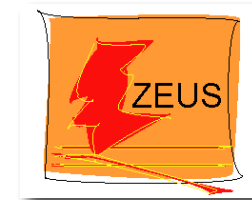


Combined Measurements and PDF fits including HERA-II high Q^2 data



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on behalf of H1 and ZEUS Collaboration



3rd of June, 2011

Outline

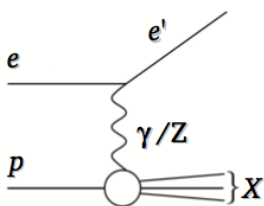
- HERA Experimental Settings
- H1 and ZEUS Data Combination
- HERA PDF analysis framework
- Results and Comparisons
- Summary



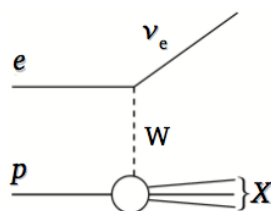
HERA at DESY

- HERA was world's only $e^\pm p$ collider
 - located at DESY, Hamburg - Germany
 - In operation for 15 years (1992-2007)
 - H1 and ZEUS collider experiments
 - General purpose detectors
 - $\sim 1\text{fb}^{-1}$ of integrated luminosity of physics data.
- HERA provides unique opportunity to study the structure of proton via DIS processes:

NC: $e p \rightarrow e' X$



CC: $e p \rightarrow \nu_e X$



○ Kinematic variables:

○ Virtuality of exchanged boson:

$$Q^2 = -q^2 = -(k - k')^2$$

○ Bjorken scaling variable:

$$x = \frac{Q^2}{2p \cdot q}$$

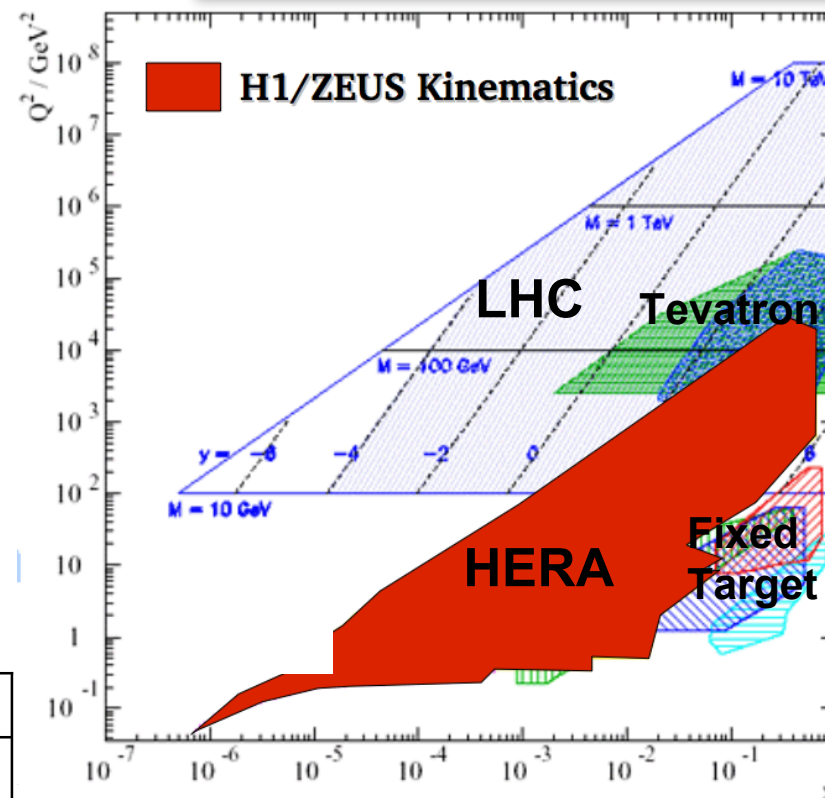
○ Inelasticity:

$$y = \frac{p \cdot q}{p \cdot k}$$

○ Invariant centre of mass:

$$s = (k + p)^2 = \frac{Q^2}{xy}$$

HERA-I	1992-2000	$E_p=820,920 \text{ GeV}$	$L \sim 110/\text{pb per exp.}$
HERA-II	2003-2007	$E_p=920, 460,575 \text{ GeV}$	$L \sim 500/\text{pb per exp.}$



Deep Inelastic Scattering at HERA

Neutral Current:

$$Y_{\pm} = 1 \pm (1 - y^2)$$

$$\sigma_r(x, Q^2) = \frac{d^2\sigma(e^{\pm}p)}{dx dQ^2} \frac{Q^4 x}{2\pi\alpha^2 Y_{\pm}} = F_2(x, Q^2) - \frac{y^2}{Y_{\pm}} F_L(x, Q^2) \mp \frac{Y_{\mp}}{Y_{\pm}} x F_3(x, Q^2)$$

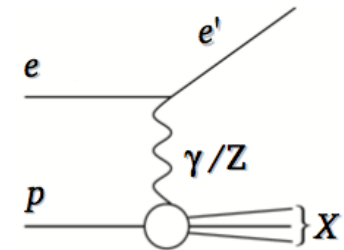
- $x F_3$ only sensitive at large Q^2 ($\sim M_Z^2$)
- F_L only sensitive at low Q^2 and high y
- F_2 dominates

$$x F_3 \sim \sum (x q_i - x \bar{q}_i)$$

$$F_L \sim \alpha_S g$$

$$F_2 \sim \sum e_i^2 (x q_i + x \bar{q}_i)$$

NC: $e p \rightarrow e' X$

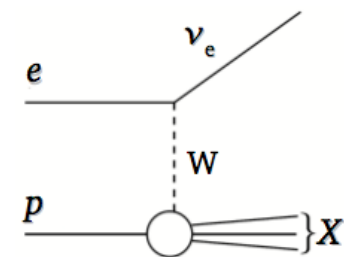


Charged Current: provides important flavour decomposition

$$\text{e-p: } \frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) \left[\textcolor{blue}{u} + c + (1-y)^2 (\bar{d} + \bar{s}) \right]$$

$$\text{e+p: } \frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right) \left[\bar{u} + \bar{c} + (1-y)^2 (\textcolor{red}{d} + s) \right]$$

CC: $e p \rightarrow \nu_e X$



Input Data from HERA into the HERAPDF fits

- Combined HERA I inclusive data

[JHEP01(2010)109]

- HERAPDF1.0 NLO (full errors) and NNLO
- Data used in NNPDF2.0(I), CT10, ABKM

- Combined HERA I+high Q^2 HERA II Data [prelim]:

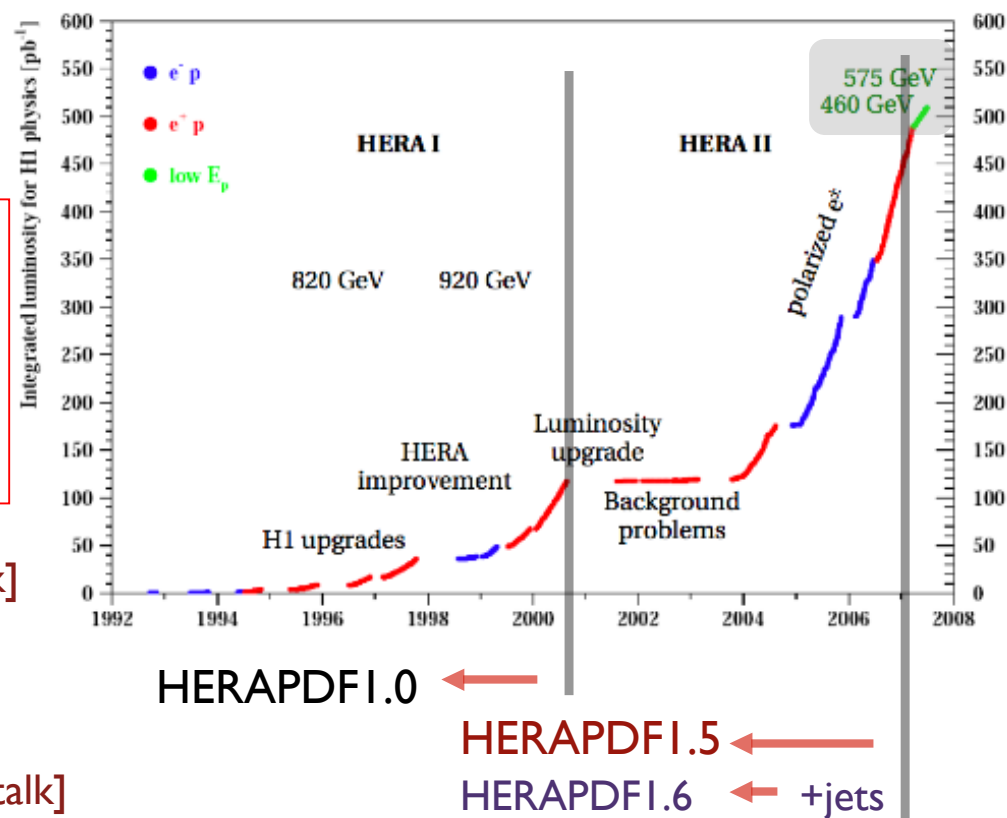
- Accurate measurements in high Q^2 region
 - Sensitivity to valence quarks
- HERAPDF1.5, HERAPDF1.5f (full errors)
 - NLO (full errors)
 - NNLO (full errors)**

- HI and ZEUS DIS Jet data [See A. Cooper's talk]

- HERAPDF1.6 NLO (full errors)
- Determination of strong coupling**

- Combined Charm F_2 data [prelim] [See P. Roloff's talk]

- Provides constraints on charm mass
- Accounts for some differences among various PDF sets



- Low Energy Data HERA II [EPJ(2011)71]:

[See A. Petrukhin's talk]

- Accurate measurement in $Q^2 \geq 1.5 \text{ GeV}^2$ range, sensitive to structure function F_L :
 - Investigate the low Q^2 region;
 - Test sensitivity to different heavy flavour treatments

Combination of the H1 and ZEUS Measurements

- Ultimate precision is obtained by combining the H1 and ZEUS measurements.
- The combination procedure is performed before QCD analysis:
 - Based on χ^2 minimisation procedure allowing systematic error sources free in the fit
 - Improvement on Statistical precision:
 - ◆ H1 and ZEUS collected similar amounts of physics data.
 - Improvement of Systematic precision:
 - ◆ H1 and ZEUS have different detectors and use different analysis techniques;
 - ◆ H1 and ZEUS have different sensitivities to similar sources of correlated systematic unc.

⇒ Combination of HERA I data was published in [\[JHEP01 \(2010\) 109\]](#) ⇒ [HERAPDF1.0](#)

- Preliminary High Q^2 HERA II data included in combination on top of HERA I data.

ZEUS CC e^-p	175 pb ⁻¹	EPJ C 61 (2009) 223-235
ZEUS CC e^+p	132 pb ⁻¹	EPJ C 70 (2010) 945-963
ZEUS NC e^-p	170 pb ⁻¹	EPJ C 62 (2009) 625-658
H1 CC e^-p	149 pb ⁻¹	H1prelim-09-043
H1 CC e^+p	180 pb ⁻¹	H1prelim-09-043
H1 NC e^-p	149 pb ⁻¹	H1prelim-09-042
H1 NC e^+p	180 pb ⁻¹	H1prelim-09-042

- $\chi^2/\text{dof}=967/1032$
- 131 systematic uncertainties and 3 additional procedural

⇒ [HERAPDF1.5](#)

ZEUS NC e^+p	135 pb ⁻¹	ZEUS-prel-11-003
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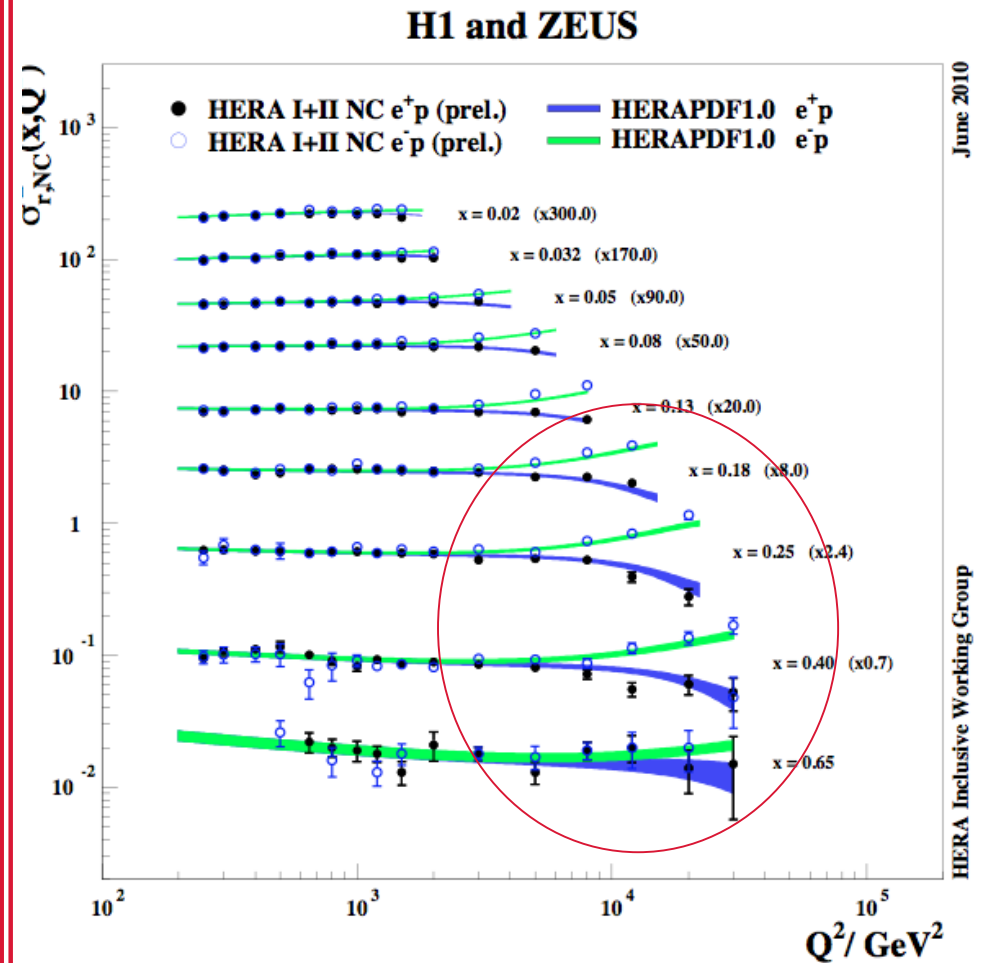
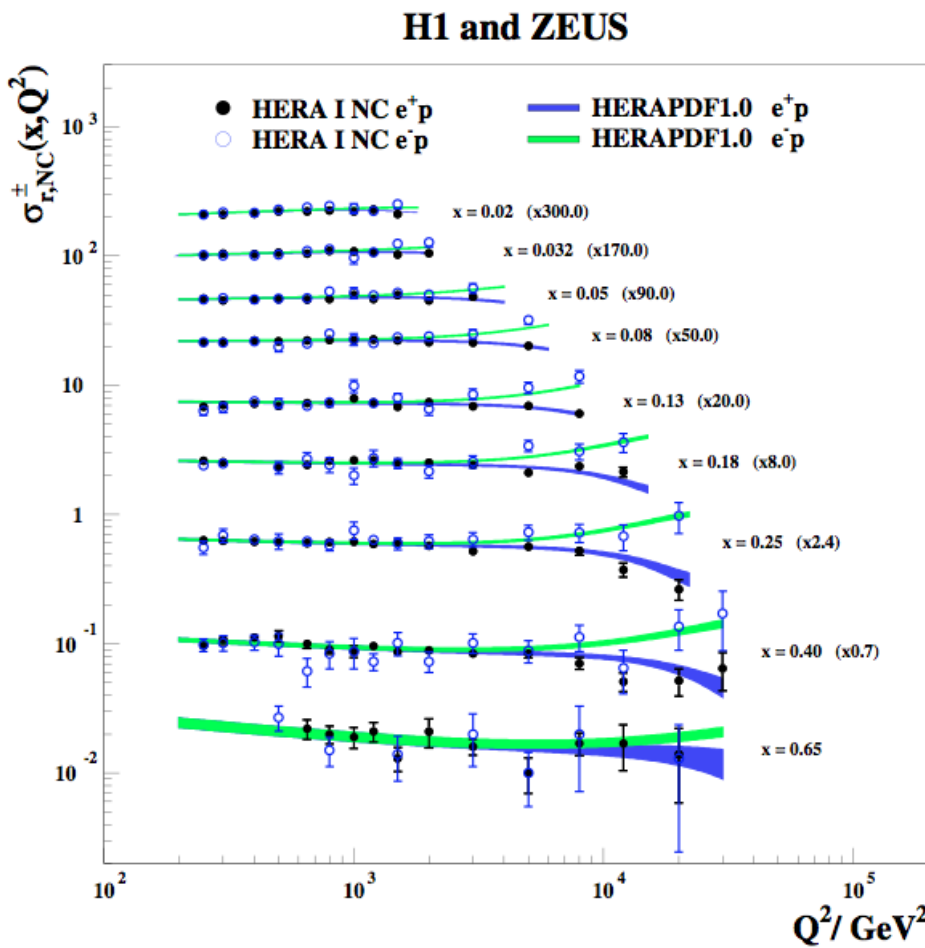
To be included
In final Combination

High Q^2 NC Cross Sections

At High $Q^2 \Rightarrow$ interference term $Z\gamma$: **destructive**(e+p) and **constructive** (e-p)

HERA I

HERA I+II



Larger HERA II luminosity yields in significant improvement in precision at high x , Q^2

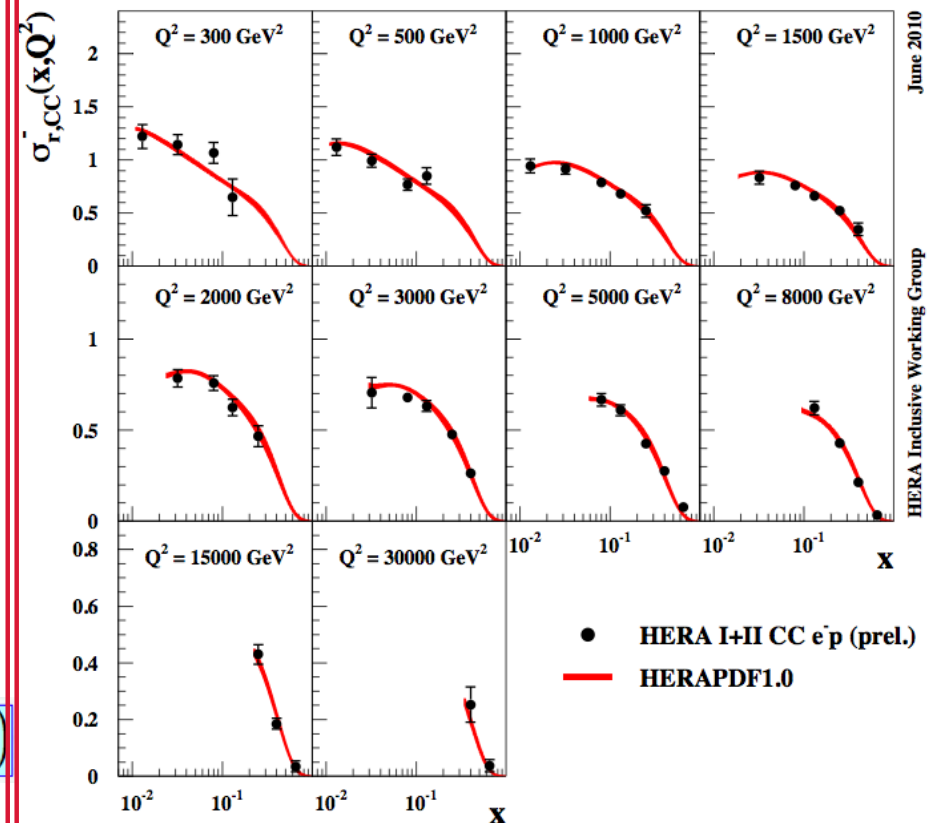
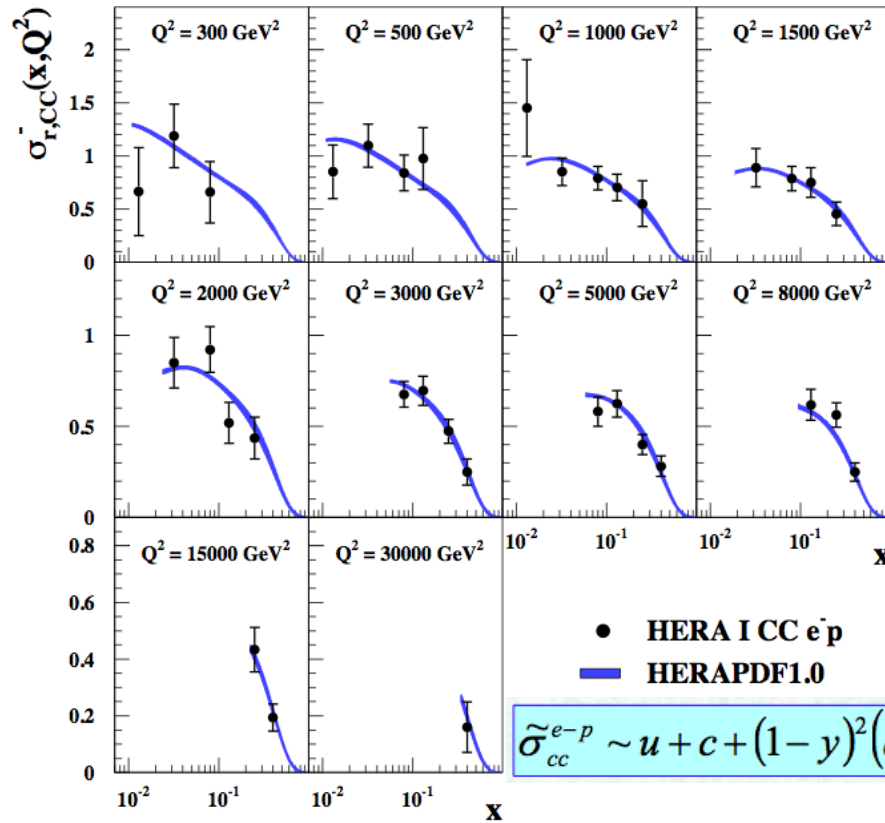
High Q^2 CC Cross Sections

HERA I

HERA I+II

H1 and ZEUS

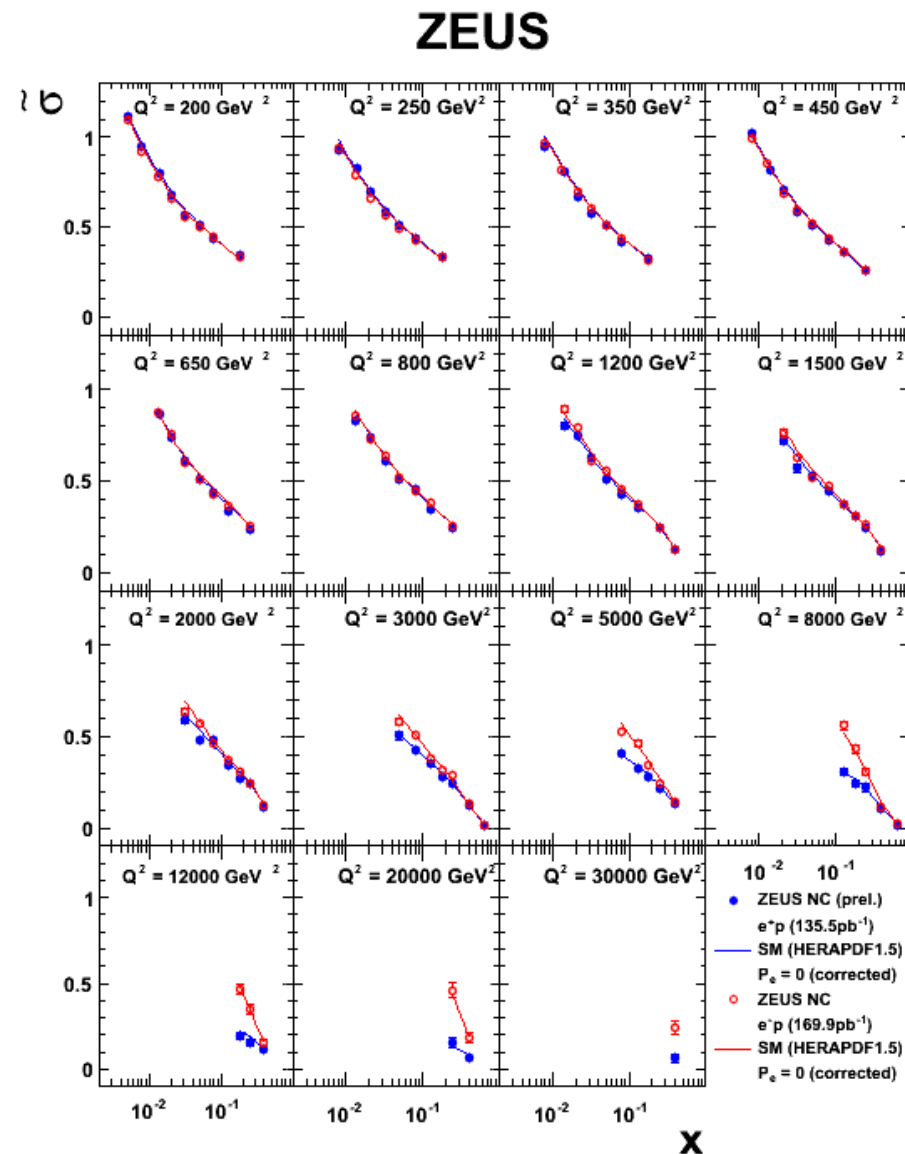
H1 and ZEUS



Much more precise CC measurements after including new high Q^2 HERA II set!

New High Q^2 NC Data

- New preliminary ZEUS e^+p NC data at High Q^2 is available:
 - Will provide additional constrain for PDFs at high x
- To be included in Final HERA Combination and future fits

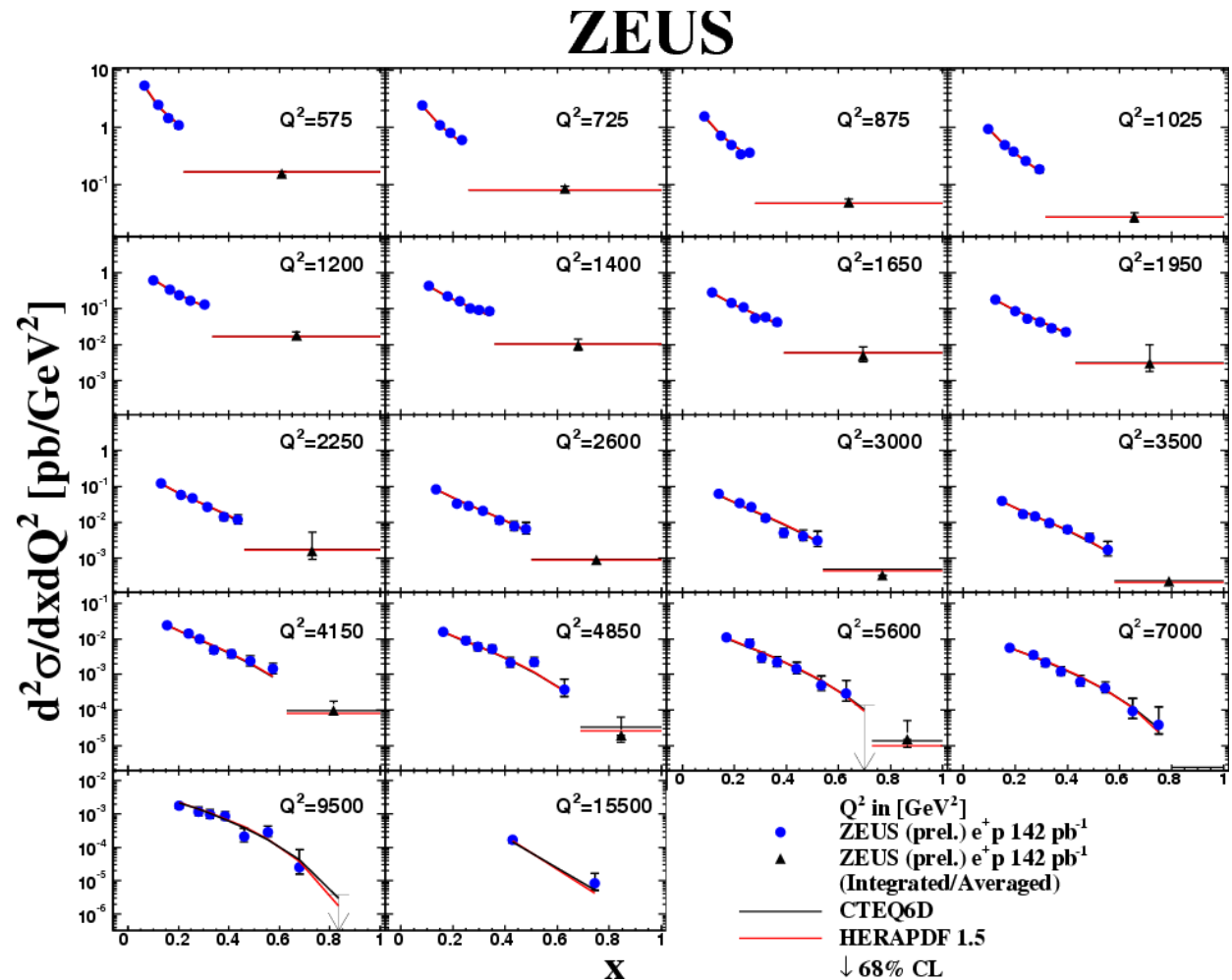


New High x NC Data

- New NC measurement at high x from ZEUS:

- x reconstruction relies on jets
- Force jets to balance pT of electron
- Gives better x resolution

- To be included in Final HERA Combination and future fits



QCD Fit Settings for HERAPDFs

PDF determination at HERA

- HERA PDFs are determined from QCD Fits to solely HERA data of $Q^2 > 3.5 \text{ GeV}^2$
- The QCD settings are optimised for HERA measurements of proton structure functions

$$F_2(x, Q^2) = \frac{4}{9}(xU + x\bar{U}) + \frac{1}{9}(xD + x\bar{D}) \quad (\text{dominated by gamma exchange})$$

- NLO (and NNLO) DGLAP evolution equations, RT-VFNS (as for MSTW08)
- PDF parametrised at the starting scale Q_0^2 : $xg, xu_{val}, xd_{val}, x\bar{U} = x\bar{u}(+x\bar{c}), x\bar{D} = x\bar{d} + x\bar{s}(+x\bar{b})$
 $Q_0^2 = 1.9 \text{ GeV}^2$ (below m_c)
 - central fit with 10 free parameters (standard) - for HERAPDF1.0 (NLO and NNLO), HERAPDF1.5(NLO)

$$xf(x, Q_0^2) = Ax^B(1-x)^C(1+Dx+Ex^2)$$
 - extended fit with 14 free parameters (flexible) - for HERAPDF1.5f (NLO), HERAPDF1.5 (NNLO) and for jet fits HERAPDF1.6 [see A. Cooper's talk]

$$xf(x, Q_0^2) = Ax^B(1-x)^C(1+Dx+Ex^2) - A'x^{B'}(1-x)^{25}$$

Imposing momentum sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Additional Constraints:

$x\bar{s} = f_s x\bar{D}$ strange sea is a fixed fraction f_s of \bar{D} at Q_0^2

$B_{Ubar} = B_{Dbar}$
 sea = 2 x (Ubar + Dbar)
 Ubar = Dbar at $x=0$

In 10p fit: $B_{uv} = B_{dv}$

Sources of PDF uncertainties at HERA

Experimental Uncertainties:

- Consistent data sets \rightarrow use $\Delta\chi^2 = 1$
- Cross checked with Monte Carlo method [PDF4LHC Interim Report arXiv:1101.0536]

Model Uncertainties:

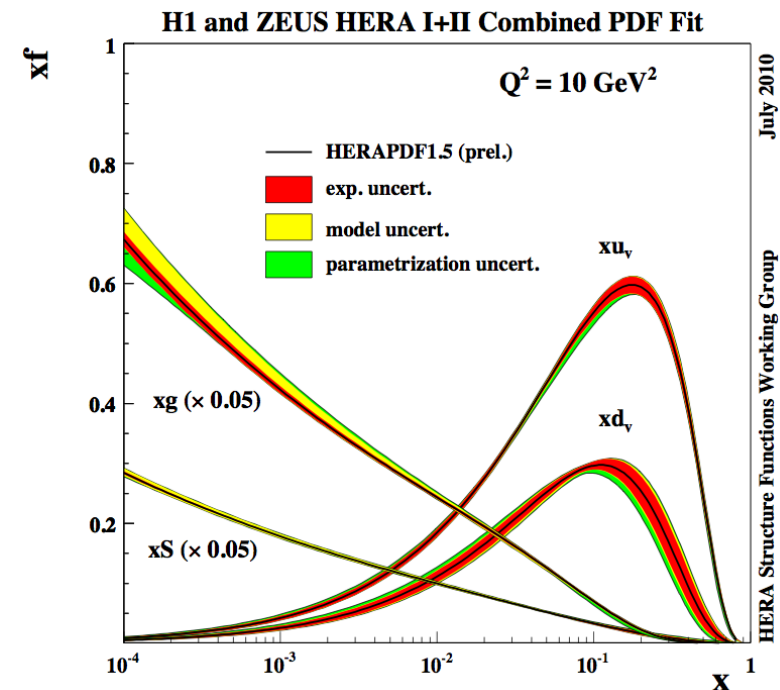
- following variations have been considered

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c [GeV]	1.4	1.35 ^(a)	1.65
m_b [GeV]	4.75	4.3	5.0
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.5 ^(b)	2.5 ^(c,d)

^(a) $Q_0^2 = 1.8$ ^(c) $m_c = 1.6$
^(b) $f_s = 0.29$ ^(d) $f_s = 0.34$

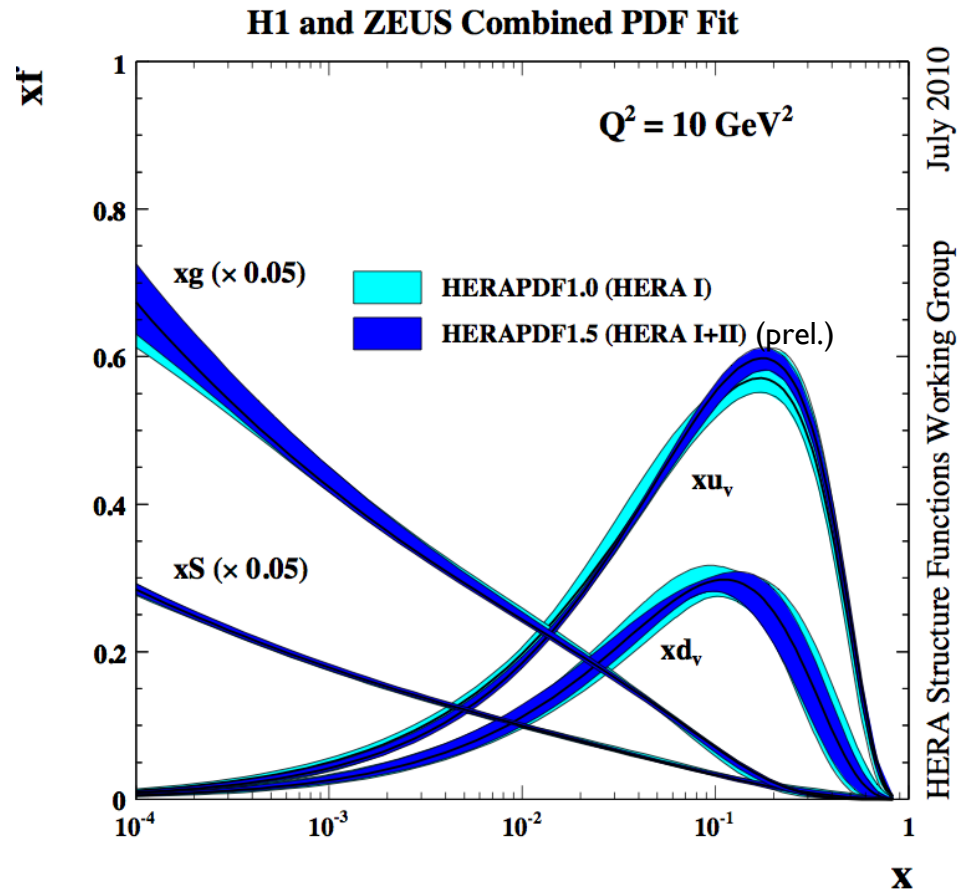
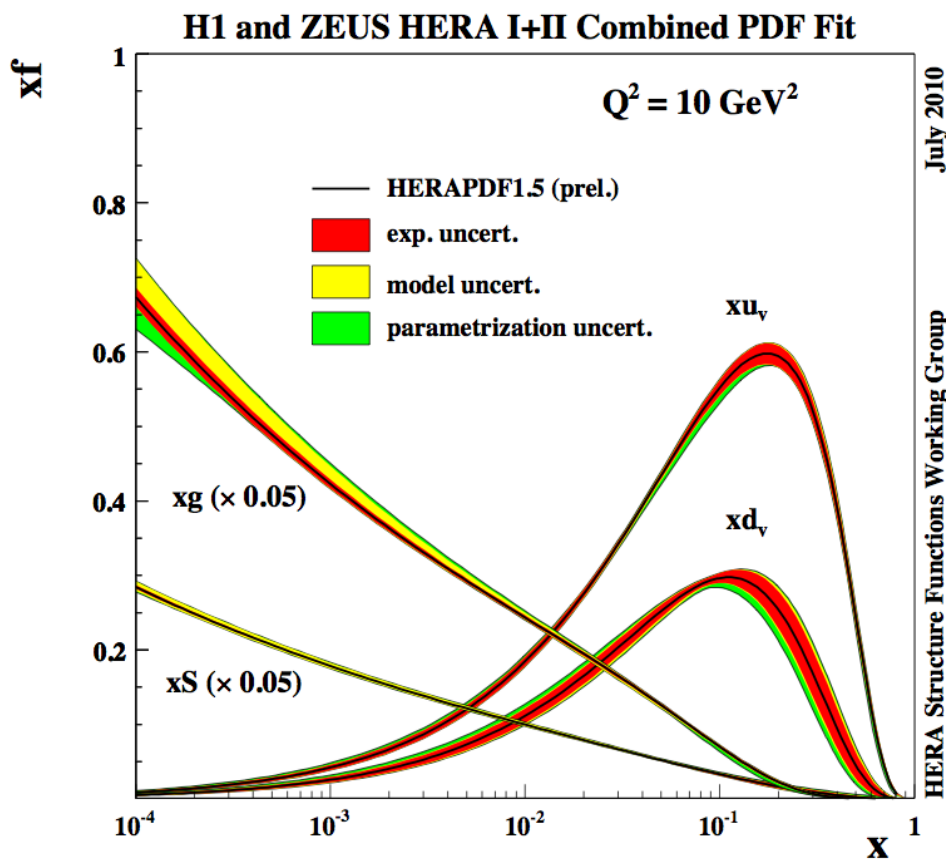
Parametrisation Uncertainties:

- An envelope formed from PDF fits using other variants of parametrisation form at the starting scale (especially sensitive to the higher x region):
 - Scanning of parameter space
 - Q_0^2 variation and a more flexible gluon parametrisation



Results based on HERA I+II data: HERAPDF1.5 (NLO)

- xg , xu_v , xd_v , xS ($xS=xU+xD$) at the scale $Q^2=10 \text{ GeV}^2$

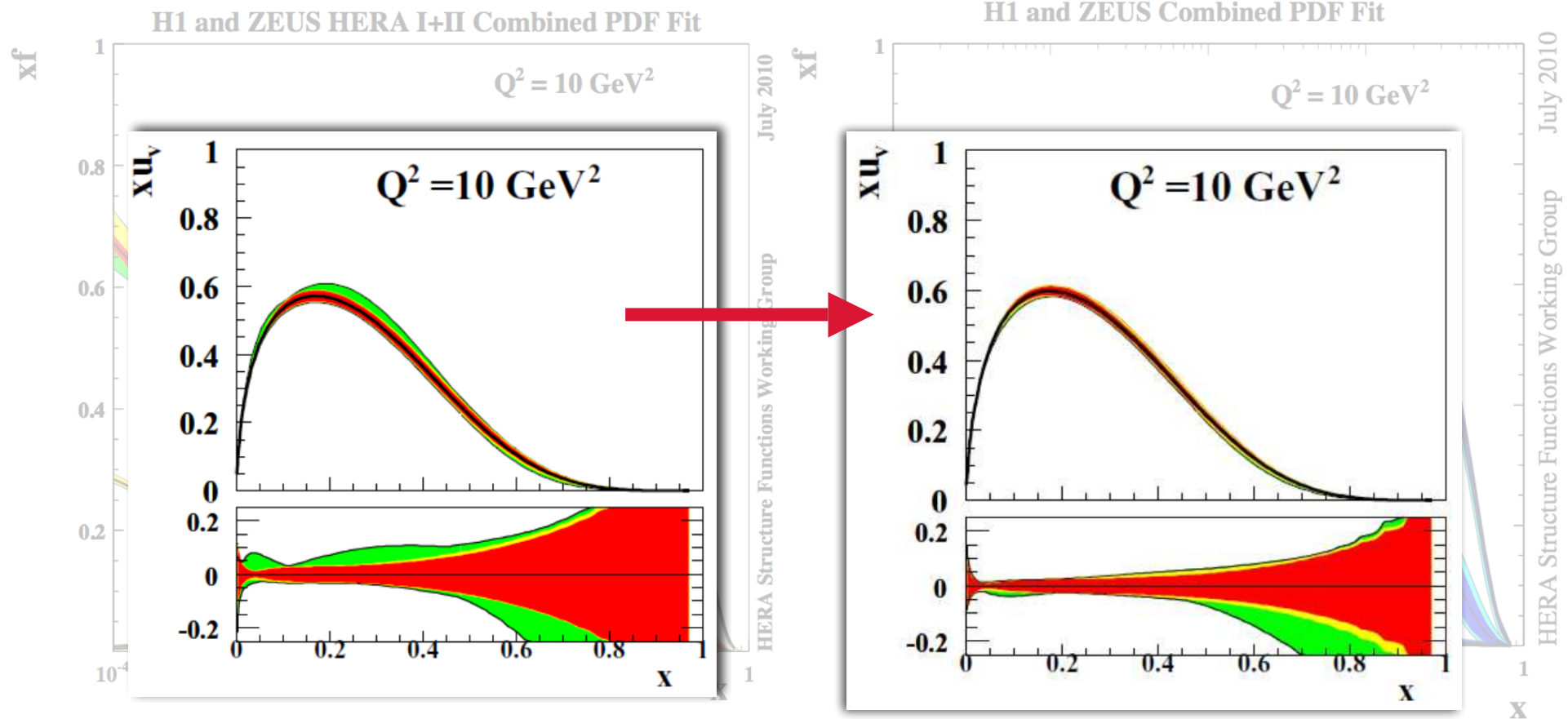


- Inclusion of the HERA II data reduces the uncertainties on PDFs in the high x region especially visible on the valence distributions!
 - See HERAPDF1.5(prel) vs HERAPDF1.0

Results based on HERA I+II data: HERAPDF1.5 (NLO)

HERA I

HERA I+ II



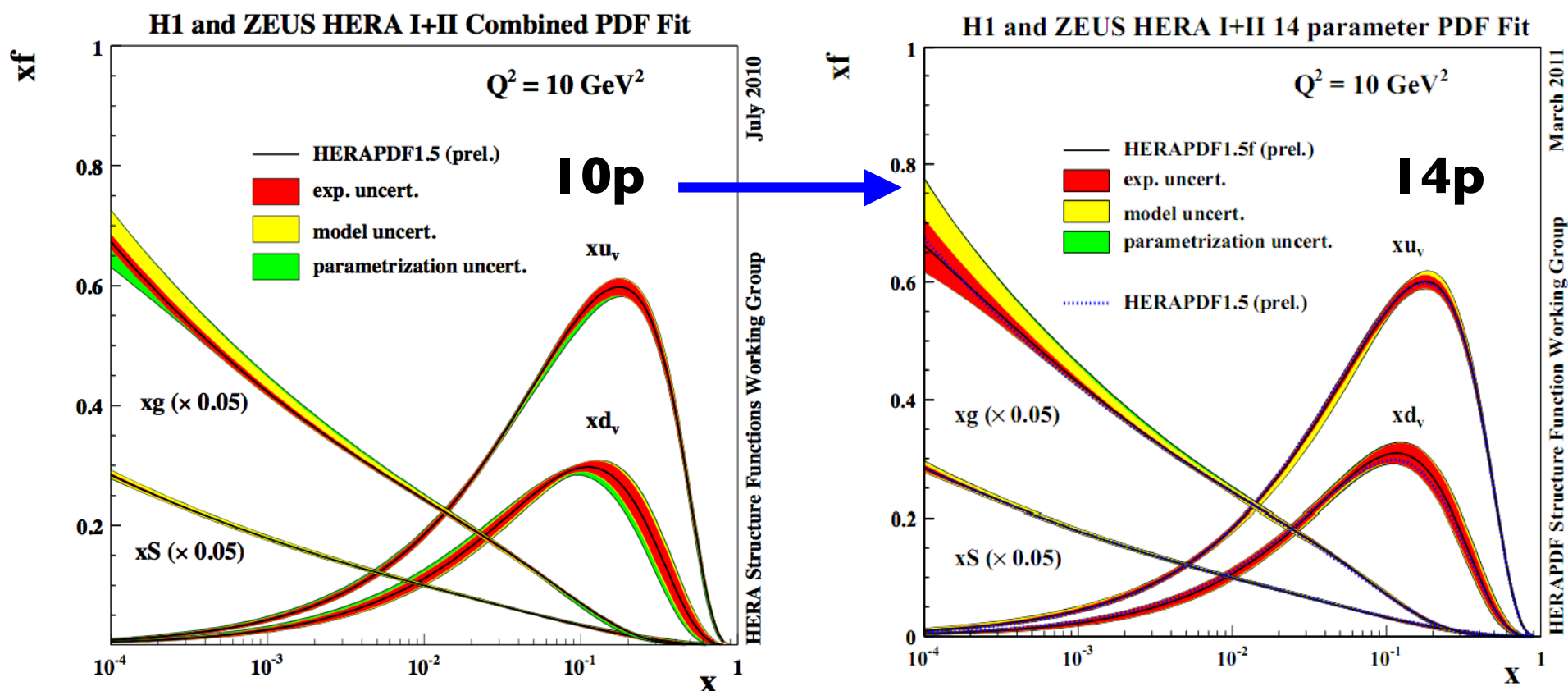
- Inclusion of the HERA II data reduces the uncertainties on PDFs in the high x region especially visible on the valence distributions!
 - See [HERAPDF1.5\(prel\)](#) vs [HERAPDF1.0](#)

HERAPDF1.5 vs HERAPDF1.5f at NLO

- Additional studies show that a more flexible gluon parametrisation would be more suitable for further studies (NNLO fits, addition of the jet data):

$$xg(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C - \underbrace{A' \cdot x^{B'}}_{\text{more flexible}} \cdot (1-x)^{25}$$

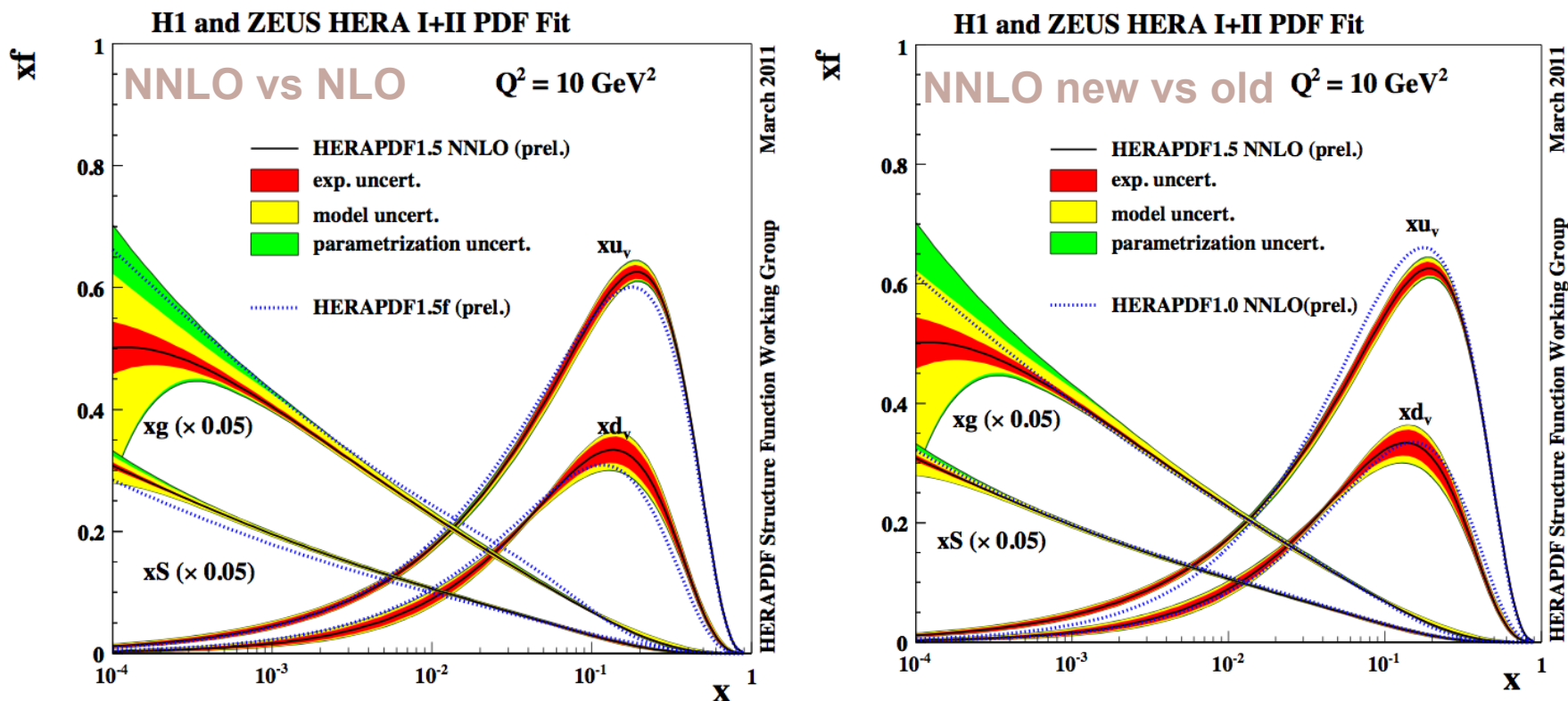
- HERA II data can provide constraints for valence distributions, hence the assumption of $B_{uv}=B_{dv}$ is released and a more flexible valence parametrisation can be used.



Results based on HERA I+II data: HERAPDF1.5 (NNLO)

- Fits performed to HERA I data (as used for HERAPDF1.0) at NNLO using RT-VFNS:

$$\alpha_s(M_Z) \text{ at NNLO} = 0.1176$$



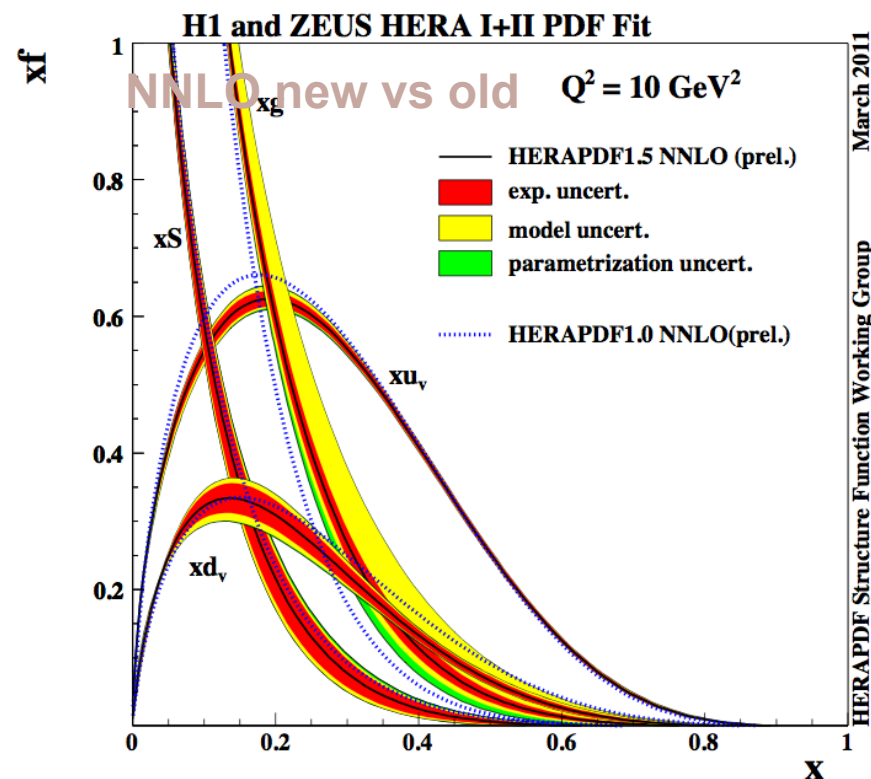
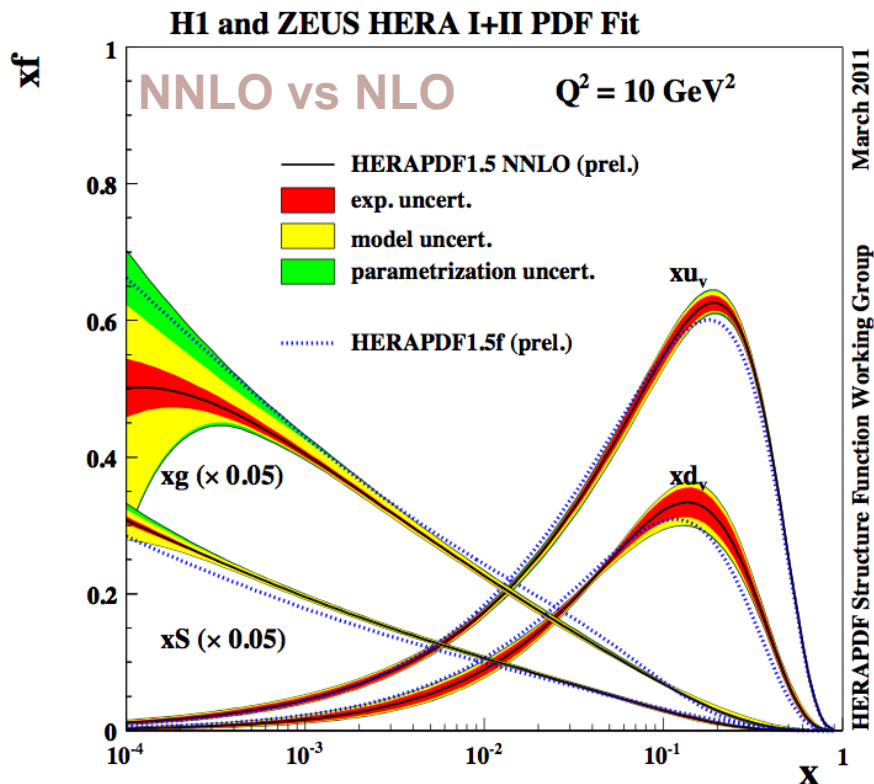
scheme	NNLO $\alpha_s(M_Z)=0.1176$	NLO $\alpha_s(M_Z)=0.1176$
All χ^2/dof	744.3/660	735.1/660

- HERAPDF1.5 NLO vs NNLO is in much better agreement than for HERAPDF1.0 case
 - use of a more flexible parametrisation for the central fit (10 parameters vs 14 parameters fit)
- HERAPDF1.5 NNLO vs HERAPDF1.0 NNLO yields a harder gluon and softer valence at high x

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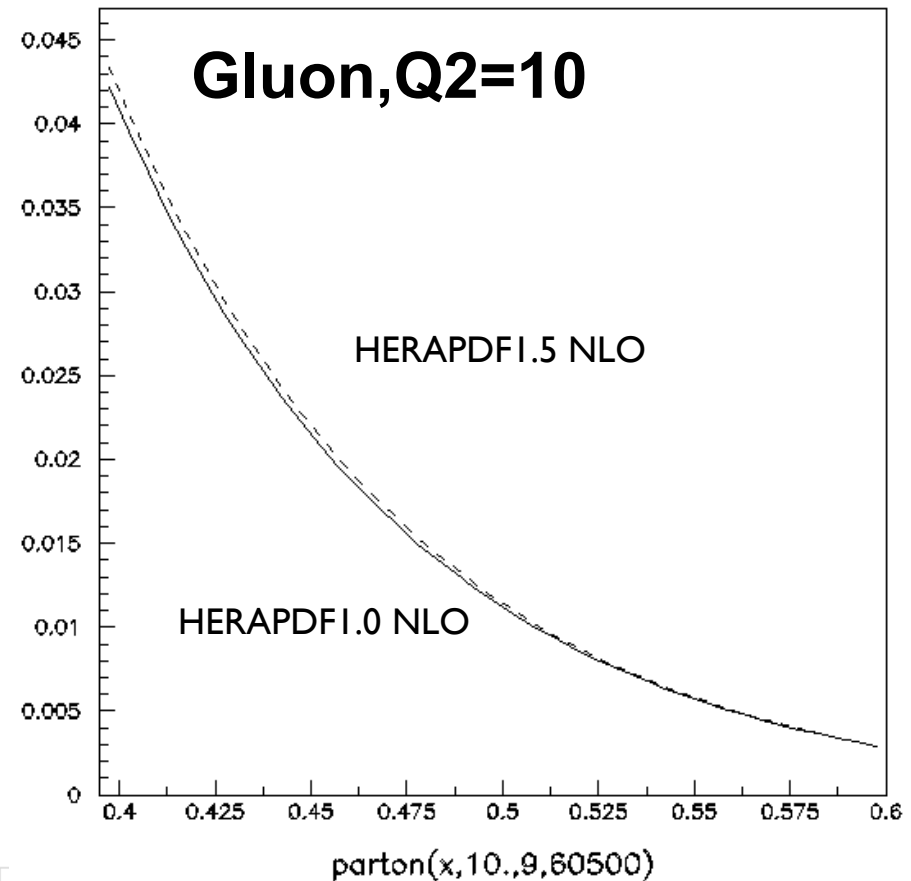
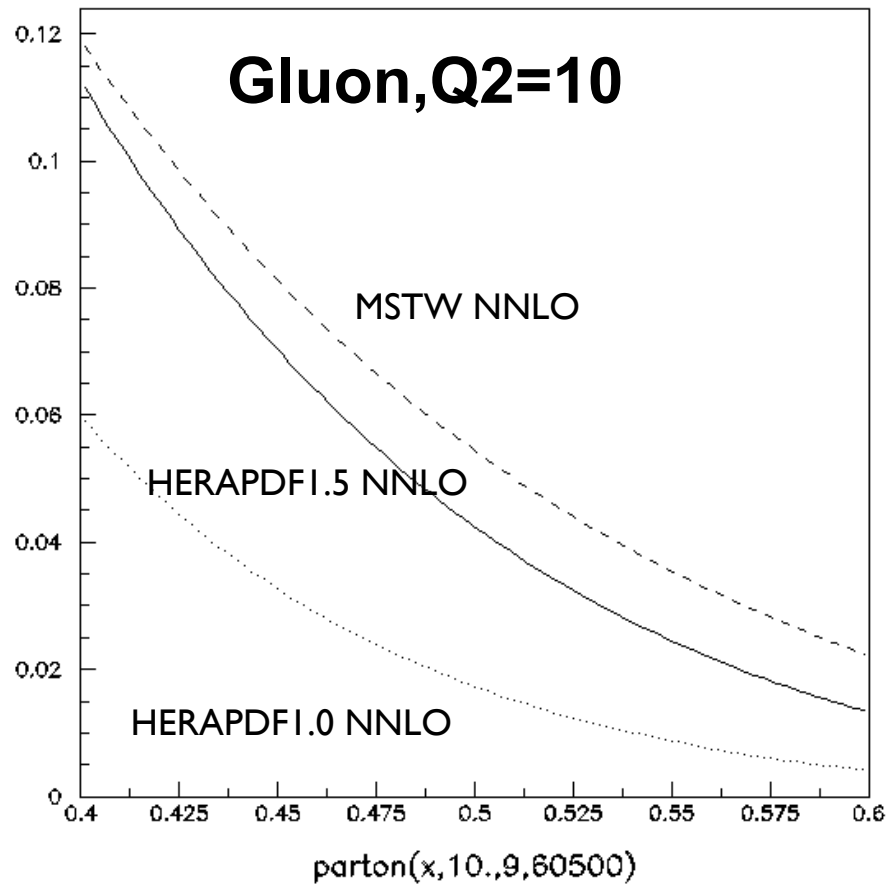
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HERAPDF comparisons vs MSTW08

2011/03/18 17.40

2011/03/18 17.55



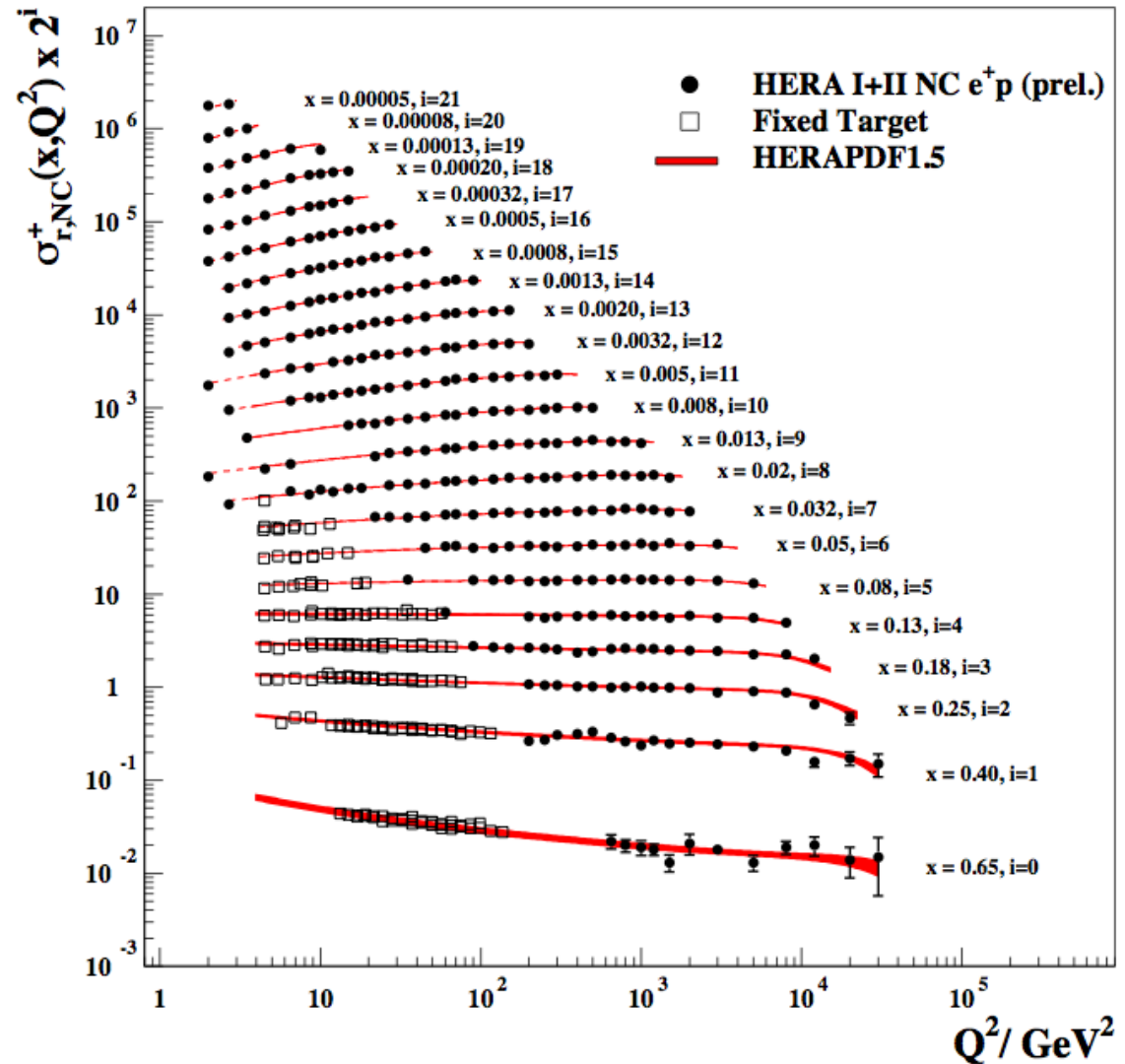
- HERAPDF1.0 NLO vs HERAPDF1.5NLO differences are minimal for gluon at high x
- HERAPDF1.0 NNLO vs HERAPDF1.5 NNLO large differences.

Predictions based on HERAPDFs

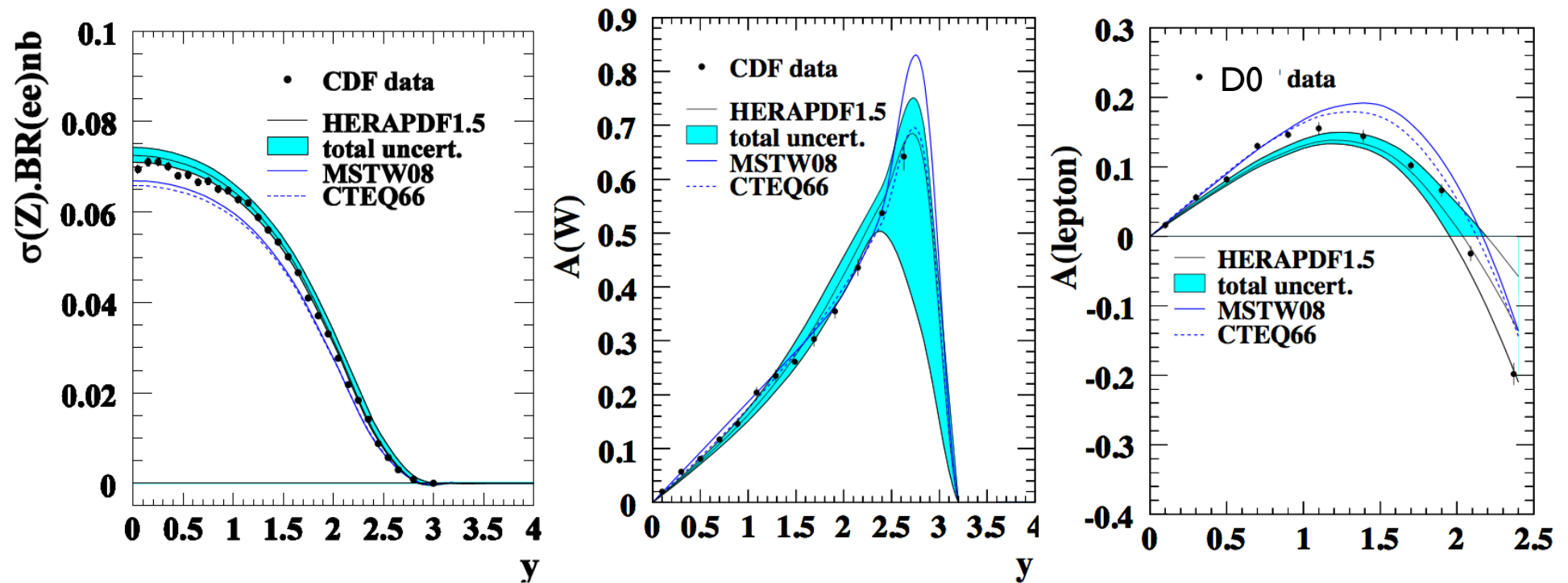
HERAPDF1.5 vs DIS Data

H1 and ZEUS

- Extended kinematic range of the HERA I and II data as compared to the fixed target data:
 - Fit line includes total error
- HERAPDF1.5 fit describes our data well over
- Extrapolation of the HERAPDF1.5 fits agree well with fixed target data:
 - SLAC and BCDMS

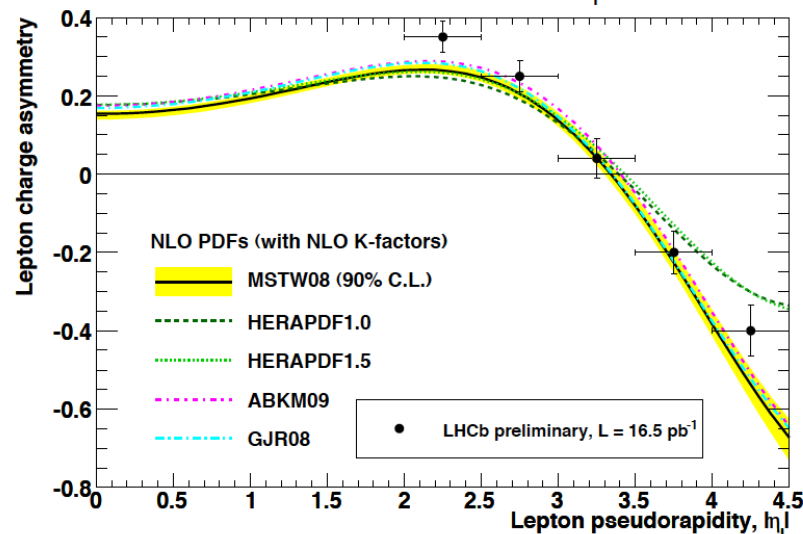
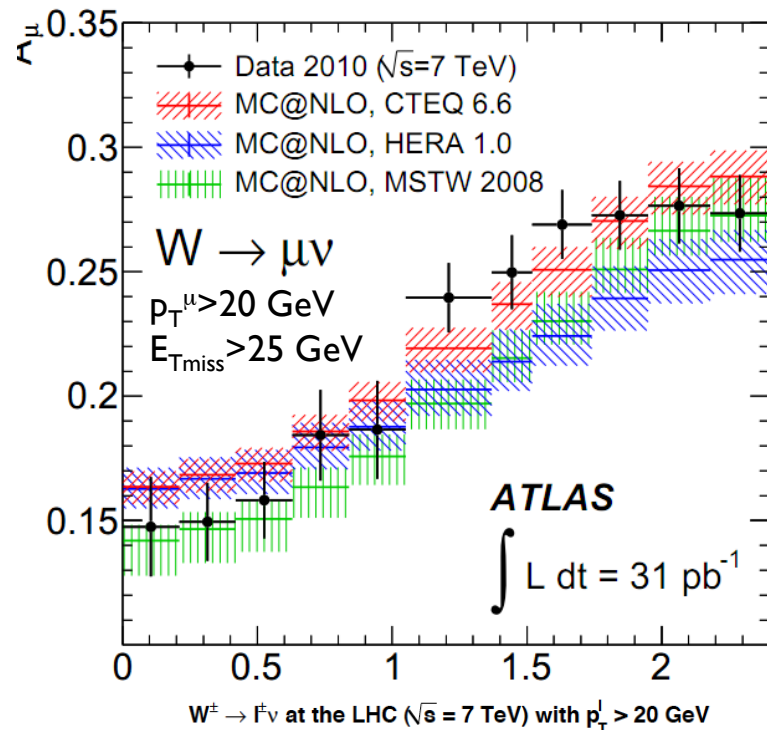


HERAPDF1.5 (NLO) vs Tevatron Data



- HERAPDF1.5 results in a reasonable agreement with the CDF data for Z rapidity, the W asymmetry and the D0 lepton asymmetry, even if this data is not included in the HERA fits.
- DIS data from HERA predicts well Z and W at Tevatron from the $p\bar{p}$ processes.

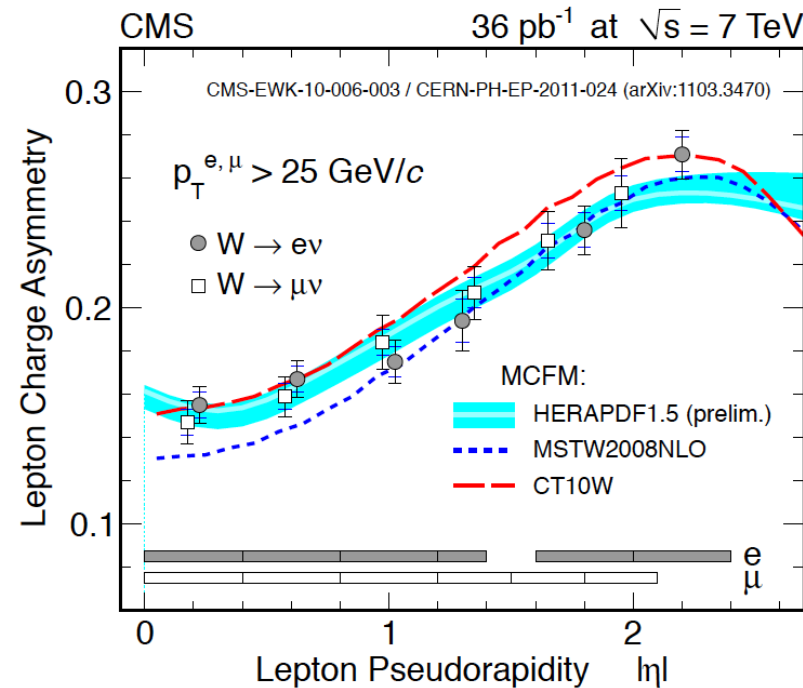
HERAPDF Predictions for W and lepton asymmetries at LHC



- W asymmetry is sensitive to differences between u and d
- Difference in u and d quarks can be better measured by all experiments at the LHC

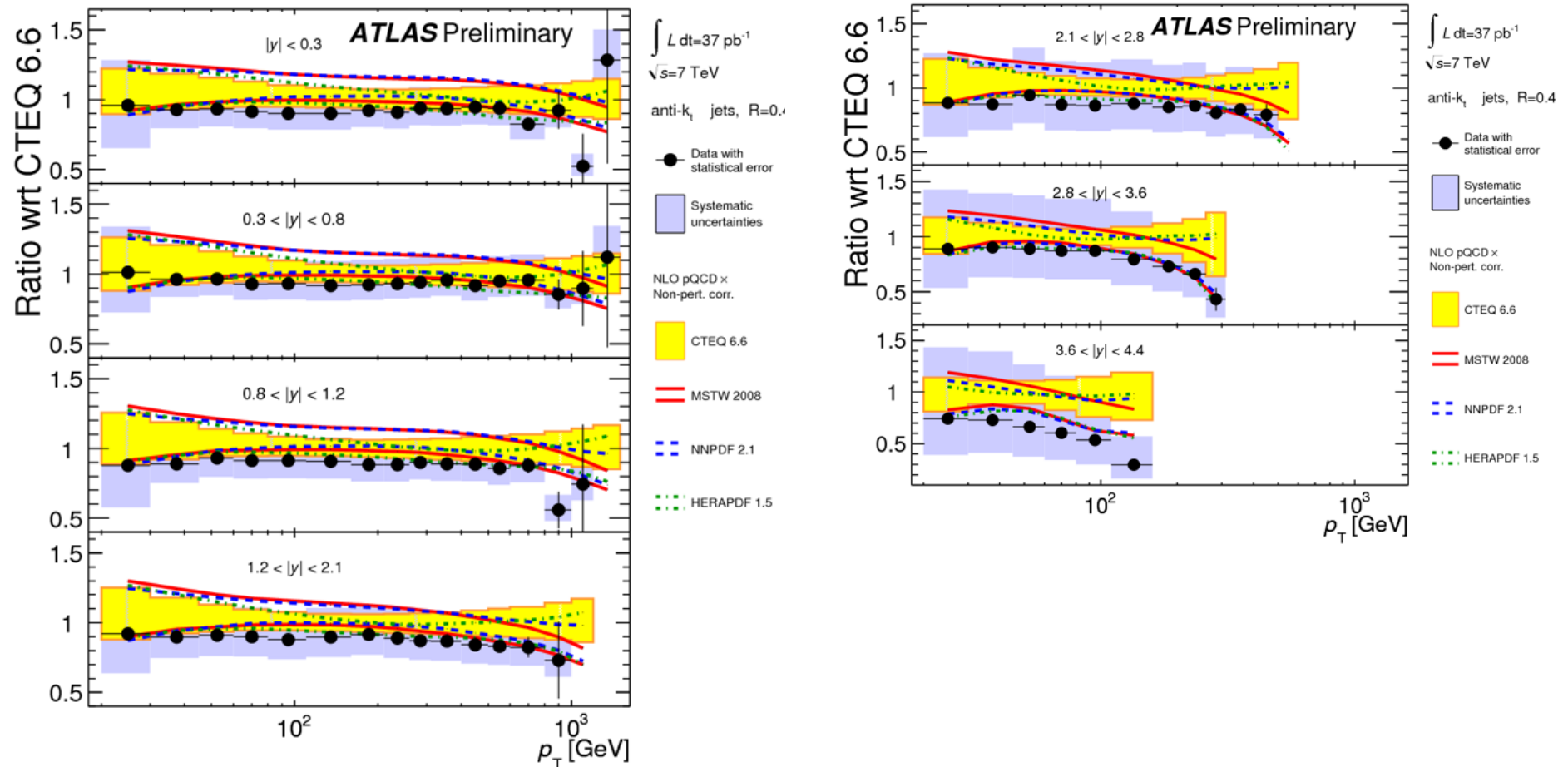
$$A_\pm(y_W) = \frac{d\sigma/dy_W(W^+) - d\sigma/dy_W(W^-)}{d\sigma/dy_W(W^+) + d\sigma/dy_W(W^-)}$$

$$\approx \frac{u(x_1)\bar{d}(x_2) - d(x_1)\bar{u}(x_2)}{u(x_1)\bar{d}(x_2) + d(x_1)\bar{u}(x_2)} \approx \frac{u(x_1) - d(x_1)}{u(x_1) + d(x_1)}$$



HERAPDF provides good description to pp process too

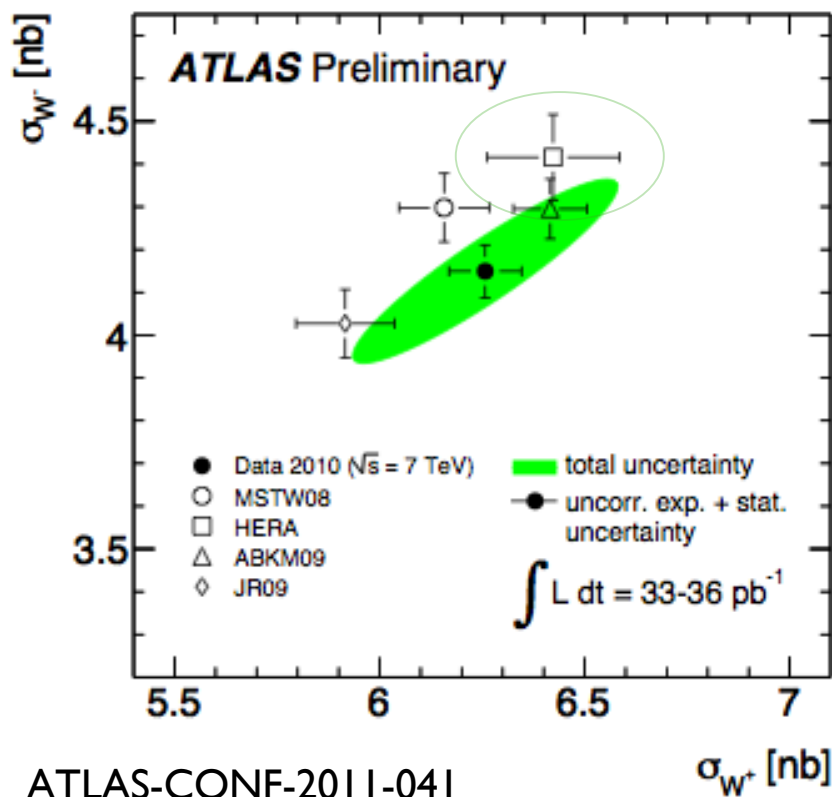
Predictions for ATLAS Jet Data



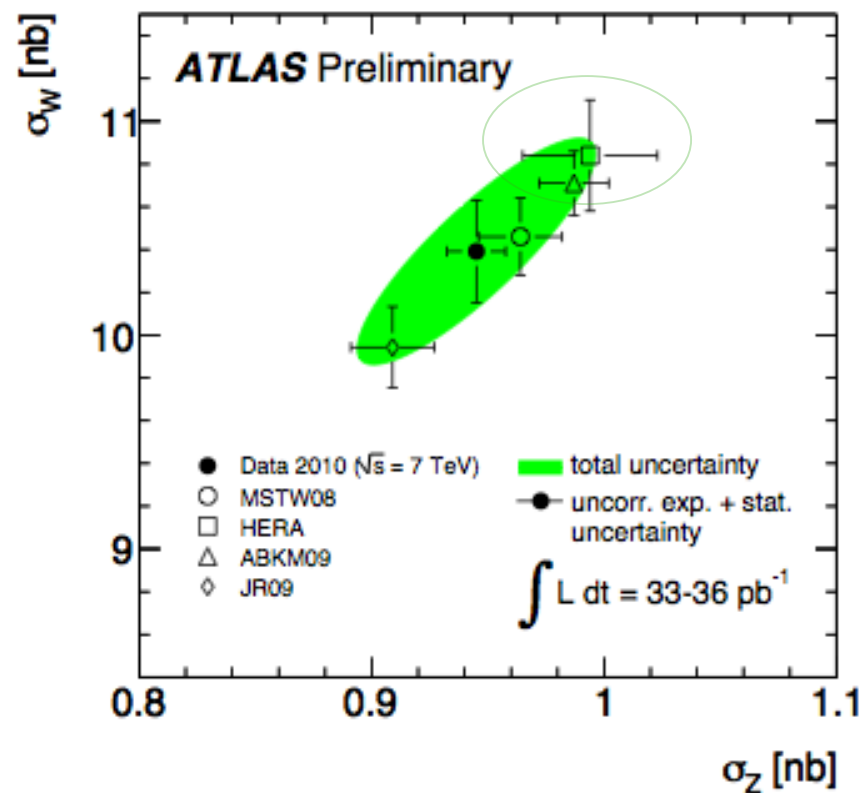
- New ATLAS measurement based on complete 2010 data set extending to forward and lower p_T regions, with improved JES uncertainty.
- Best agreement seems to be with HERAPDF1.5, however experimental/theoretical uncertainties are sizeable

LHC predictions for W, Z cross sections

- Compare measured and predicted cross sections (NNLO):
 - HERAPDF1.0($\alpha_s=0.1145$), ABKM, JR09, MSTW08



ATLAS-CONF-2011-041



HERAPDF1.0 based solely on ep data provides a competitive prediction to the LHC data!

Summary

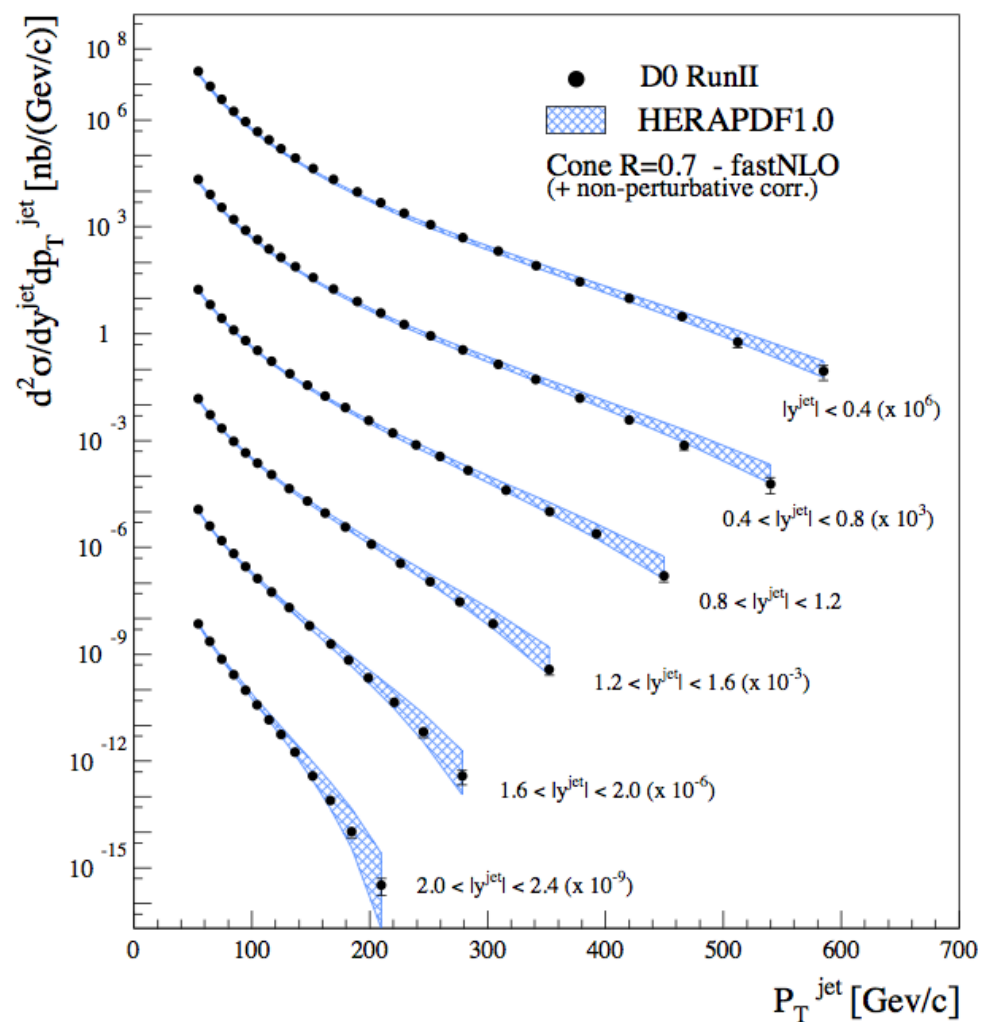
- HERA provides unique determinations of the proton structure and can predict related Standard Model processes.
- New preliminary combined HERA-II measurements improves accuracy at high x and allow for releasing of PDF assumptions:
 - ➔ HERAPDF1.5 at NLO and NNLO with full error band
 - New measurements available with potential to further constrain the PDFs at high x to be included in the next data combination towards final HERAPDF release.
- HERAPDF predicts measurements from Fixed Target and Tevatron experiments well.
- HERA data are confronted with the first results from the LHC:
 - Quantitative test of the Standard Models: predictions from ep scattering are in good agreement with first observations at pp machine.
- HERAPDF is a unique platform for understanding the q-g dynamics in the proton by focused studies based on new HERA measurements and for providing predictions free of higher twist and nuclear corrections which are inherent to global fits.

https://www.desy.de/h1zeus/combined_results/index.php?do=proton_structure

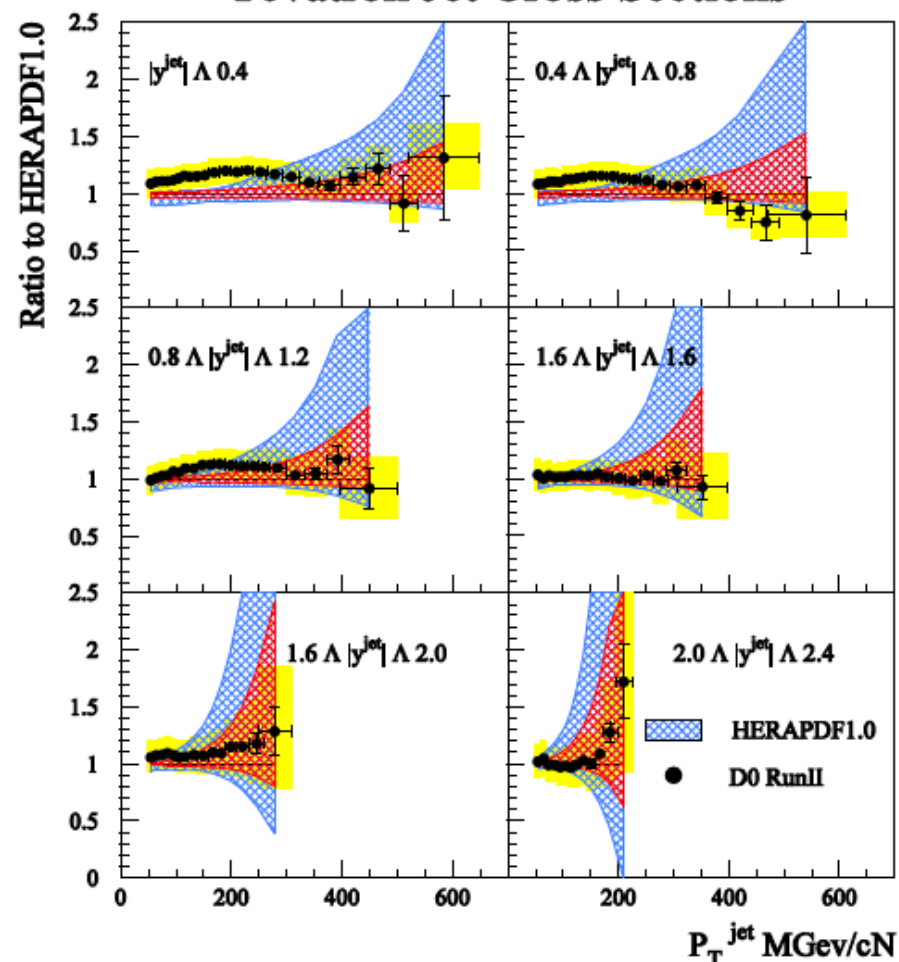
Backup
not necessarily useful

HERAPDF1.0 vs Tevatron Jet Data

Tevatron Jet Cross Sections



Tevatron Jet Cross Sections



- Predictions for high- E_T jet cross-sections with full uncertainties compared to the D0 data
- DIS data from HERA predicts Tevatron jets production from $p\bar{p}$ process.

More on Tevatron Jets

description of CDF II inclusive jet (k_T) data [hep-ex/0701051]

- Values of $\chi^2/N_{\text{pts.}}$ with (without) accounting for correlations:

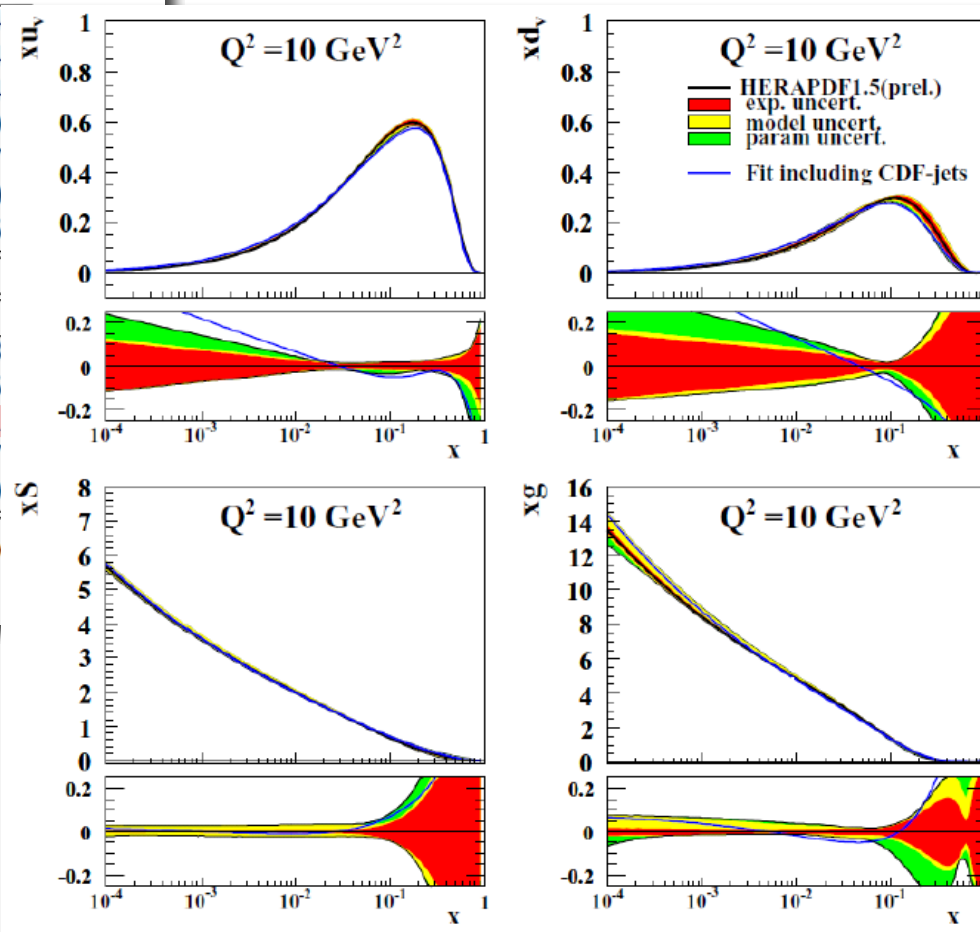
NLO PDF	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	0.75 (0.30)	0.68 (0.28)	0.91 (0.84)
CTEQ6.6	1.25 (0.14)	1.66 (0.20)	2.38 (0.84)
CT10	1.03 (0.13)	1.20 (0.19)	1.81 (0.84)
NNPDF2.1	0.74 (0.29)	0.82 (0.25)	1.23 (0.69)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.43 (0.39)	3.26 (0.66)	4.03 (1.67)
ABKM09	1.62 (0.52)	2.21 (0.85)	3.26 (2.10)
GJR08	1.36 (0.23)	0.94 (0.13)	0.79 (0.36)

NNLO PDF	$\mu = p_T/2$	$\mu = p_T$	$\mu = 2p_T$
MSTW08	1.39 (0.42)	0.69 (0.44)	0.97 (0.48)
HERAPDF1.0 ($\alpha_S = 0.1145$)	2.64 (0.36)	2.15 (0.36)	2.20 (0.46)
HERAPDF1.0 ($\alpha_S = 0.1176$)	2.24 (0.35)	1.17 (0.32)	1.23 (0.31)
ABKM09	2.55 (0.82)	2.76 (0.89)	3.41 (1.17)
JR09	0.75 (0.37)	1.26 (0.41)	2.21 (0.49)

- Similar trends for CDF II (cone) data and DØ II (cone)

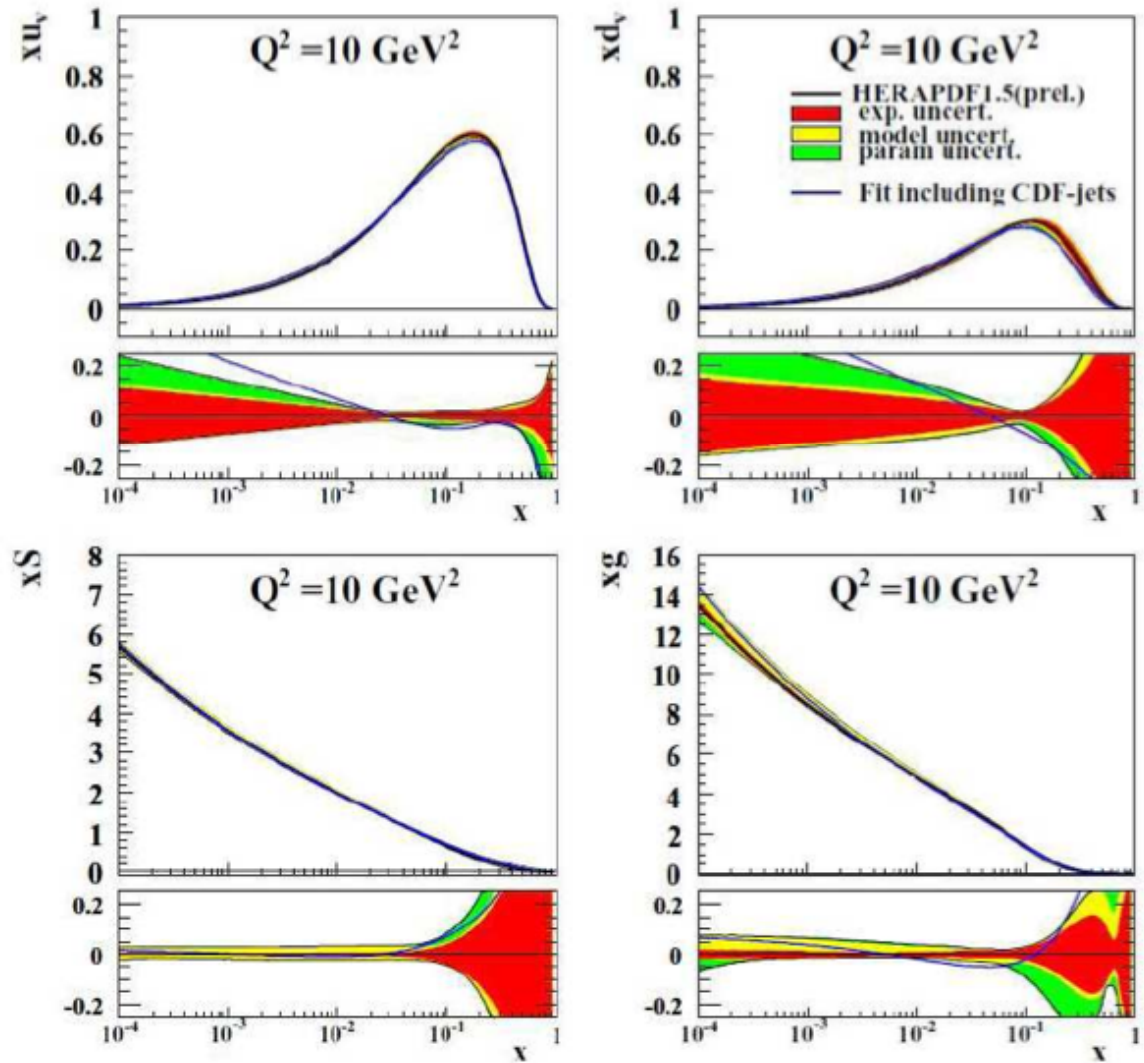
Table from G Watt

- Based on HERAPDF1.5 (NLO):
 - NO fit : 176/76 (central line)
 - Similar to HERAPDF1.0 due to the same high x gluon between 1.0 and 1.5
 - After fit: 113/76
- HERAPDF1.5 NLO describes Tevatron Data within uncertainties!
- HERAPDF1.5 NNLO: NO fit: 72/76

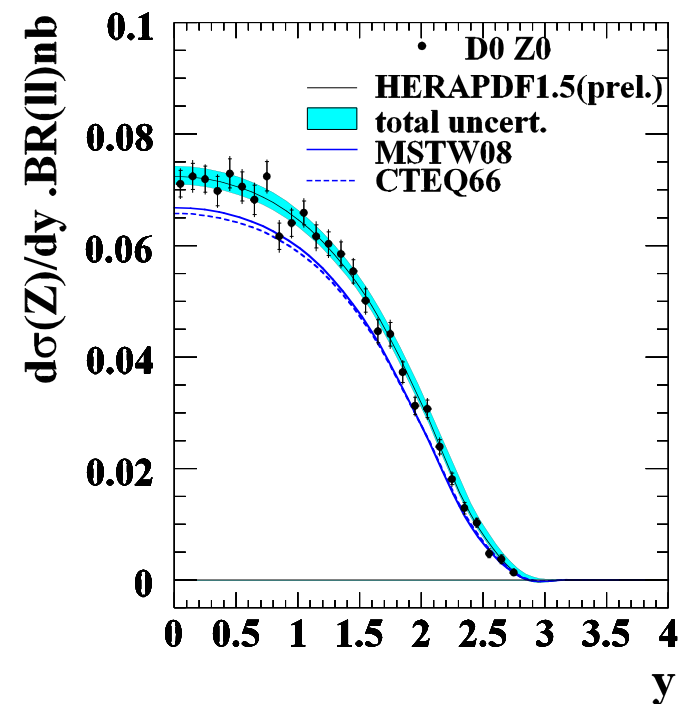
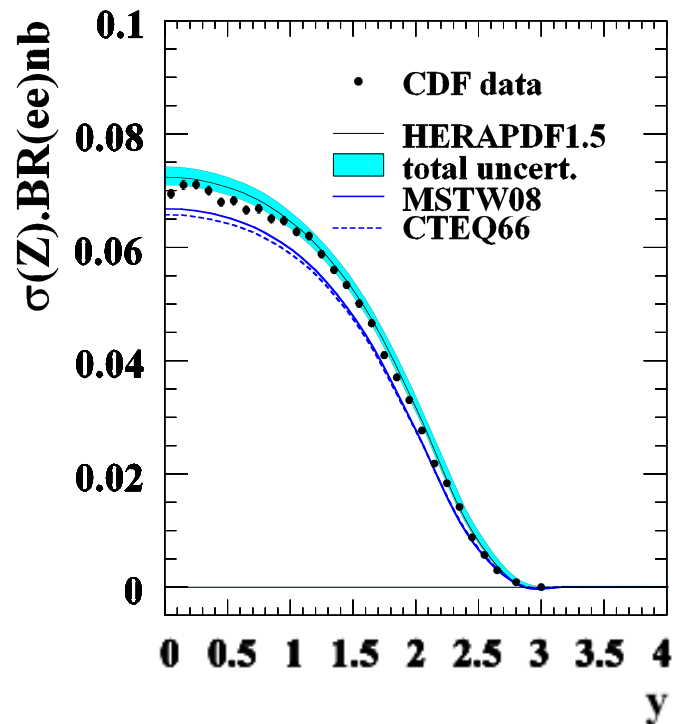


Tevatron jets

- Tevatron jet data provides additional constraints on gluon at high x .
- HERAPDF1.5 provides “reasonable” description of the data.
- Putting the data in the fit gives $\chi^2/dof = 113/76$.



HERAPDF predictions vs Tevatron: Z rapidity

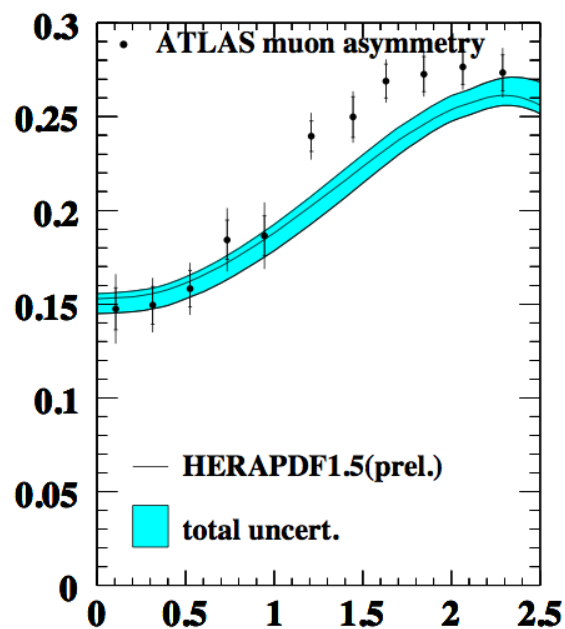


- The description of CDF and D0 Z rapidity by HERAPDF1.5 is good:
 - Without fitting these data (without taking into account PDF uncertainties):
 - $\chi^2/\text{dof}=36/28$ CDF - more precise data
 - $\chi^2/\text{dof}=23/28$ D0
 - After fitting these data:
 - $\chi^2/\text{dof}=27/28$ CDF
 - $\chi^2/\text{dof}=16/28$ D0

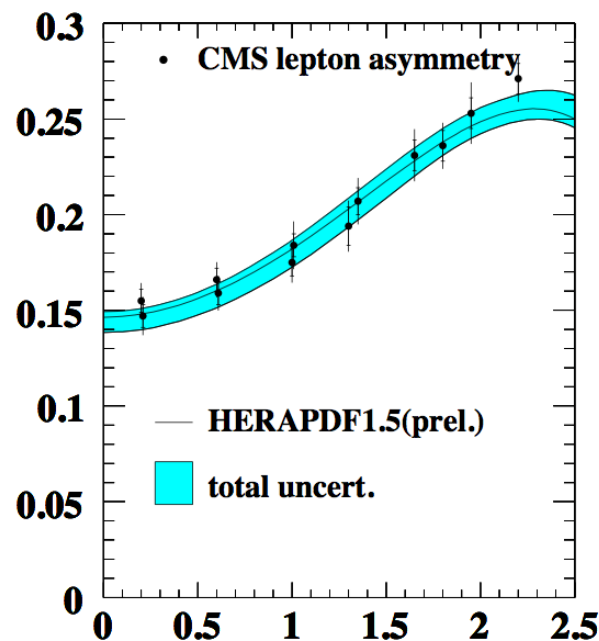
Question is: does this fit lies within the uncertainties of HERAPDF1.5?

ATLAS and CMS W charge lepton asymmetries

- HERAPDF1.5 predictions confronted with LHC W charged asymmetry data:



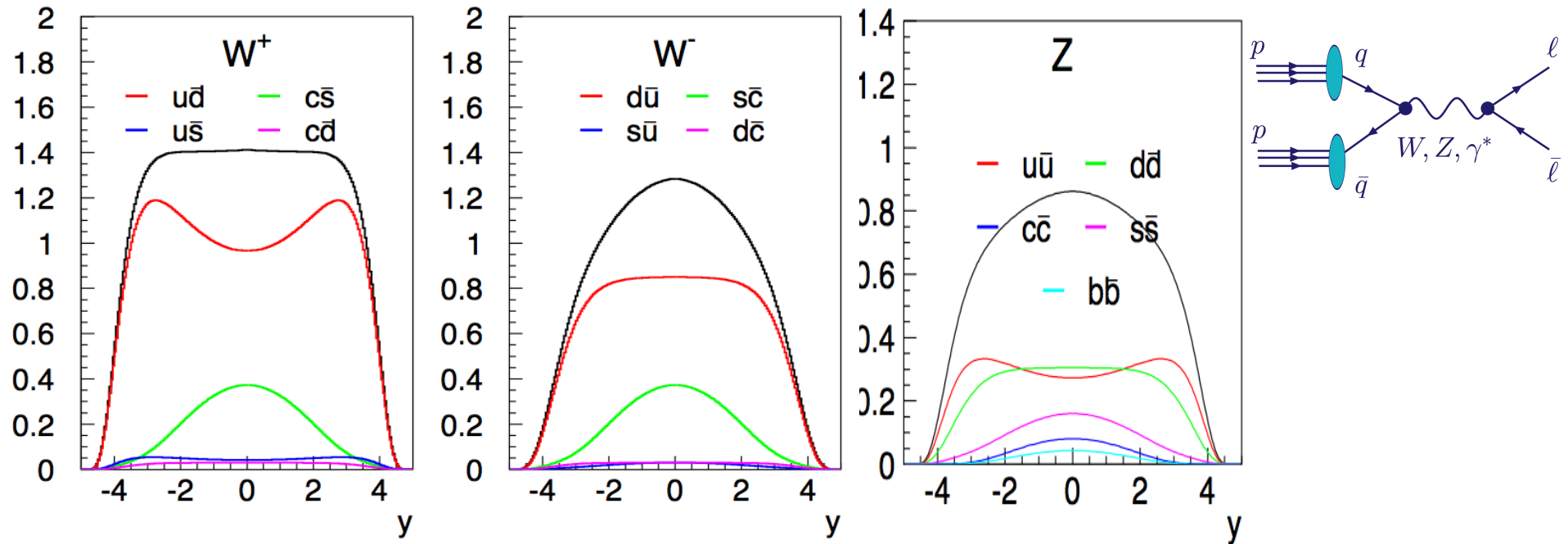
$P_{t,e} > 20 \text{ GeV}, P_{t,miss} > 25 \text{ GeV}$



$P_{t,e} > 25 \text{ GeV}$

- HERAPDF1.5 provides good description of the CMS data and not so good for ATLAS data:
 - Without including data in the fits:
 - CMS: $\chi^2/\text{dof}=6.5/12$ (muon and electron channels)
 - ATLAS: $\chi^2/\text{dof}=30/11$ (only muon channel)
 - After including data in the fits:
 - CMS: $\chi^2/\text{dof}=4.5/12$
 - ATLAS: $\chi^2/\text{dof}=16/11$

Decomposition of W and Z at the LHC



Flavour decomposition:

For Ws:

- ud dominates for W
- u_{val} peaks at large rapidity
- sc important at mid y

For Z:

- all flavours contribute, even b is significant
- larger coupling to d compared to u

$$W^+ \sim 0.95(u\bar{d} + c\bar{s}) + 0.05(u\bar{s} + c\bar{d})$$

$$W^- \sim 0.95(d\bar{u} + s\bar{c}) + 0.05(d\bar{c} + s\bar{u})$$

$$Z \sim 0.29(u\bar{u} + c\bar{c}) + 0.37(d\bar{d} + s\bar{s} + b\bar{b})$$

$$\gamma^* \sim 0.44(u\bar{u} + c\bar{c}) + 0.11(d\bar{d} + s\bar{s} + b\bar{b})$$