revealed by HERA, is the physics of huge gluon densities...
- Associated with a large ( $> 10\%$ ) contribution from diffractive processes





# Basic Deep Inelastic Scattering Processes

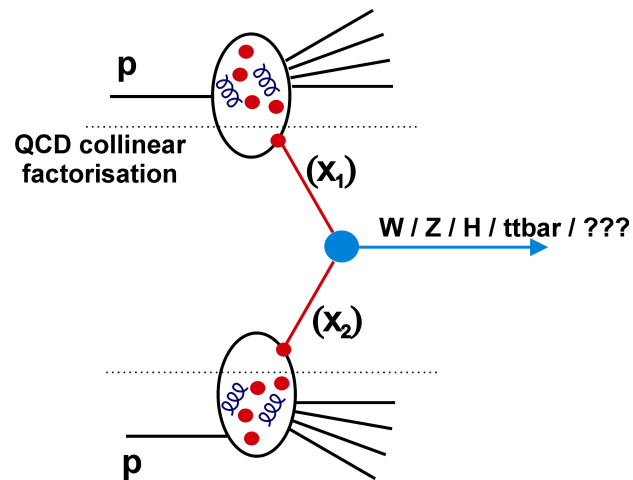


$Q^2 = -q^2$  : resolving power of interaction

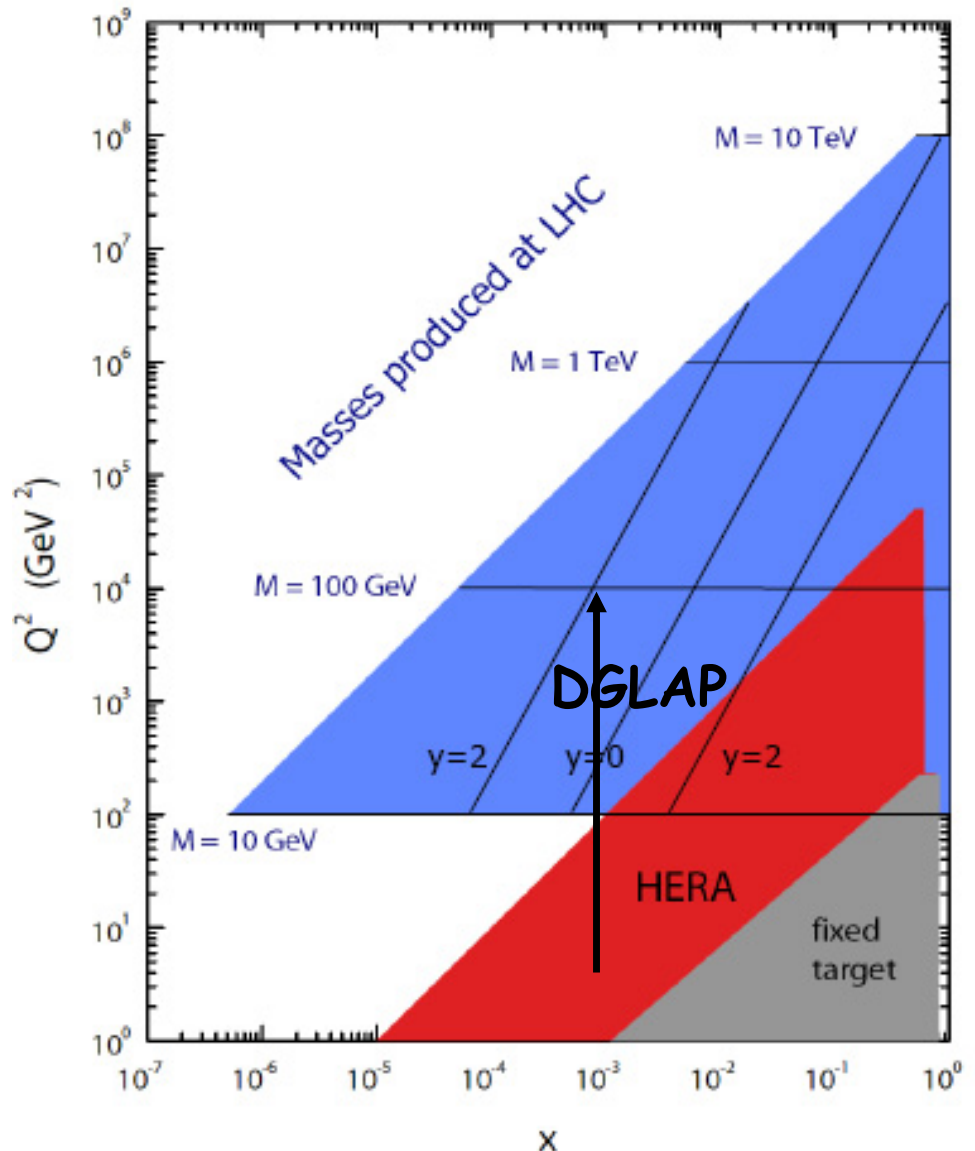
$x = Q^2 / 2q.p$  : fraction of struck quark / proton momentum

# HERA kinematic range

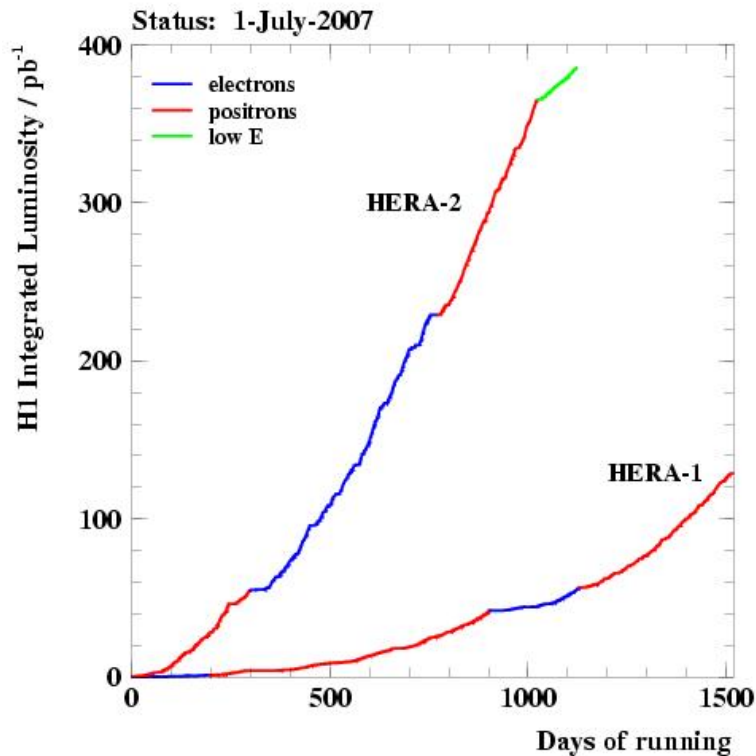
- Unprecedented low  $x$  and high  $Q^2$  coverage in DIS!
- **HERA + QCD factorisation**  
→ parton densities in full  $x$  range of LHC rapidity plateau



- Well established 'DGLAP' evolution equations generalise to any scale (for not too small  $x$ )

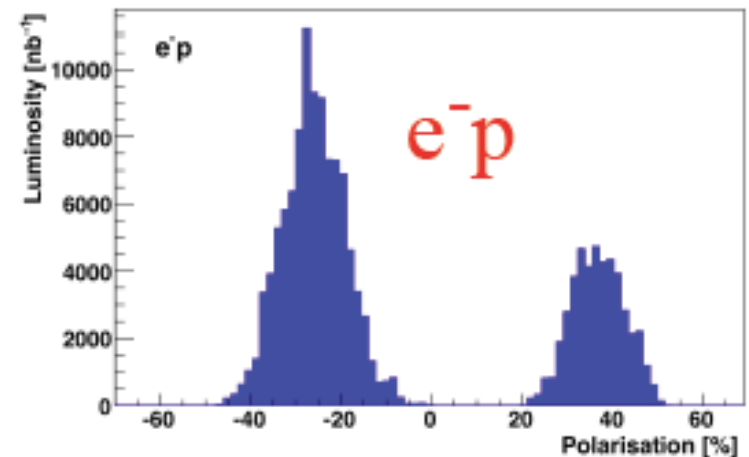
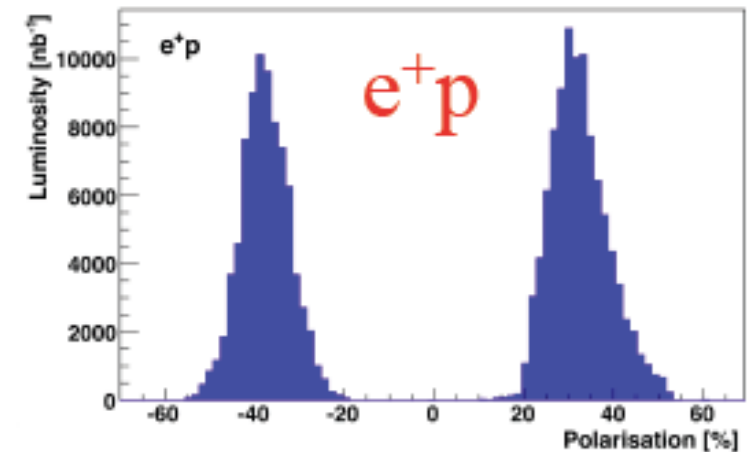


e.g. pp dijets at central rapidity:  $x_1 = x_2 = 2p_t / \sqrt{s}$



# Final HERA Data Samples

- Total of  $\sim 200 \text{ pb}^{-1} e^-p$ ,  $300 \text{ pb}^{-1} e^+p$  per experiment.
- Both lepton polarisation states
- $\sim 25 \text{ pb}^{-1}$  @ lower  $E_p = 575, 460 \text{ GeV}$

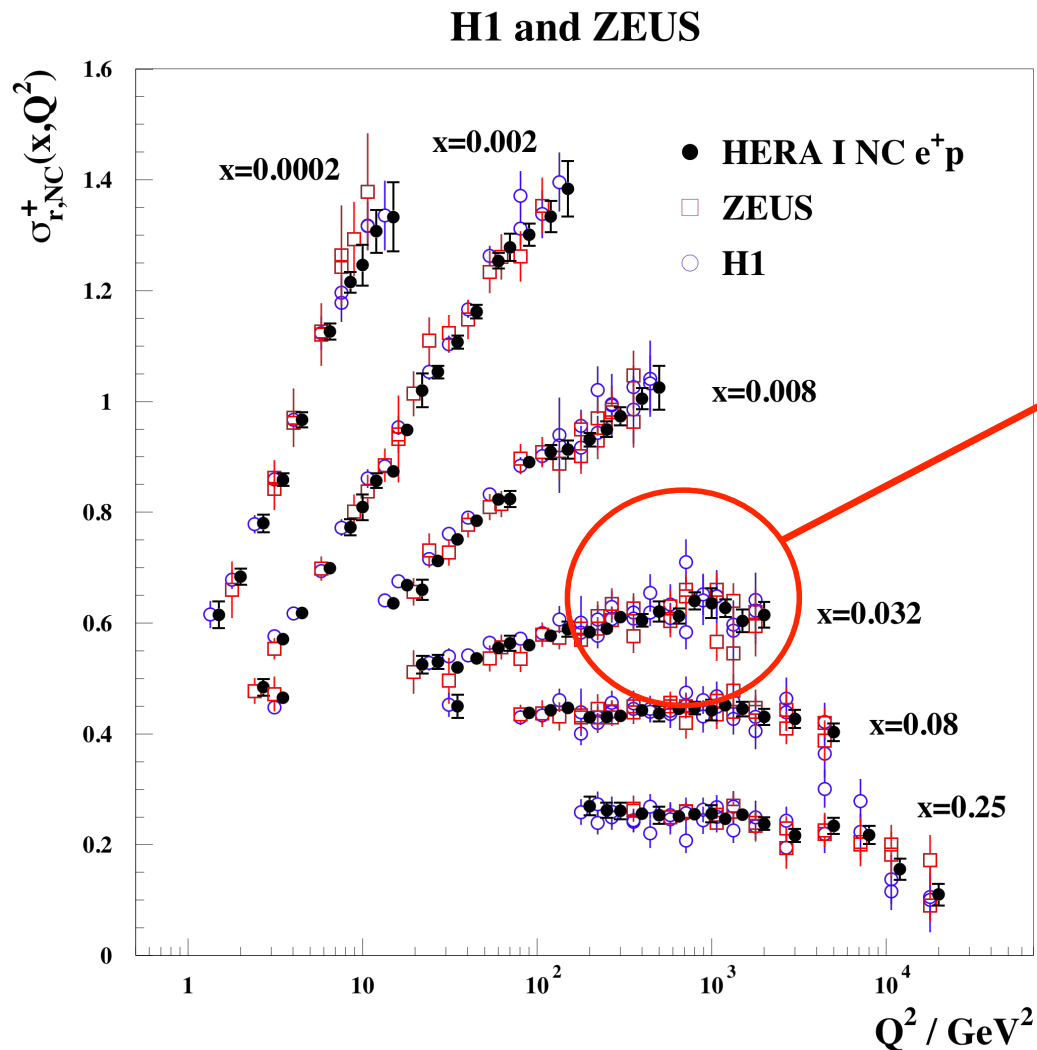


- HERA-I publications  $\sim$  complete
- Many HERA-II analyses still in progress (e.g. complicated final states such as diffraction)
- Work to combine H1, ZEUS results well underway



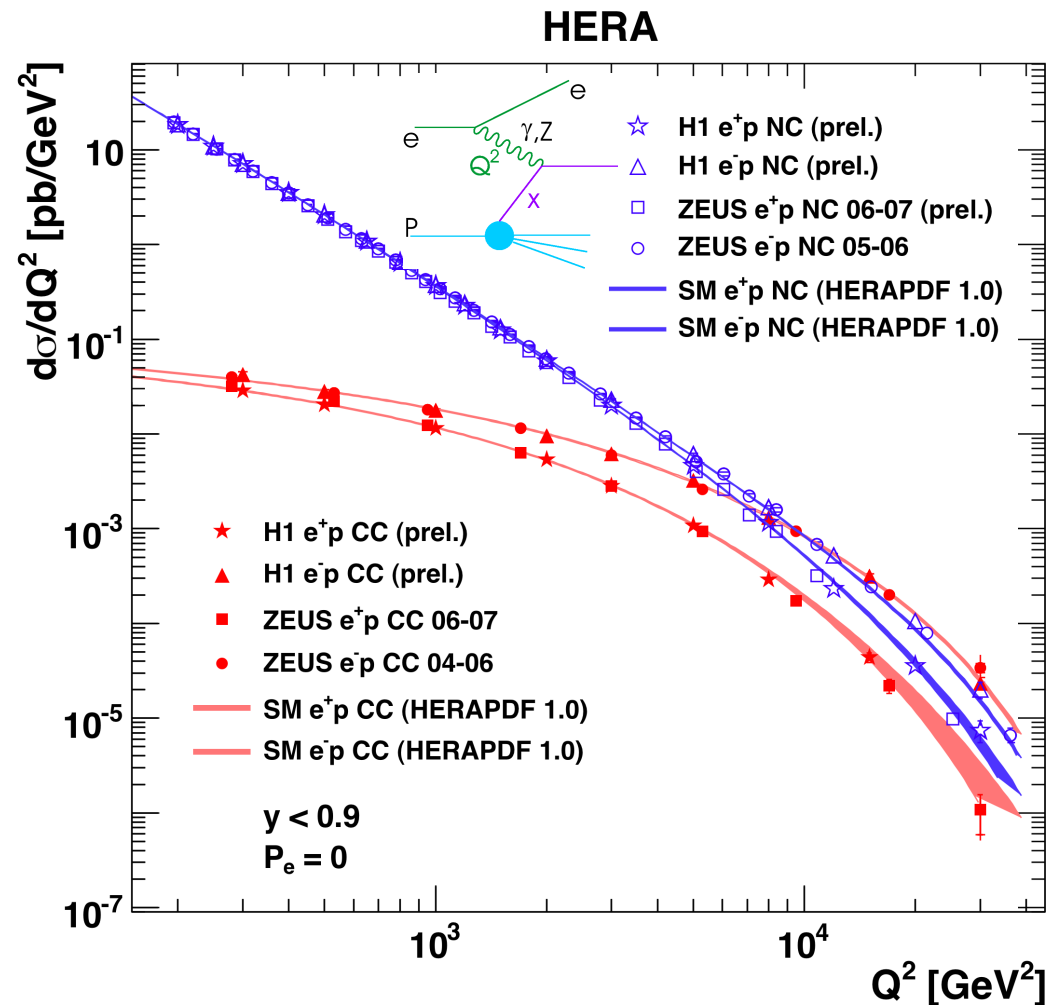
# The Power of Combinations [JHEP 1001:109 (2010)]

- Selected bins from the final combination of HERA-I NC data



Beyond the  $\sqrt{2}$  statistical improvement, effectively cross-calibrate to tackle (different) dominating H1, ZEUS systematics.

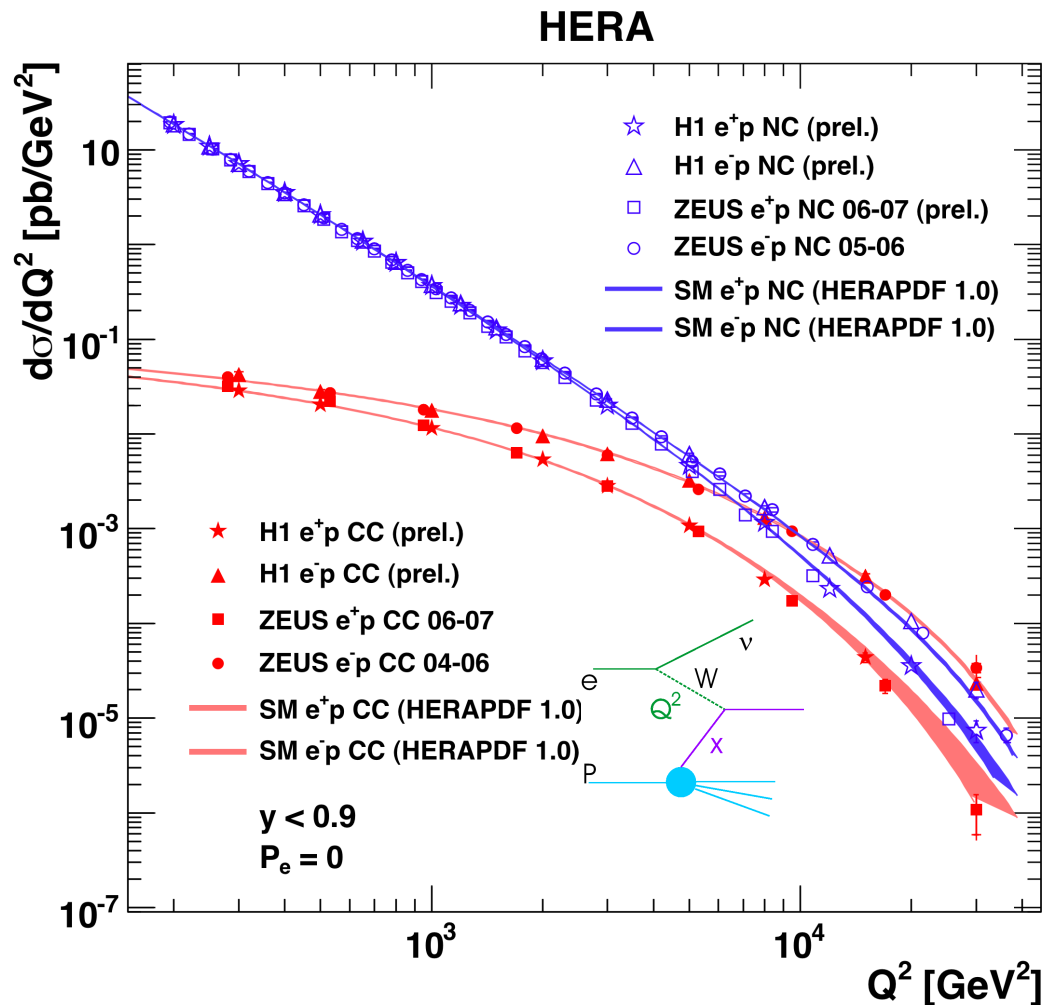
# Electroweak Unification for Space-like Bosons



## Neutral Current x-sec

$$\frac{d\sigma^{NC}}{dx dQ^2} \sim \alpha_{em}^2 \cdot \left(\frac{1}{Q^2}\right)^2 \cdot \tilde{\sigma}_{NC}$$

# Electroweak Unification for Space-like Bosons



## Neutral Current x-sec

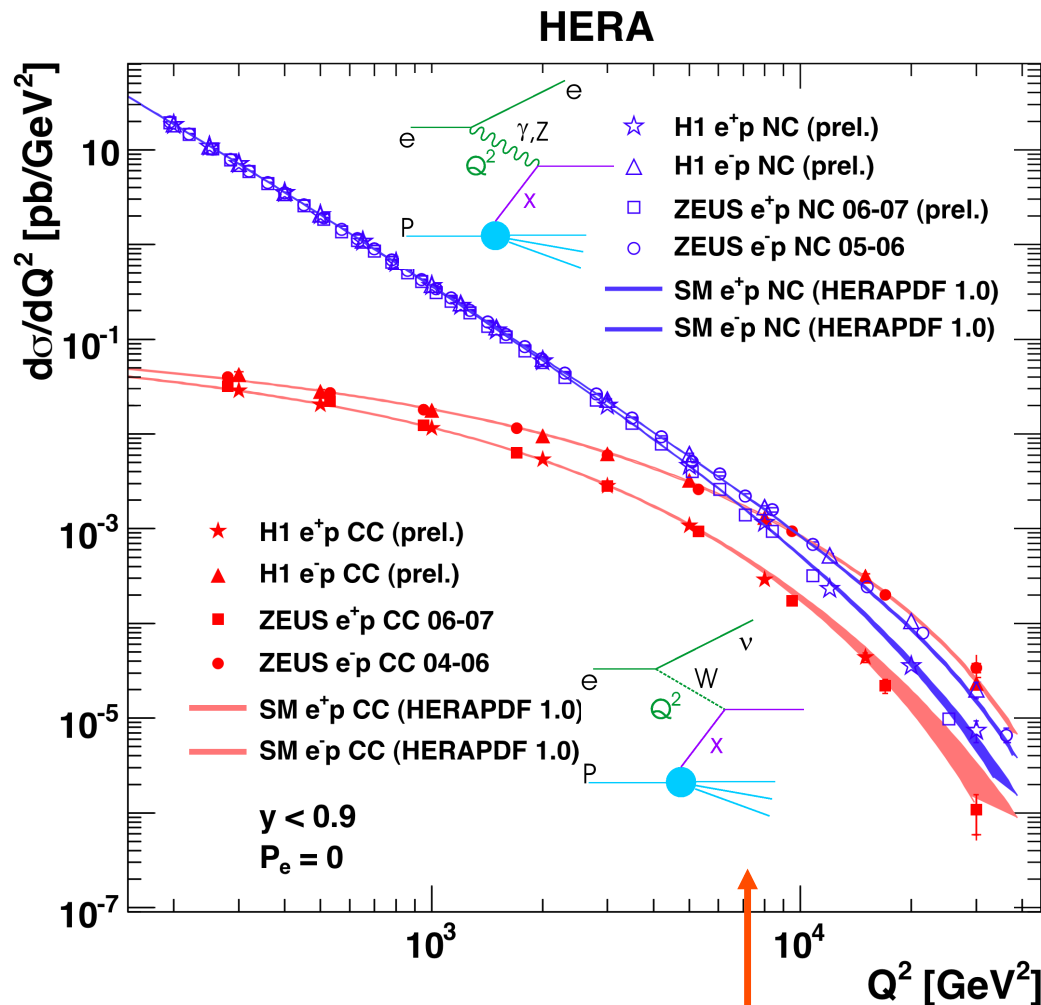
$$\frac{d\sigma^{NC}}{dx dQ^2} \sim \alpha_{em}^2 \cdot \left(\frac{1}{Q^2}\right)^2 \cdot \tilde{\sigma}_{NC}$$

## Charged Current x-sec

$$\frac{d\sigma^{CC}}{dx dQ^2} \sim G_F^2 M_W^2 \cdot \left(\frac{1}{Q^2 + M_W^2}\right)^2 \cdot \tilde{\sigma}_{CC}$$



# Electroweak Unification for Space-like Bosons



$$Q^2 \sim M_W^2, M_Z^2$$

## Neutral Current x-sec

$$\frac{d\sigma^{NC}}{dx dQ^2} \sim \alpha_{em}^2 \cdot \left(\frac{1}{Q^2}\right)^2 \cdot \tilde{\sigma}_{NC}$$

## Charged Current x-sec

$$\frac{d\sigma^{CC}}{dx dQ^2} \sim G_F^2 M_W^2 \cdot \left(\frac{1}{Q^2 + M_W^2}\right)^2 \cdot \tilde{\sigma}_{CC}$$

- NC and CC cross sections become comparable at EW unification scale (couplings unified)

- Parton density info encoded in  $\tilde{\sigma}_{NC}$  and  $\tilde{\sigma}_{CC}$

# Neutral Current Sensitivity to the Quarks

Unpolarised NC cross section depends on 3 structure fns ...

$$\tilde{\sigma}^{NC}(e^{\pm} p) = \boxed{F_2} \mp \frac{Y_-}{Y_+} \boxed{x F_3} - \frac{y^2}{Y_+} \boxed{F_L}$$

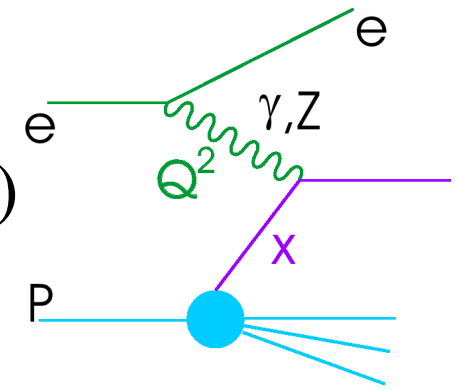
... where  $Y_{\pm} = 1 \pm (1-y)^2$

... and  $y$  measures the process inelasticity

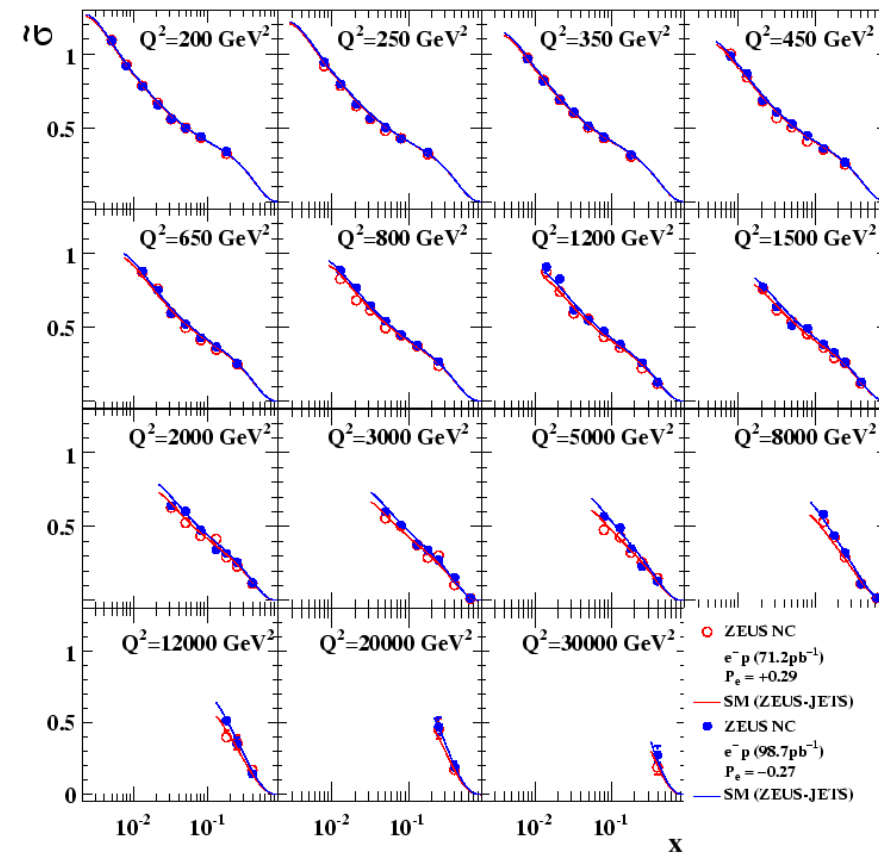
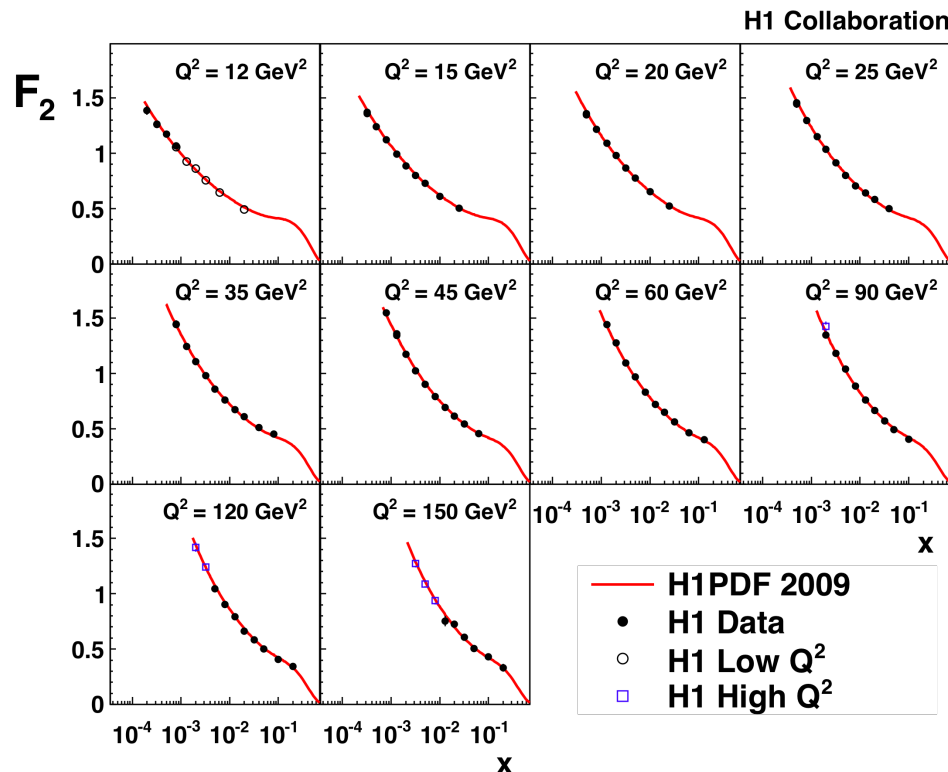
- $F_2$  dominates throughout most of the phase space
- $x F_3$  contributes at high  $Q^2$  (Z exchange) can be obtained from difference between  $e^+p$  and  $e^-p$  cross sections
- $F_L$  contributes at high  $y$  (longitudinally polarised photons)

# Recent Neutral Current Data

- NC data primarily measure  $F_2 = \sum_q e_q^2 x (q + \bar{q})$
- Due to  $e_q^2$  photon coupling, NC Provides best constraints on **u** & **ubar** densities



ZEUS



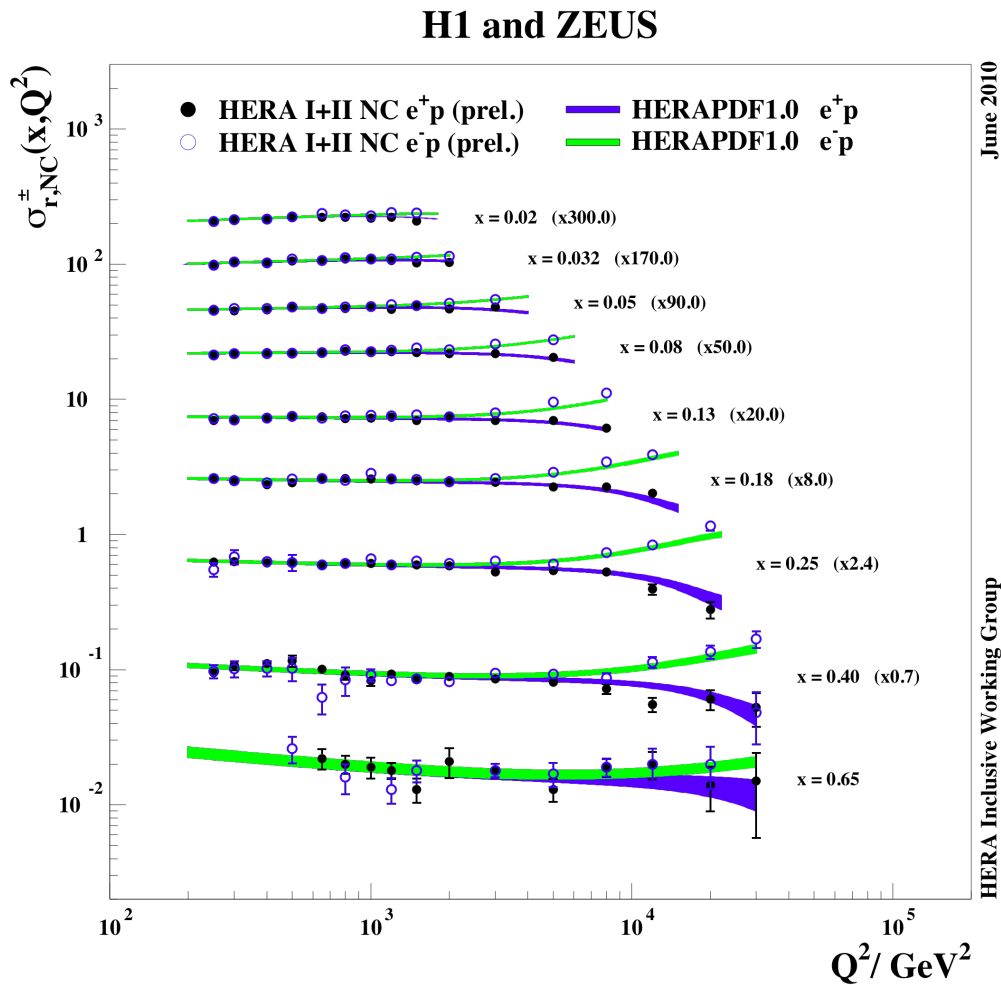
- 1.5-2% precision in final H1 intermediate  $Q^2$  data

- 169pb<sup>-1</sup> (final ZEUS high  $Q^2$  e-p data) ... 2-3% syst precision



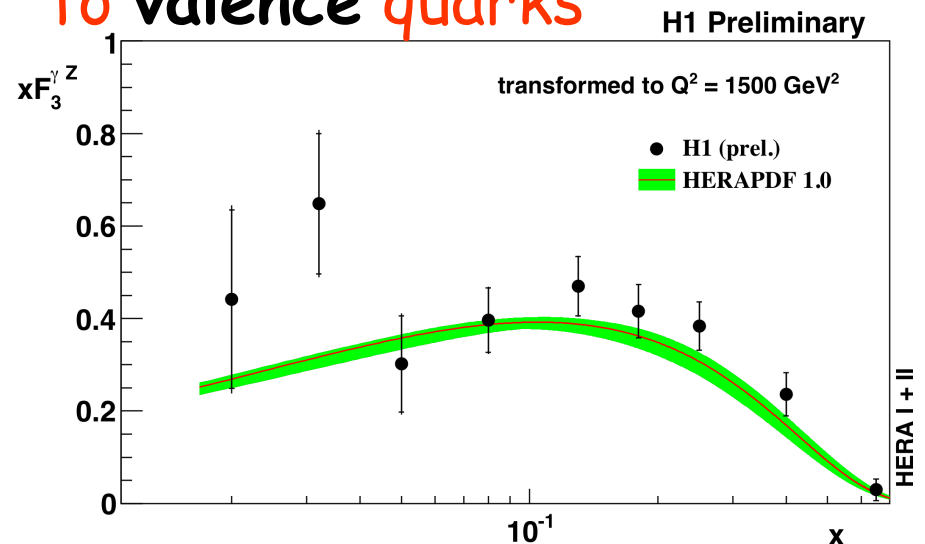
# NC Lepton Charge Dependence & $x F_3$

- Difference between  $e^-p$  and  $e^+p$  NC cross sections at large  $Q^2$  measures  $x F_3$  structure fn...
- Dominated by interference Between  $\gamma$  and  $Z$  exchange
- ... unique sensitivity to valence quarks



$$xF_3 = \frac{Y_+}{2Y_-} (\tilde{\sigma}_{NC}^- - \tilde{\sigma}_{NC}^+)$$

$$\approx \frac{x}{3} (2u_v + d_v)$$

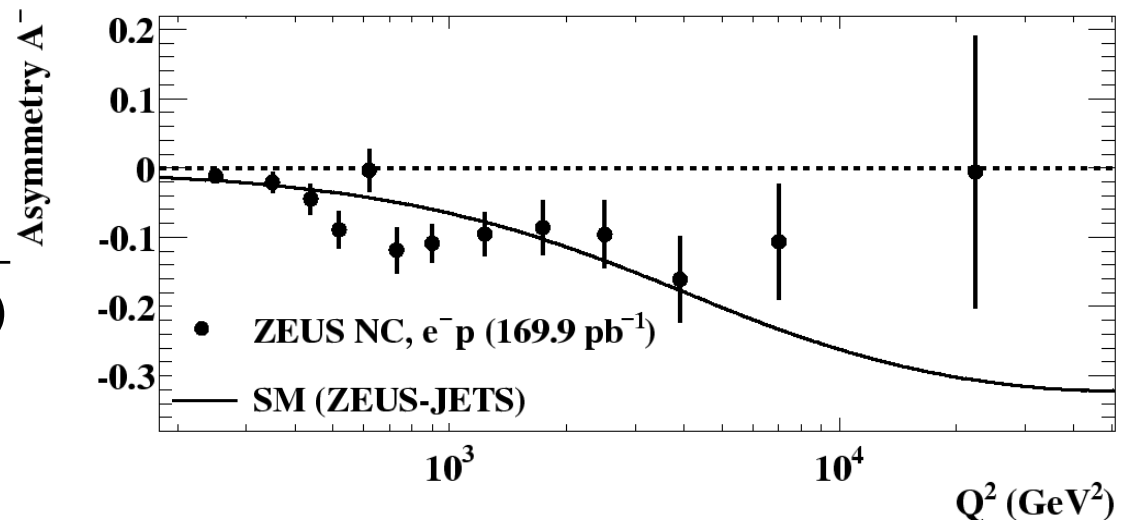
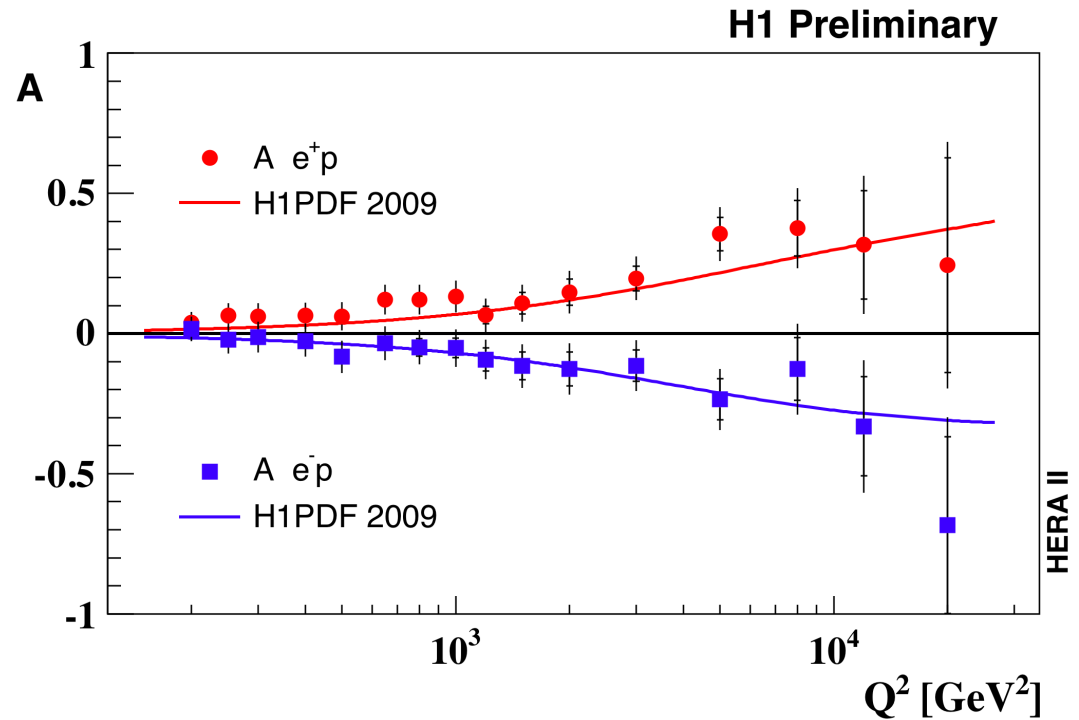


# Left v Right Hand Polarised Leptons

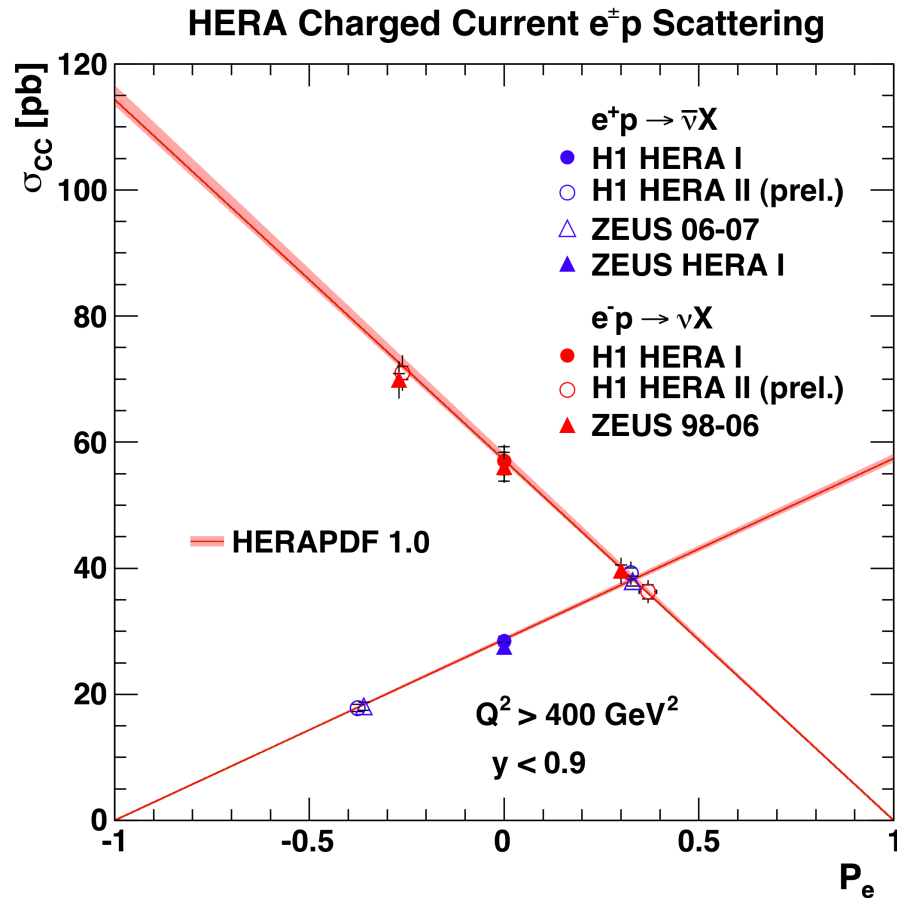
Significant NC  
lepton polarisation  
asymmetry observed  
... tests vector and  
axial EW lepton  
couplings and d/u  
ratio as  $x \rightarrow 1$

$$A = \frac{\tilde{\sigma}_{NC}(R) - \tilde{\sigma}_{NC}(L)}{\tilde{\sigma}_{NC}(R) + \tilde{\sigma}_{NC}(L)}$$

$$\approx \kappa(M_W, M_Z) \frac{(1 + d_v/u_v)}{(4 + d_v/u_v)}$$

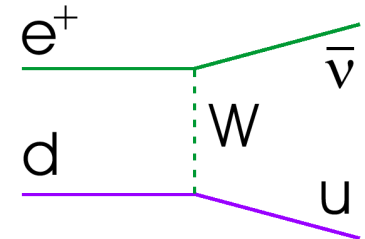
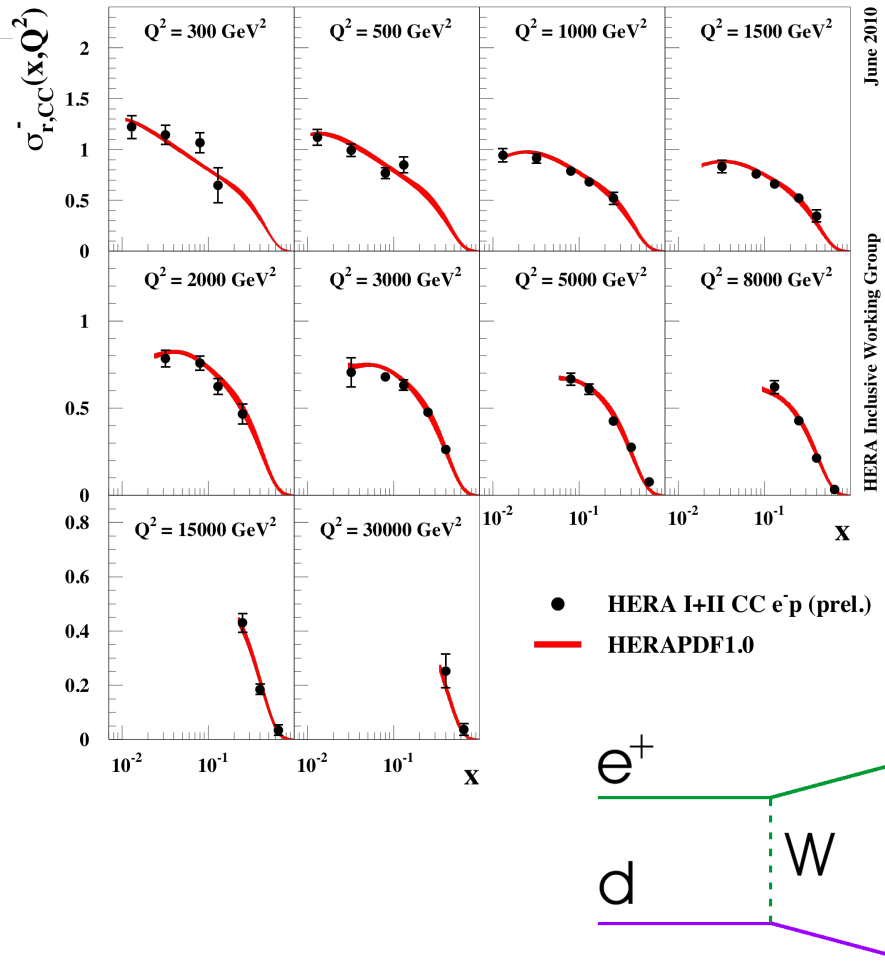


# Recent Charged Current Data



- Linear dependence on polarisation well tested ... **chiral structure of SM**

## H1 and ZEUS

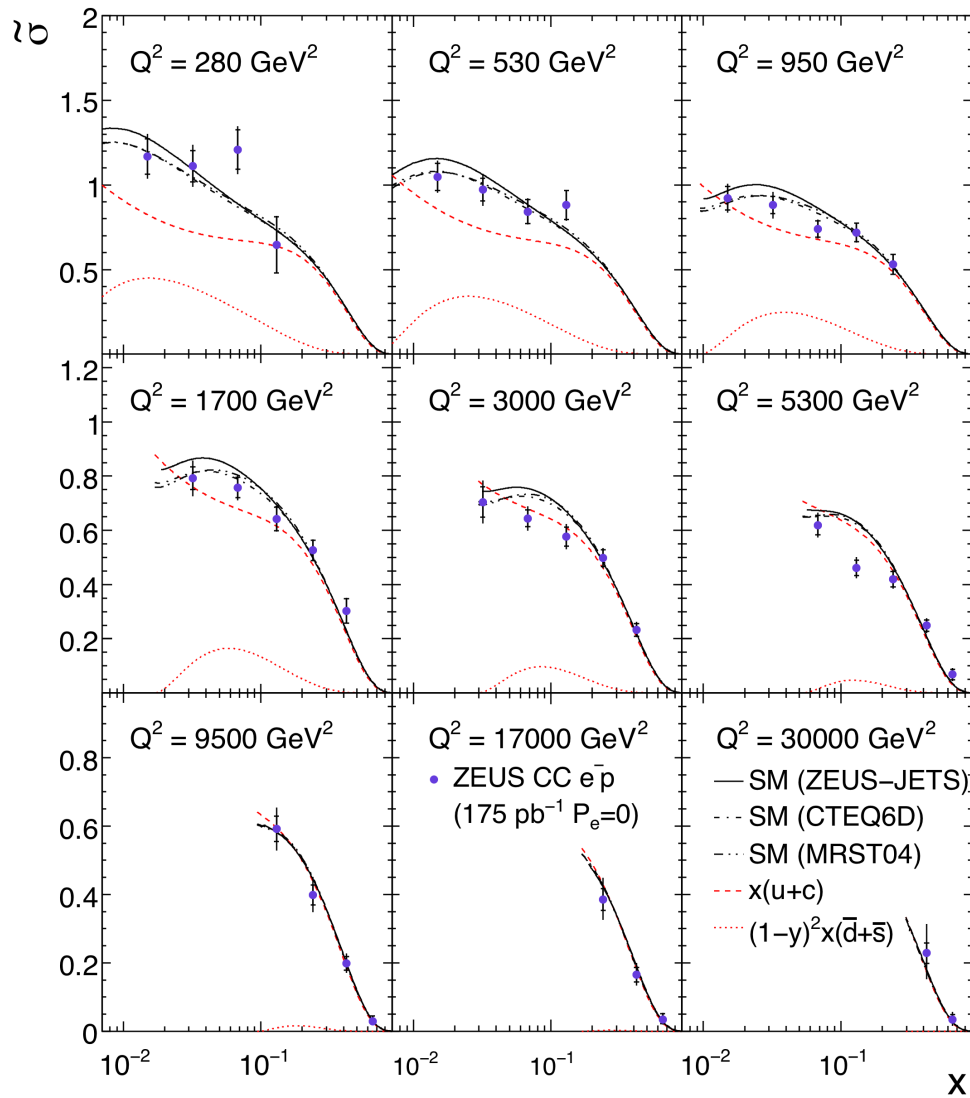


- Charged current sensitive to flavour decomposition ... e.g.  $e^+p$  constrains **d** density



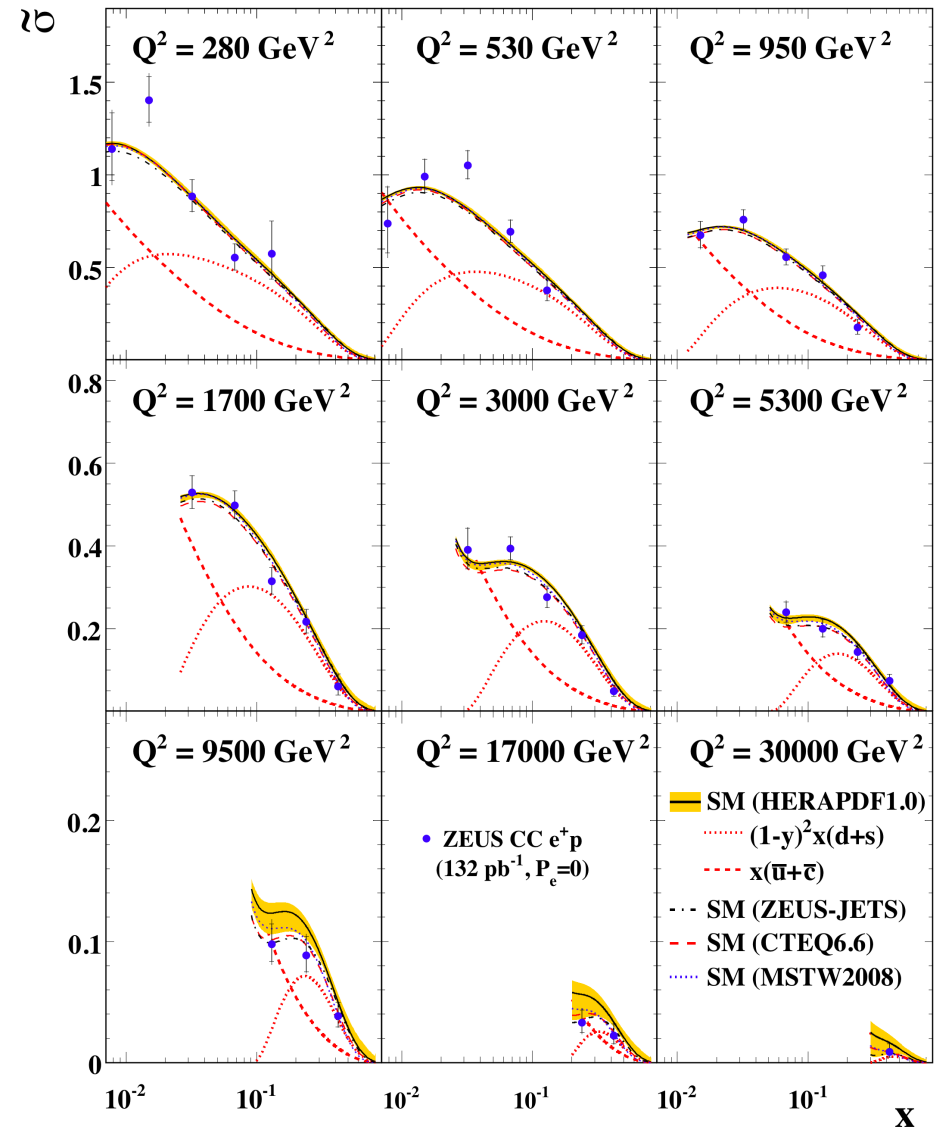
# CC Quark Decomposition

ZEUS



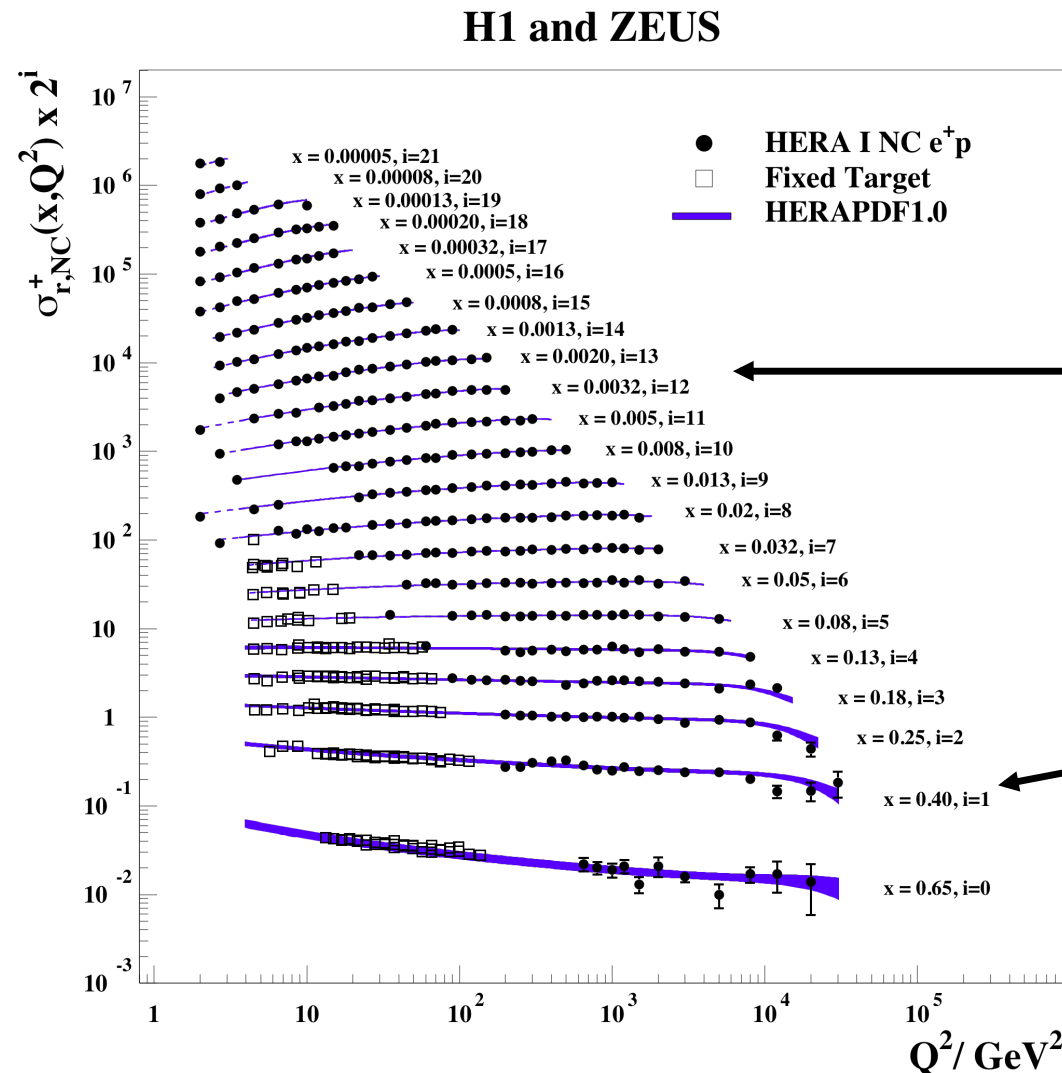
$e^- p$

ZEUS



$e^+ p$

# QCD Evolution and the Gluon Density



• NC  $Q^2$   
dependence  
driven by ...

$g \rightarrow q\bar{q}$

$q \rightarrow qg$

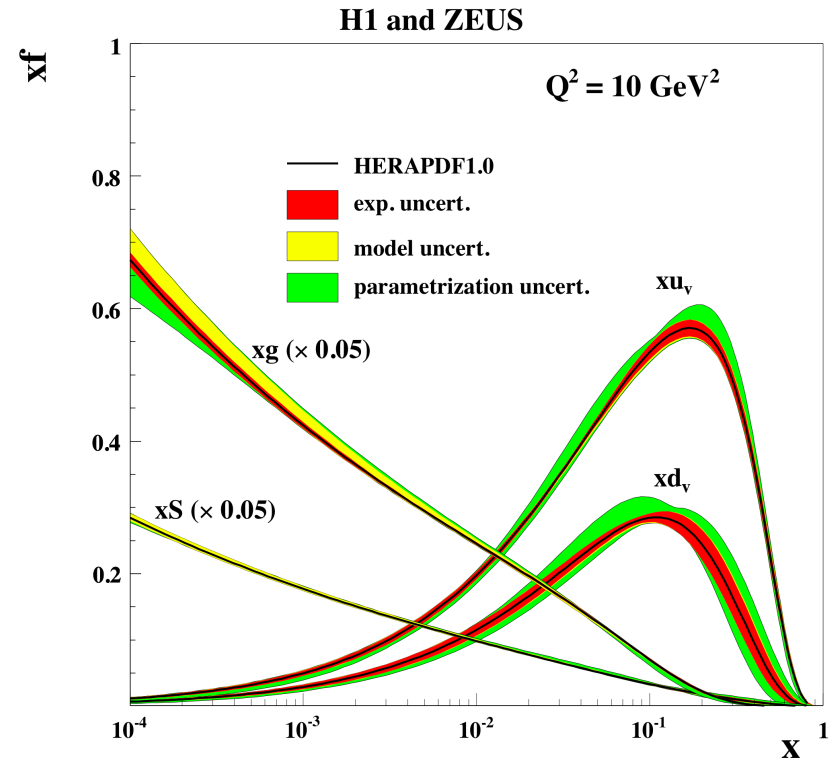
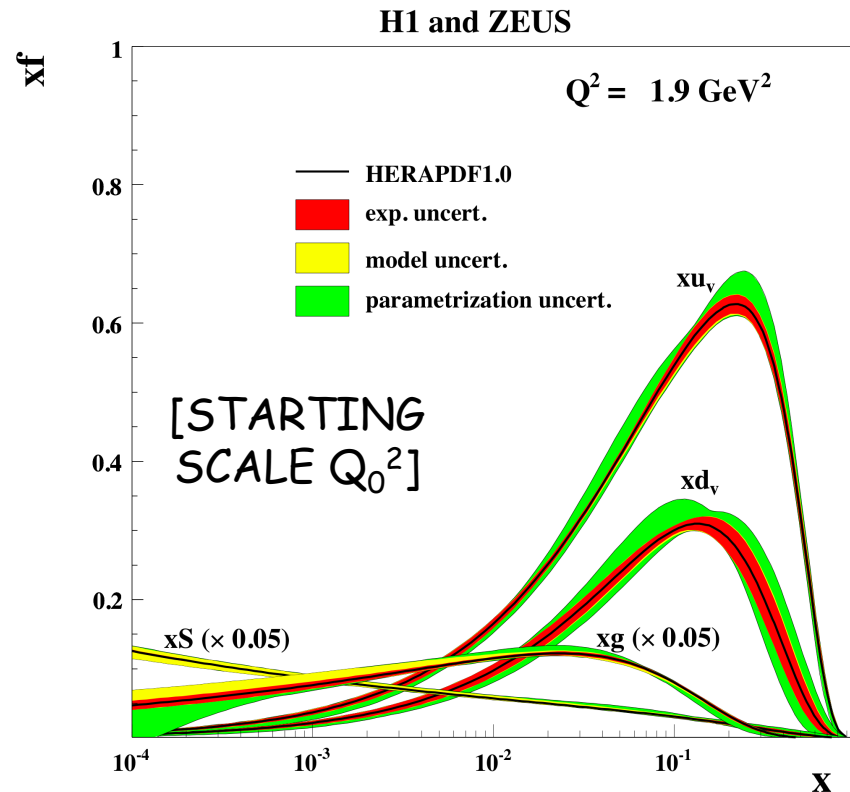
• Excellent QCD fit  
description over  
vast range.

- $Q^2$  evolution of  $F_2$  yields low  $x$  gluon, assuming DGLAP
- Other observables needed @ high  $x$ , where  $g$  sensitivity lost

# Extracting Parton Densities: HERAPDF1.0

- NLO DGLAP fits [to  $O(\alpha_s^2)$ ] performed to combined H1 and ZEUS NC and CC data **using HERA-I data alone**
- Parameterise valence and sea quarks and gluon at starting scale  $Q^2 \sim 2 \text{ GeV}^2$  
$$x f(x) = A x^B (1-x)^C (1 + \varepsilon \sqrt{x} + D x + E x^2)$$
... evolve with DGLAP and fit data  
[Thorne-Roberts GM VFNS heavy flavour scheme]
- Good quality fit:  $\chi^2 / \text{ndf} = 574 / 582$
- Now with full assessment of **uncertainties**:
  - **Experimental**, using  $\Delta\chi^2 = 1$
  - **Model**, by varying  $m_c$ ,  $m_b$ , data  $Q_{\text{min}}^2$ , strangeness frac
  - **Parameterisation**, by forming envelope of results with acceptable variations

# So What is a Proton?



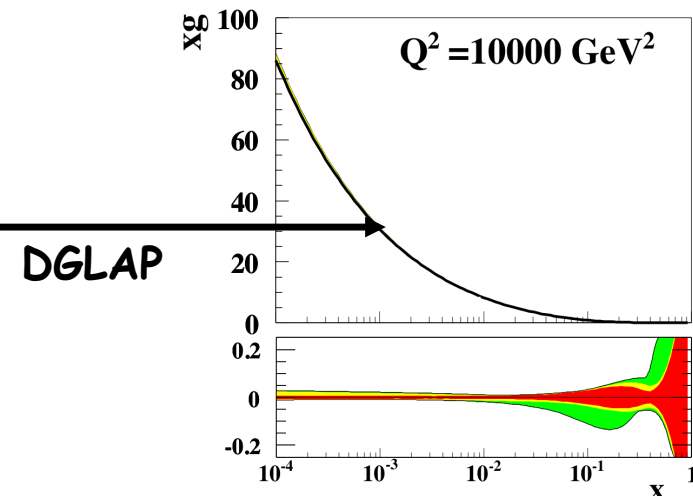
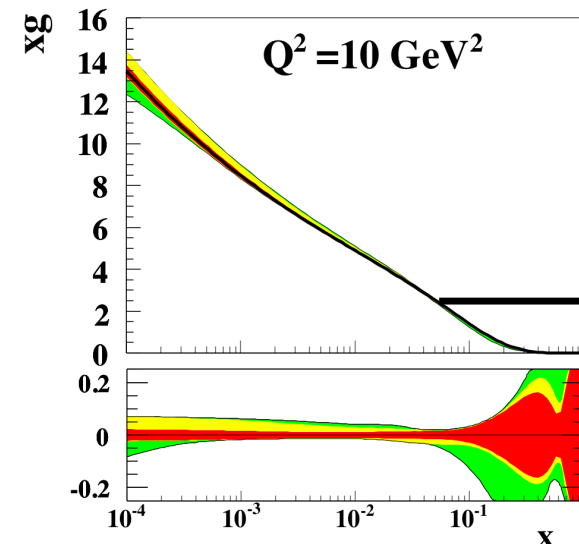
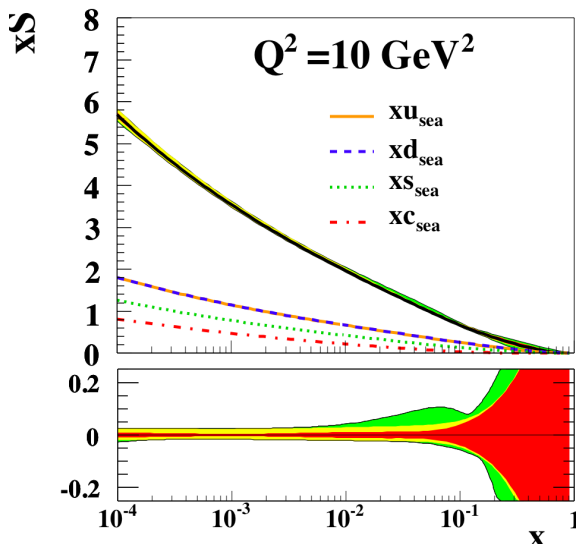
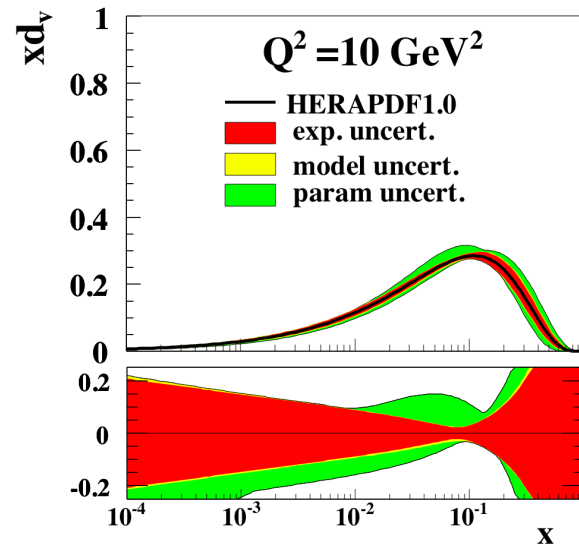
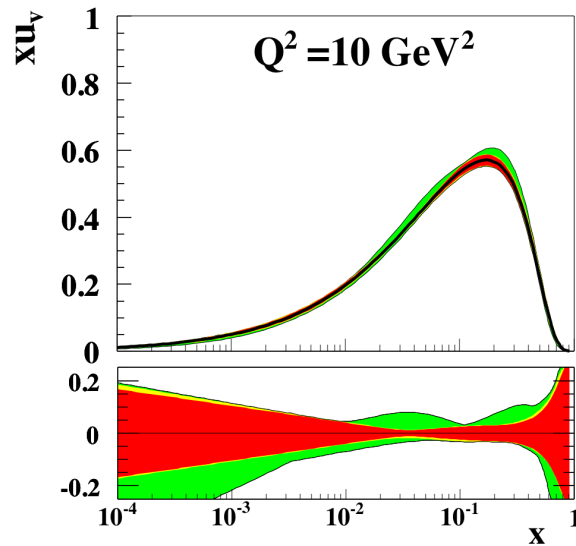
Parameterisation uncertainty dominates

Gluon 'valence-like' at starting scale, evolves to be very large at low x already by  $Q^2 = 10 \text{ GeV}^2$

Broadly consistent with global fits (MSTW, CTeQ, NNPDF)

# A Closer Look at High $x$

H1 and ZEUS



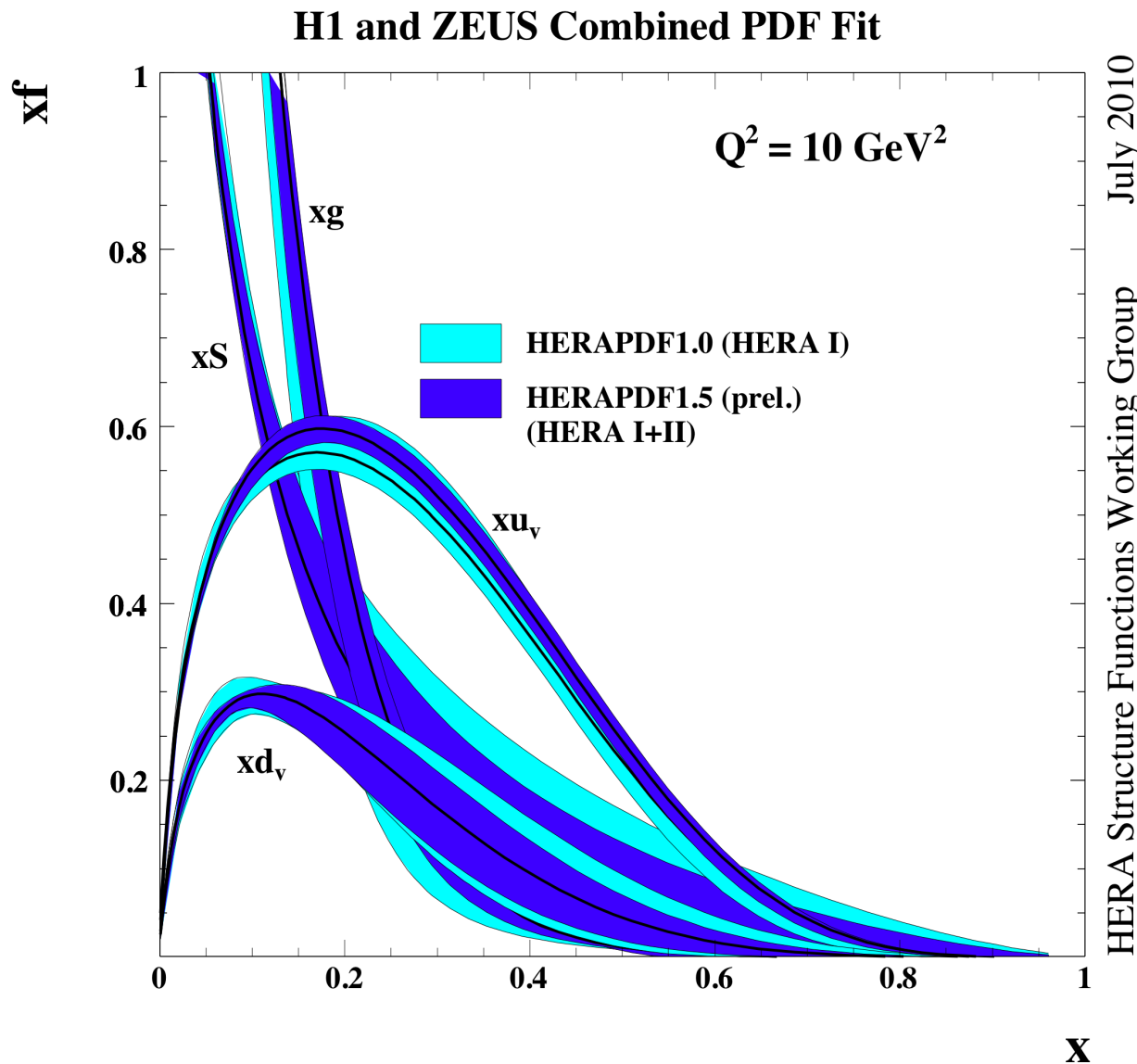
- Errors explode at highest  $x$  (improves with  $Q^2$  evolution)

- Better in global fits (MSTW, CTeQ include pp jets, DY)

- HERA-II data help  
 → HERAPDF1.5

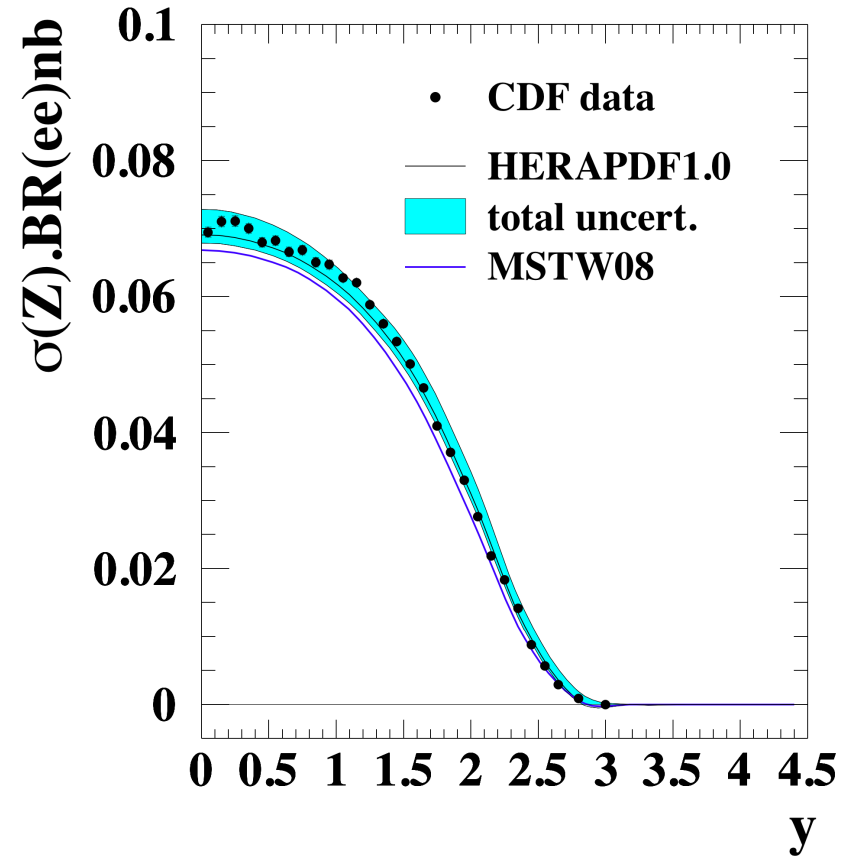
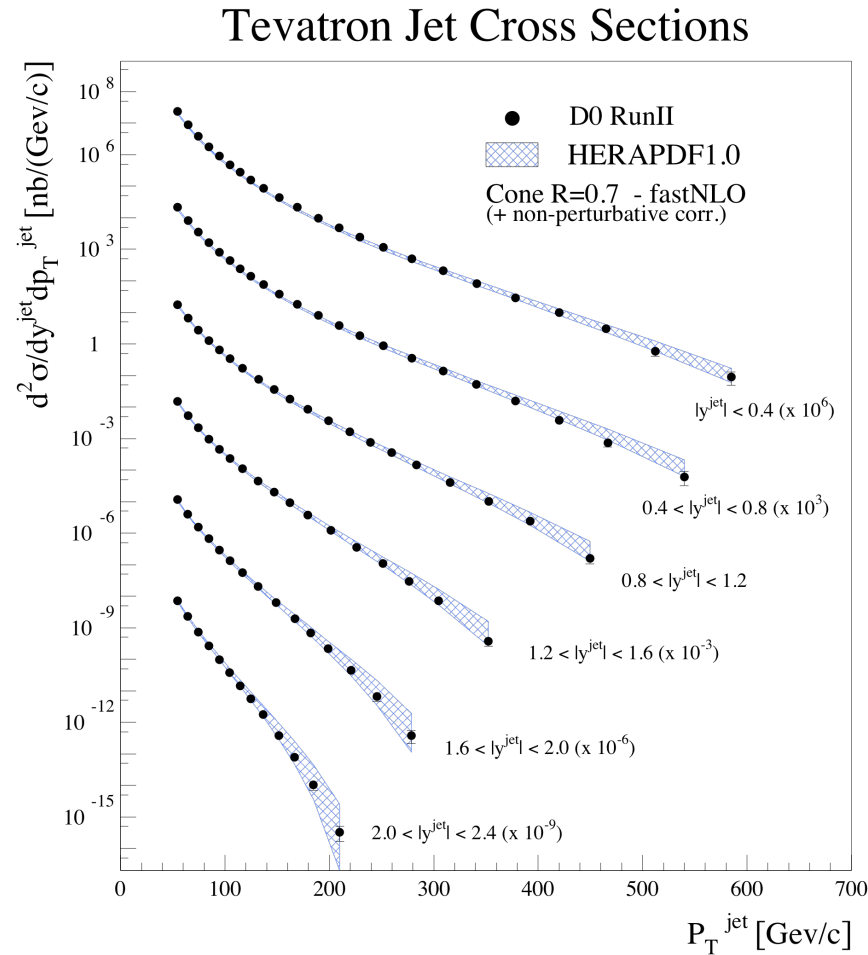


# Including HERA-II Data: HERAPDF 1.5



- Identical procedure to HERA-I case, but with enhanced statistics in high  $x$ , high  $Q^2$  region.
- Experimental and parameterisation uncertainties reduced at high  $x$
- Including low  $E_p$  data also helps (high  $x$ , medium  $Q^2$ )

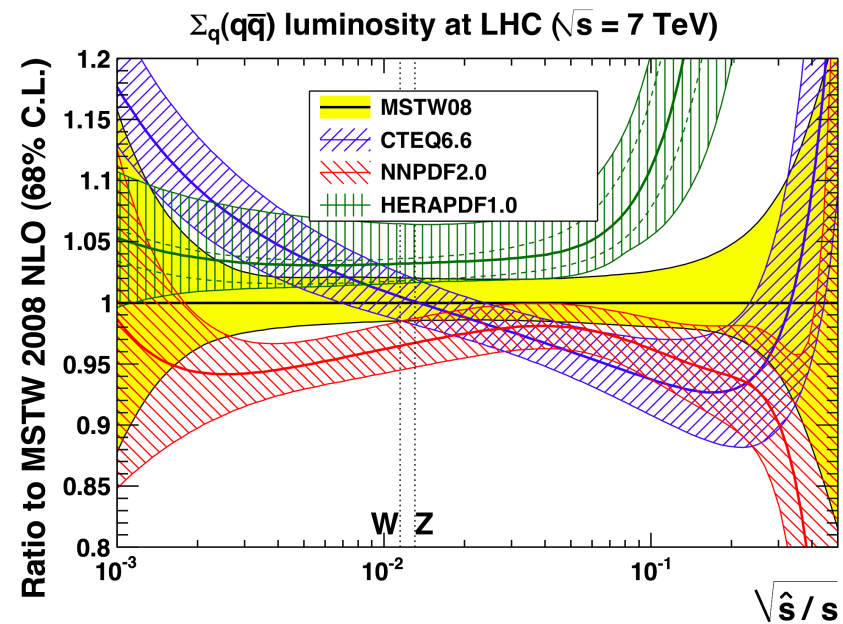
# Comparisons with Tevatron Data



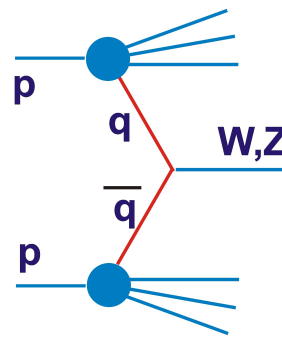
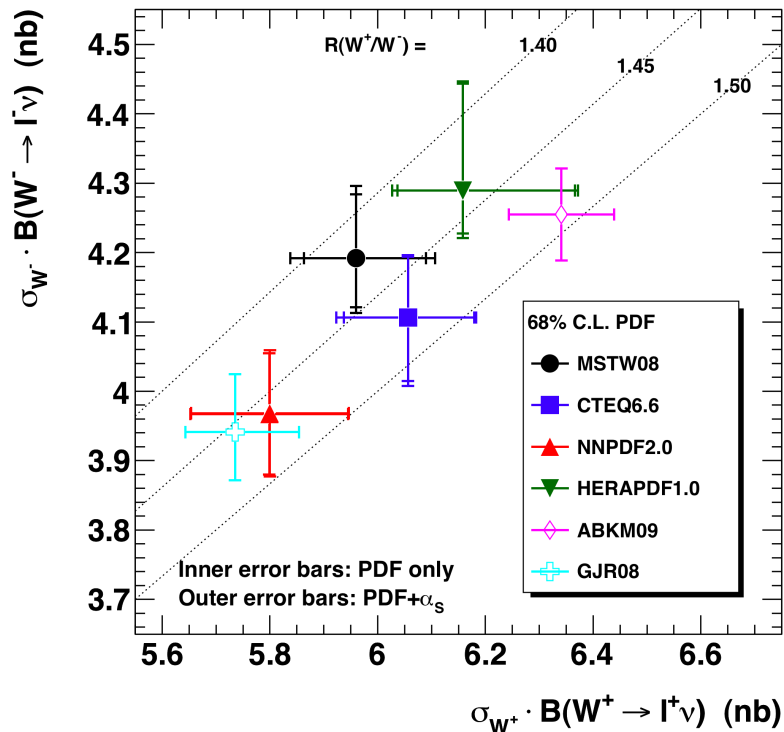
Tevatron observables well described by HERAPDF1.0  
... universal parton densities describe ep and pp  
... the cleanest test of QCD collinear factorisation

# Predictions for LHC: Quark Initiated Processes

~5% uncertainty on  $\sigma(W)$ ,  $\sigma(Z)$   
... is MSTW/CTeQ/NNPDF  
sufficient to define uncertainty?

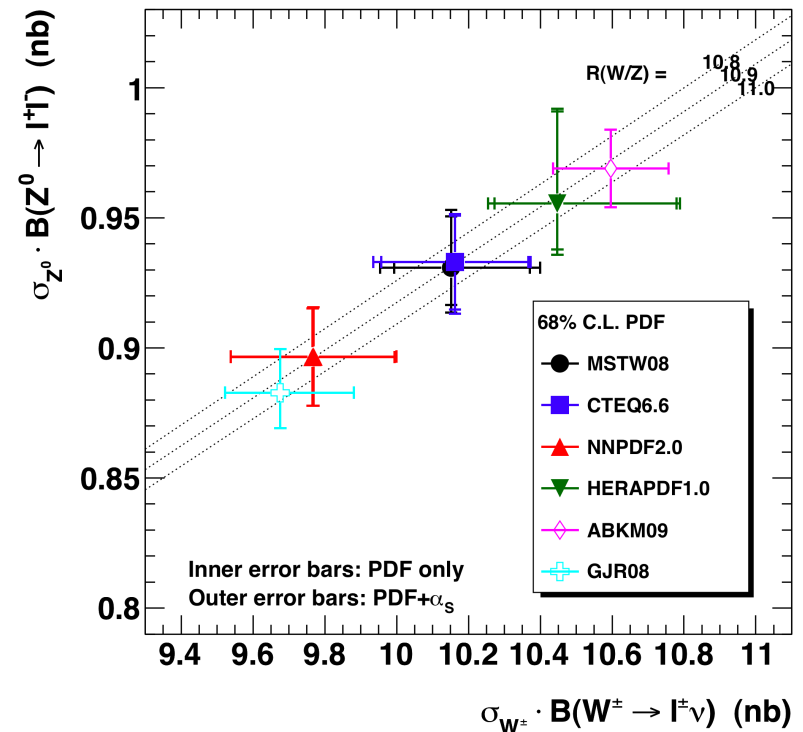


NLO  $W^+$  and  $W^-$  cross sections at the LHC ( $\sqrt{s} = 7$  TeV)



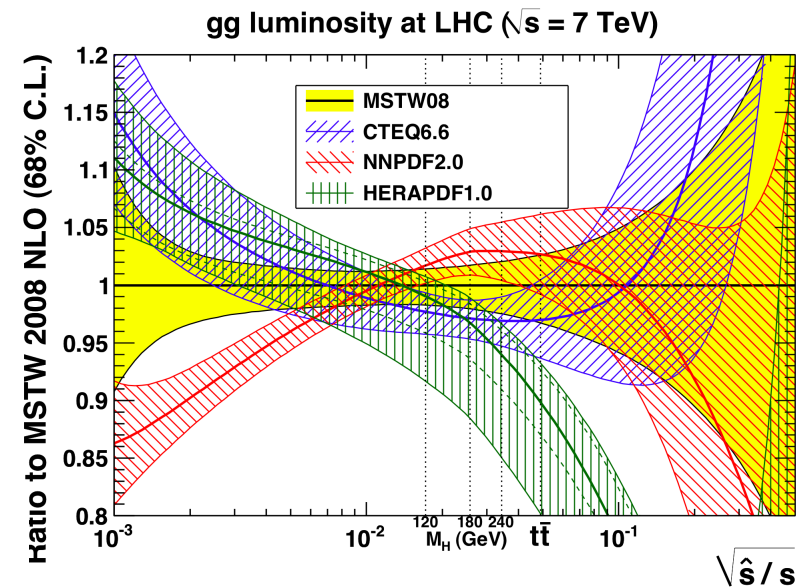
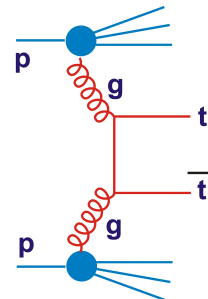
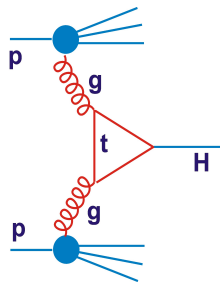
[Plots by  
G. Watt]

NLO W and Z cross sections at the LHC ( $\sqrt{s} = 7$  TeV)



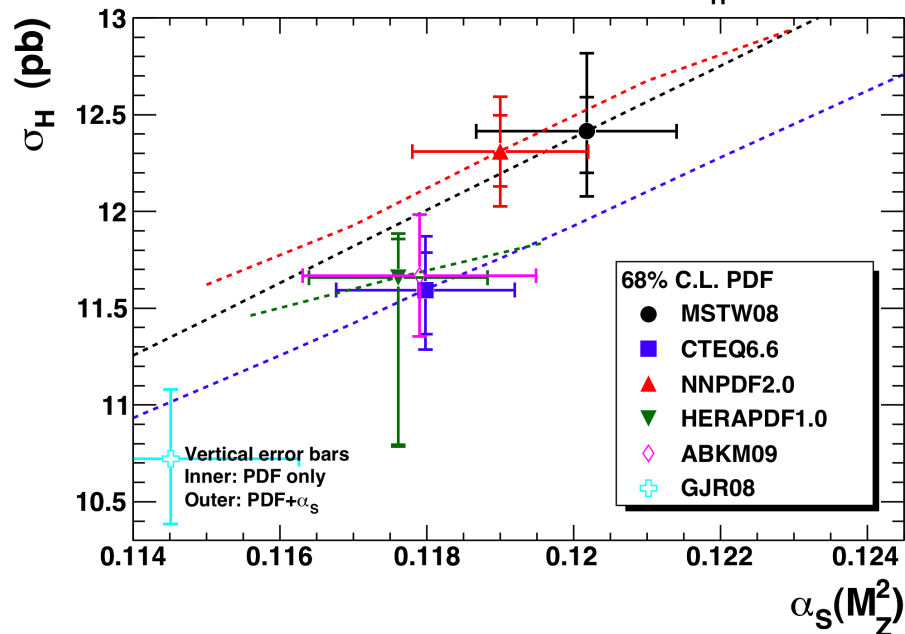
# Predictions for LHC: Gluon Initiated Processes

Top, Higgs cross section  
uncertainties up to 10-15%

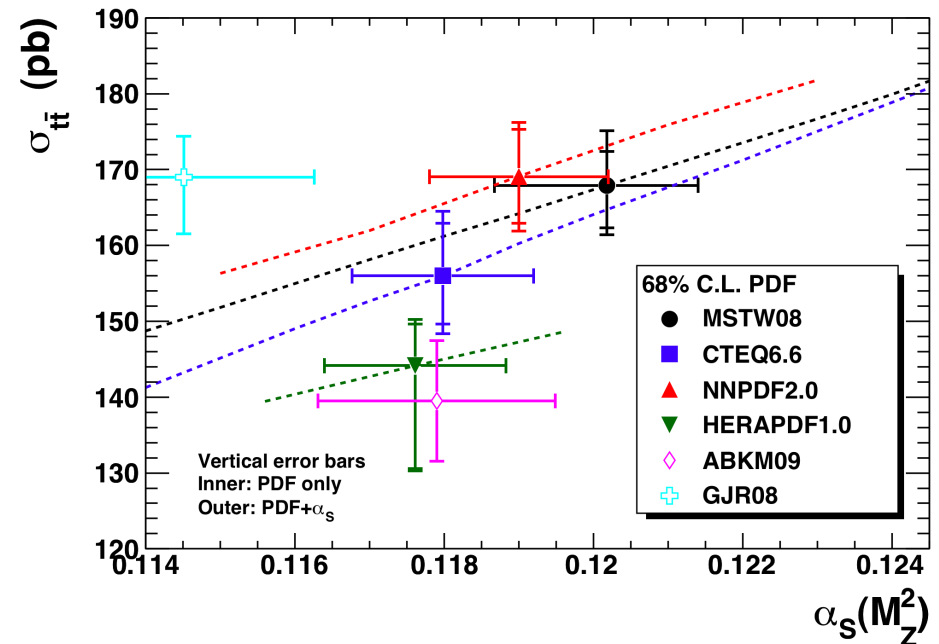


[Plots by G. Watt]

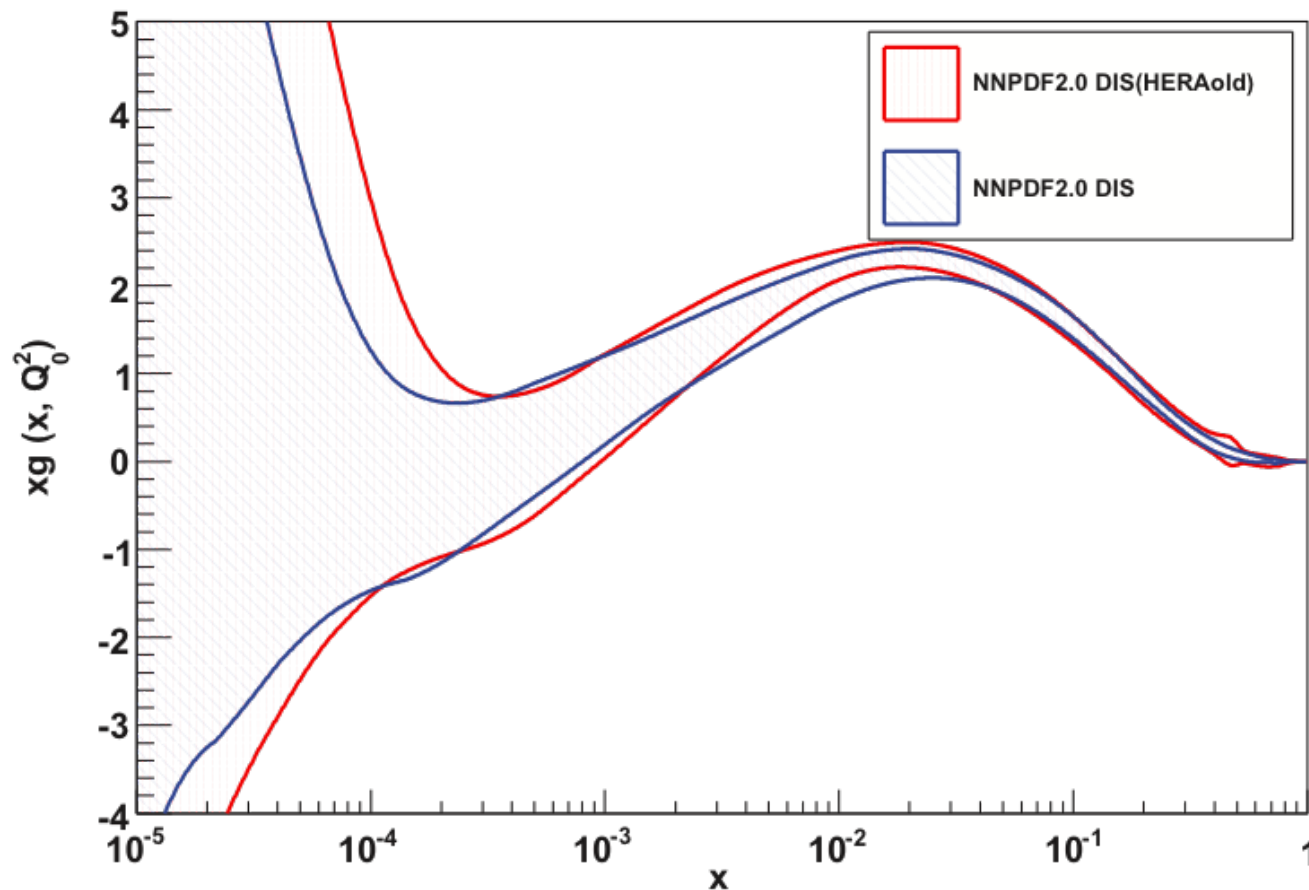
NLO  $gg \rightarrow H$  at the LHC ( $\sqrt{s} = 7$  TeV) for  $M_H = 120$  GeV



NLO  $t\bar{t}$  cross sections at the LHC ( $\sqrt{s} = 7$  TeV)



# How Well do we Know the Low $x$ Gluon?

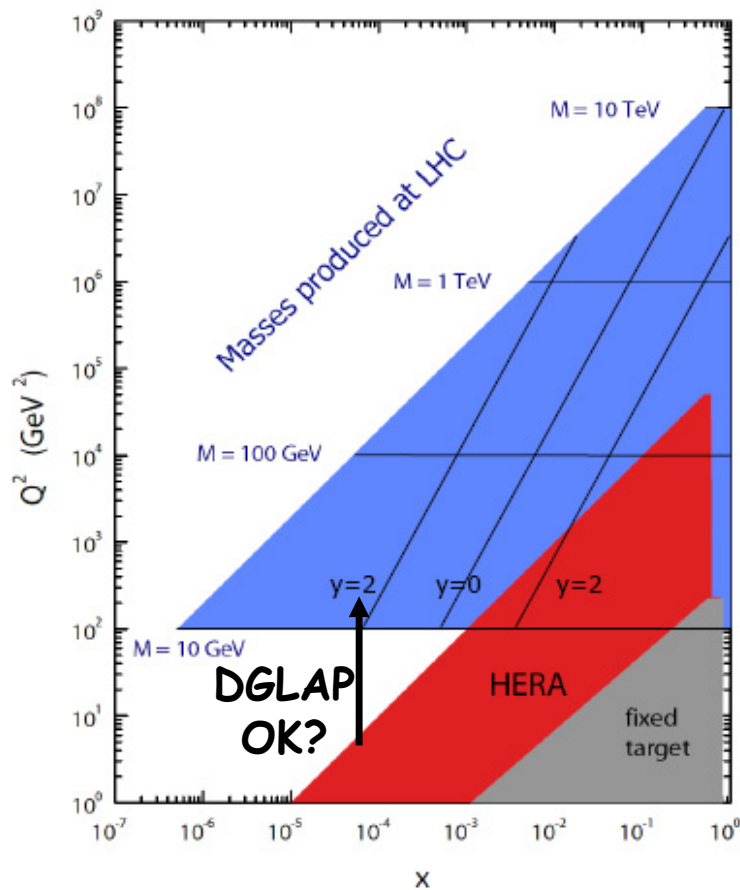


- According to NNPDF, gluon very poorly known for  $x < \sim 10^{-4}$
- Would we notice if there were problems in assumed theory?



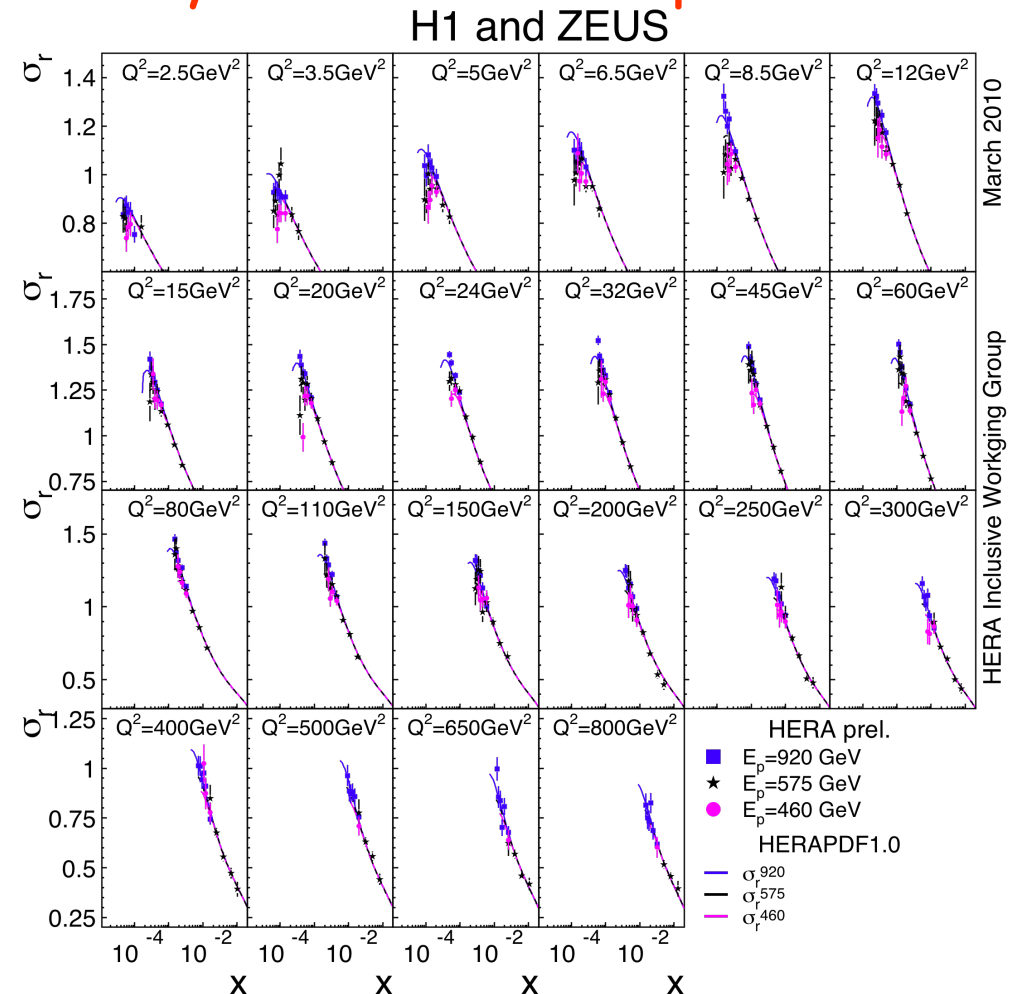
# Are DGLAP Dynamics Sufficient at Low x?

- At low x, LHC predictions rely on assumption of DGLAP evolution ... yet many novel effects predicted ...



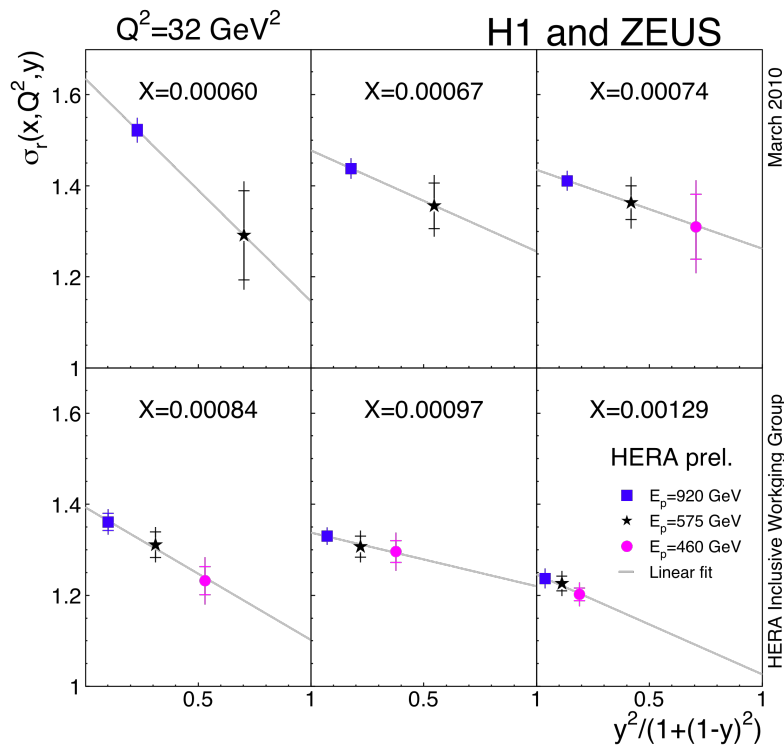
Test overall picture with  $F_L$  extracted using reduced proton beam energy data.

Where gluon dominates,  $F_L \sim \alpha_s xg(x)$ .



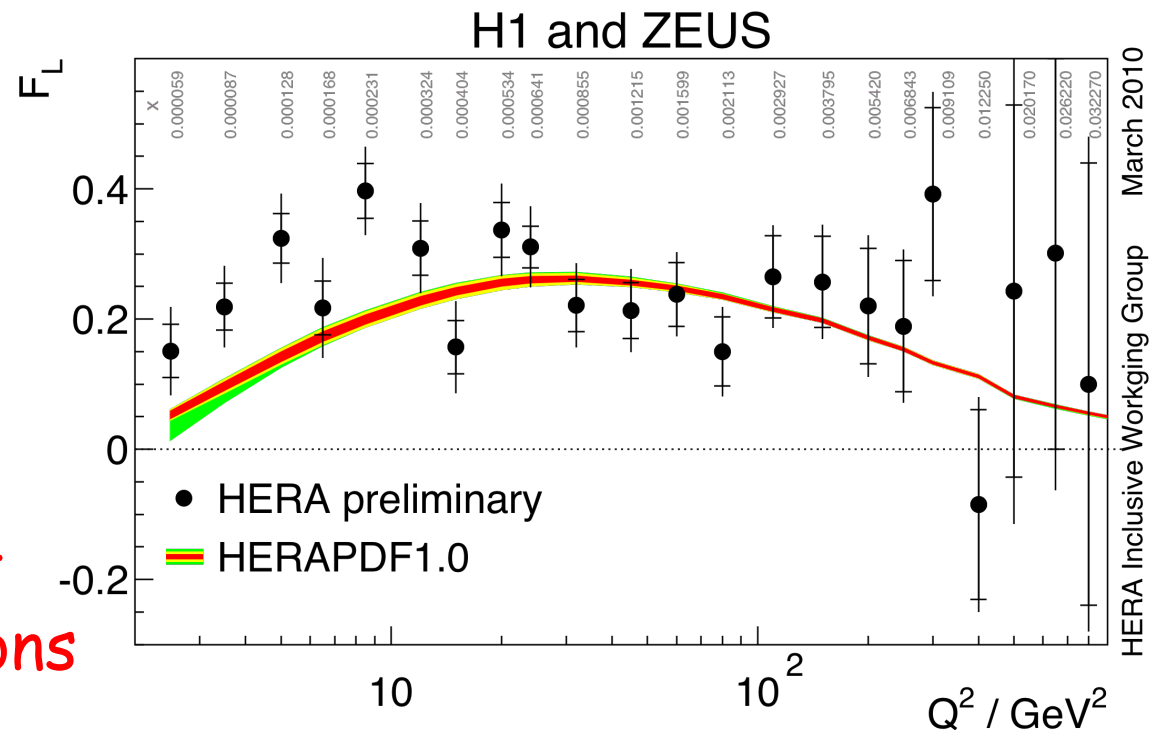
# Combined H1 + ZEUS $F_L$ Measurement

Extracted double differentially  
... Summary of  $Q^2$  dependence here

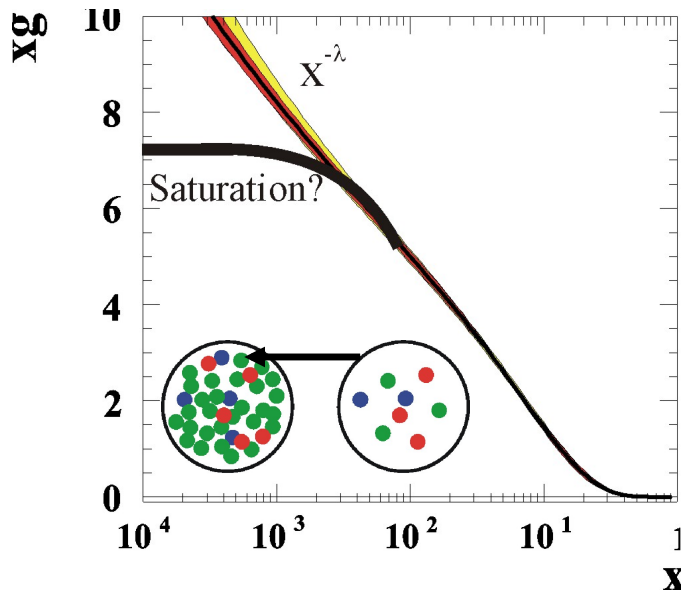


$$\sigma_r = F_2 - \frac{y^2}{Y_+} F_L$$

Basically good agreement  
With HERAPDF predictions

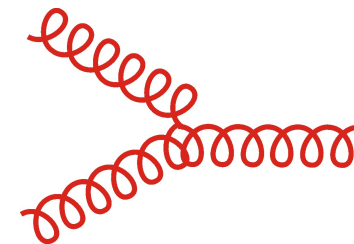
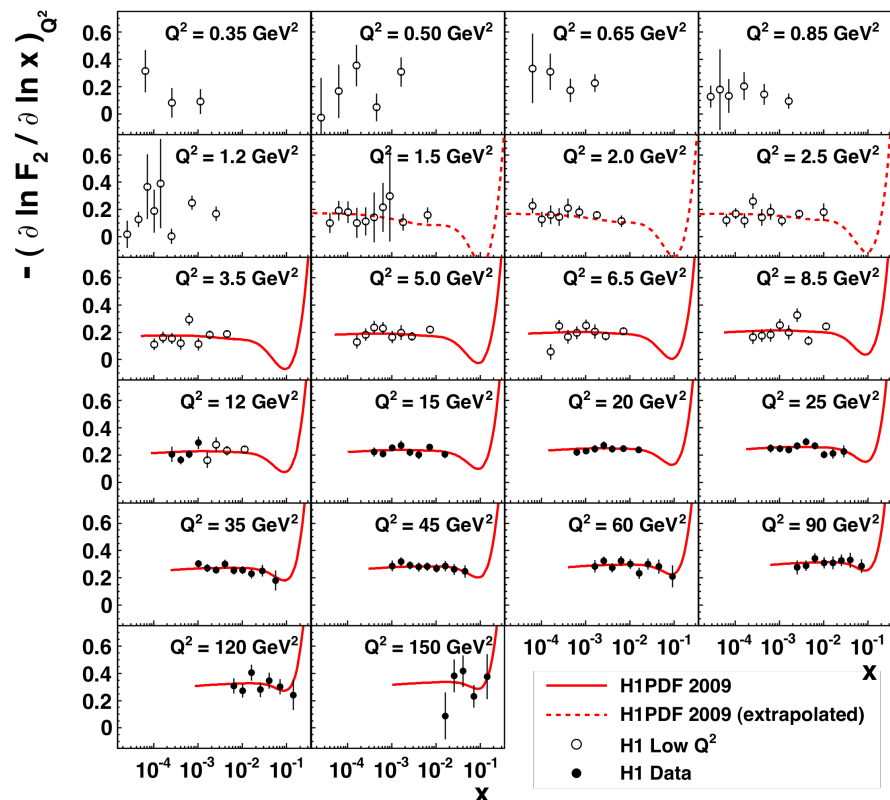


Hints of deviations at low  $x$ ,  $Q^2$  may be resolved with  
modified heavy flavour treatment or inclusion of NNLO terms?



# Search for Gluon Saturation

- Gluon density cannot rise indefinitely as  $x$  decreases (unitarity)
- DGLAP approximation to QCD may be insufficient e.g. due to neglect of  $gg \rightarrow g$  recombination



from local derivatives  
with respect to  $x$  ...  
... no evidence for any  
deviation from a single power  
law  $F_2 = A(Q^2) \cdot x^{-\lambda(Q^2)}$   
for  $Q^2 > \sim 1 \text{ GeV}^2$

# Summary

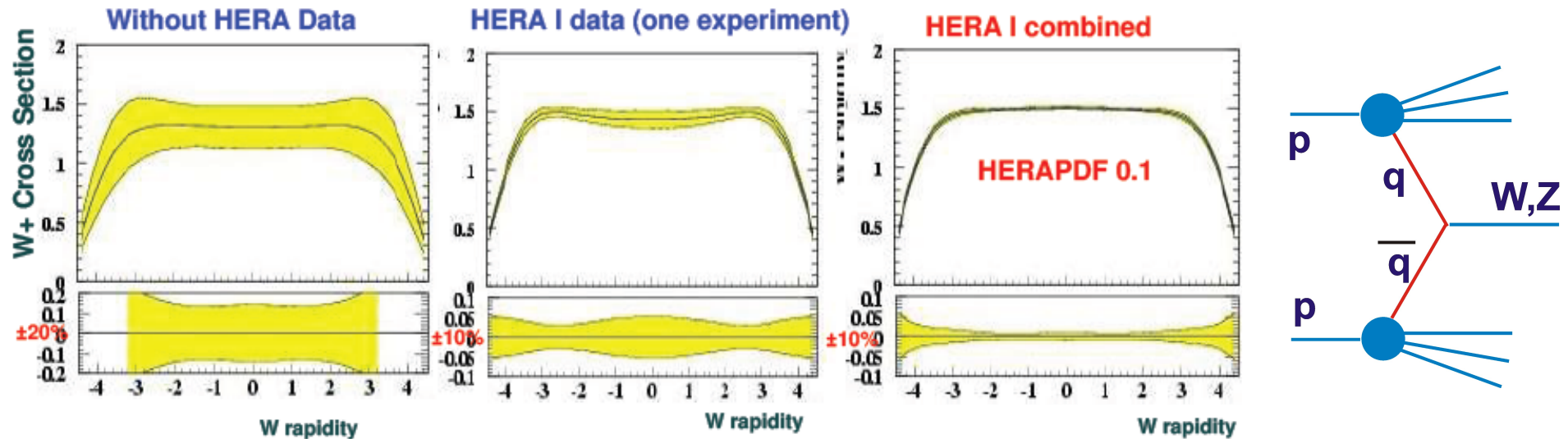
- After 15 years of running, HERA provided a unique data-set
- ~450 publications to date:
  - The main source of our knowledge of the LHC initial state
  - Big advances in understanding QCD
  - Dedicated low  $x$  dynamics studies
- Combinations of H1 and ZEUS data and fits proves powerful in reducing errors
  - HERAPDF1.0 gives competitive precision for many LHC observables without tension between datasets
  - Final HERA-II data to be included



Back-Ups Follow



# Examples of Precision on LHC Cross Sections

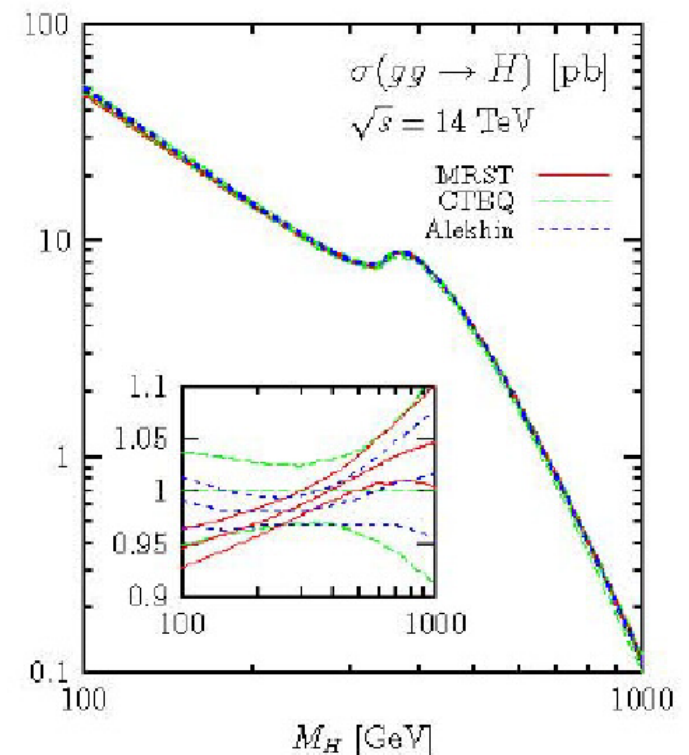
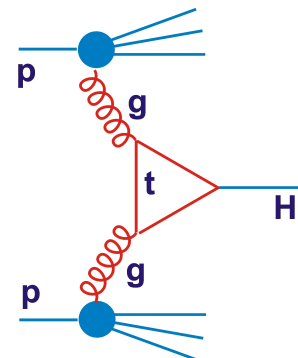


## $W$ Rapidity Spectra:

- 1.5% experimental error in central region (... from HERA-I only!)
- ... a further 3-4% theory uncertainty
- $Z/W$  ratio  $< 2\%$  total uncertainty ...

## Higgs cross section:

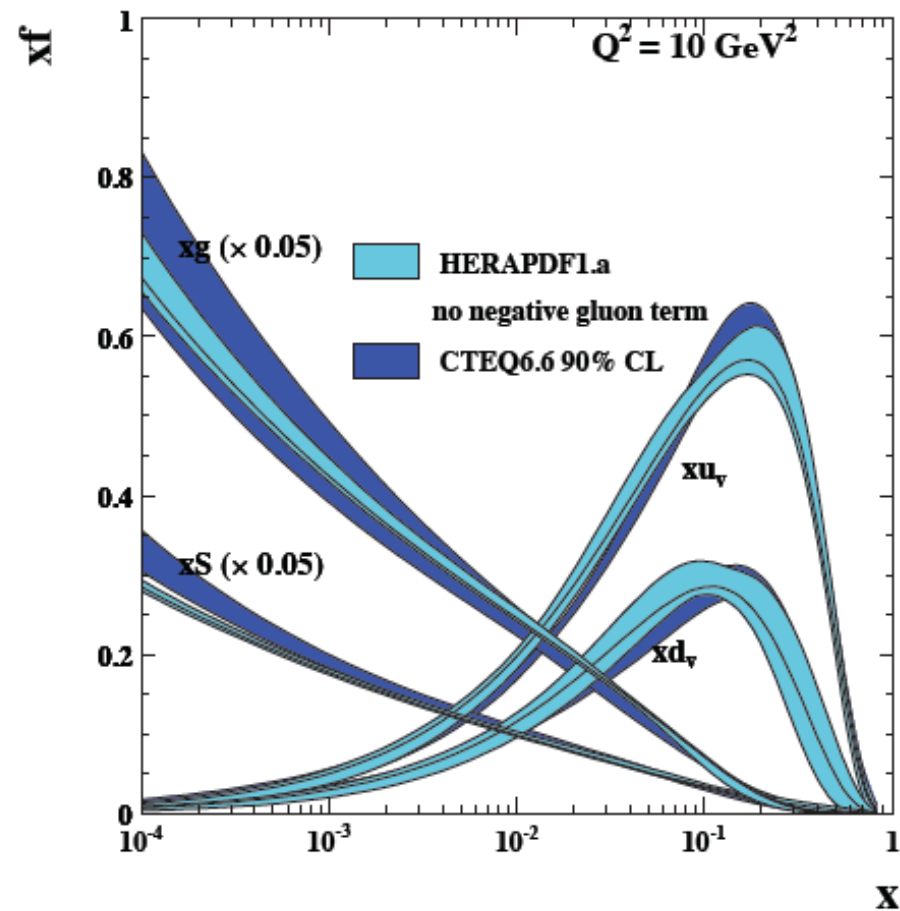
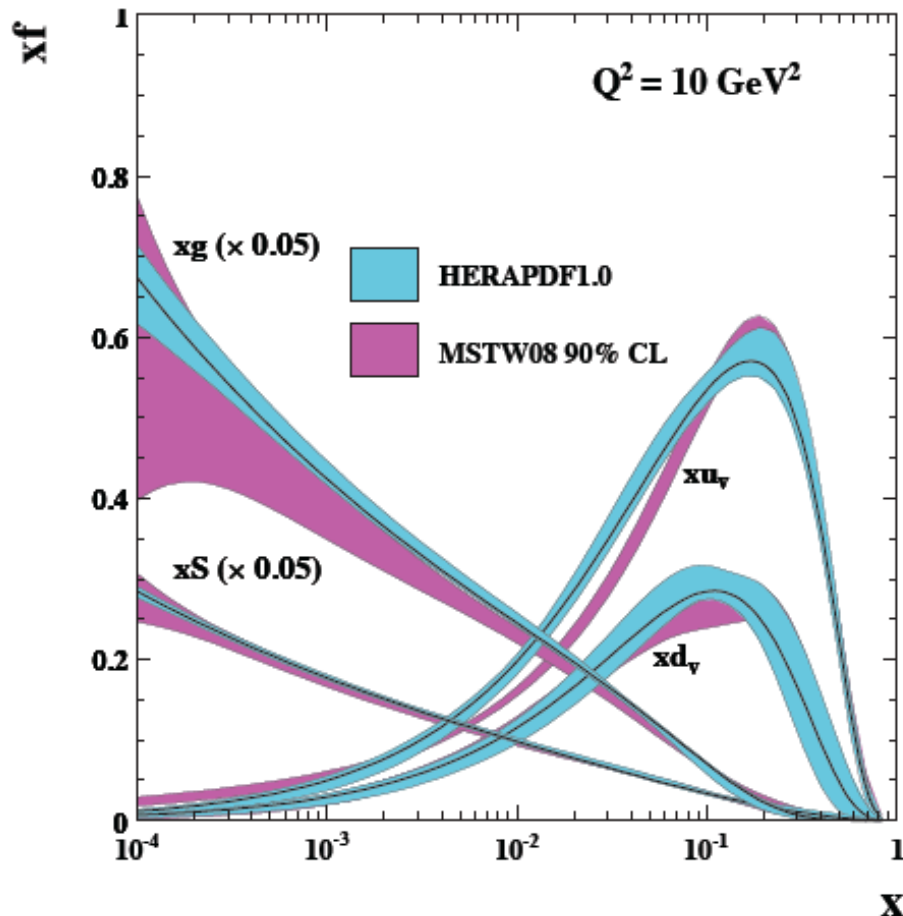
- PDF uncertainty  $\sim 3\%$
- Scale uncertainty  $\sim 10\%$





# Comparisons with Global PDF Sets

## Comparison with other PDFs

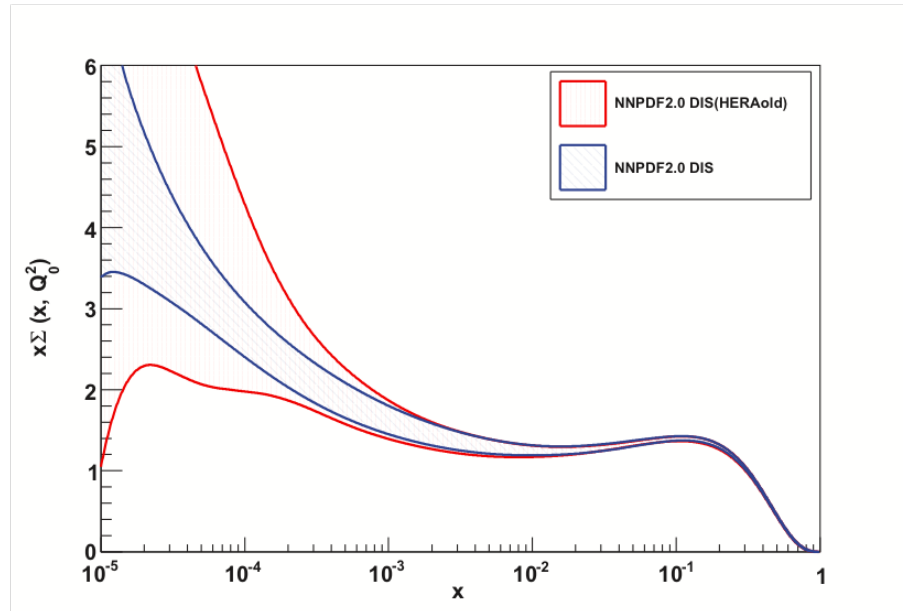
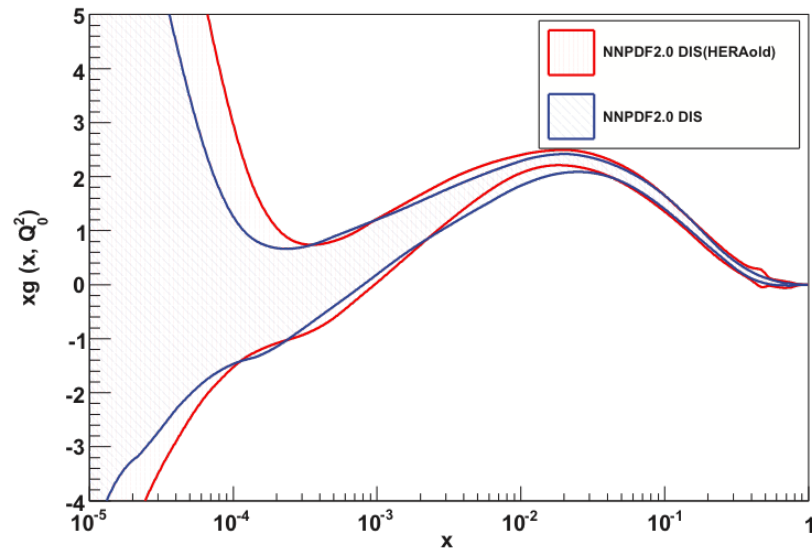


Comparison with other PDFs not trivial :

- HERAPDF uses combined data and MSTW (CTEQ) did not
- Different error treatment, model assumptions
- Consider all when making a measurement

See also  
Voica - NNLO  
Version!!!!<sup>22</sup>

# Precision on the Low $x$ Sea and Gluon



Relative uncertainties from parameter  
Free NNPDF fit.

Gluon essentially unknown for  $x < 10^{-4}$

Looks completely different from CTEQ

