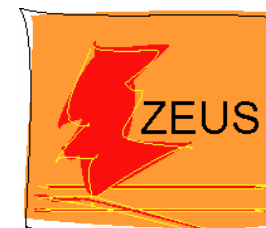


QCD measurements with jets and α_s determination at HERA



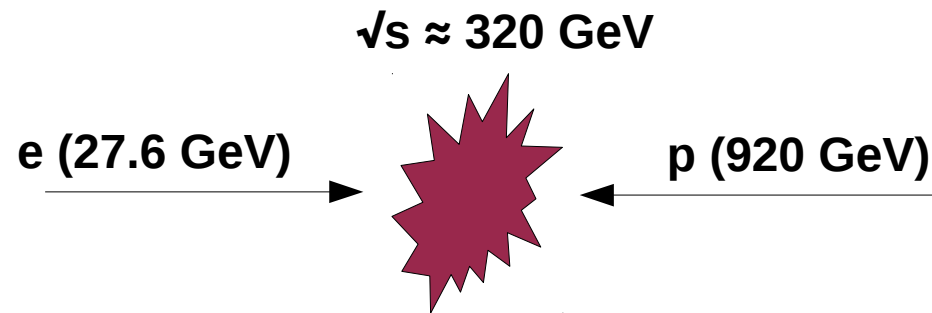
Krzysztof Nowak
on behalf of
H1 and ZEUS
collaborations



- ✓ *Introduction to jets at HERA*
- ✓ *H1 and ZEUS jet measurements*
- ✓ *Strong coupling constant α_s determination*

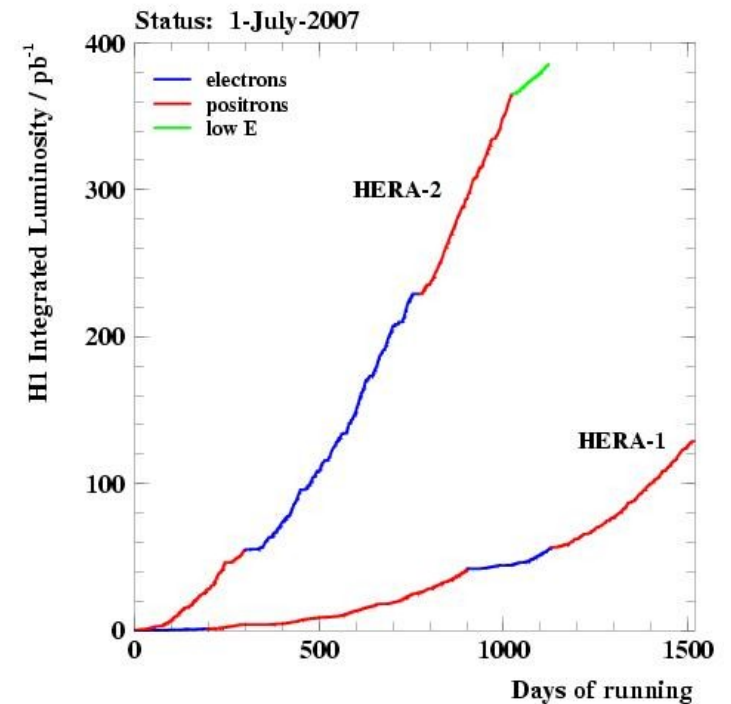
QCD at HERA

HERA ep collisions great for precise QCD studies



Collected $\sim 0.5 \text{ fb}^{-1}$ of luminosity per experiment

Work ongoing to provide final measurements using all available data

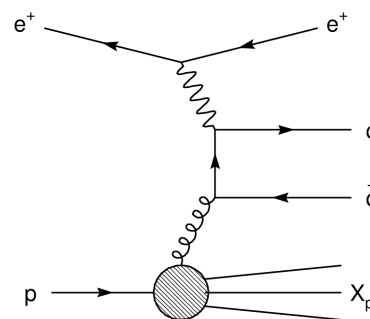


Jet production at HERA

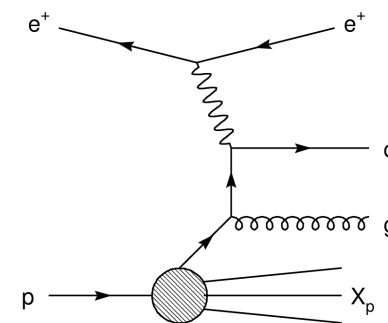
Two kinematic regions depending on the virtuality of the mediating boson Q^2 :

1. Deep Inelastic Scattering (DIS)

- ✓ $Q^2 \gg \Lambda_{QCD}$
- ✓ Two scale present, Q^2, P_T



Boson-gluon fusion



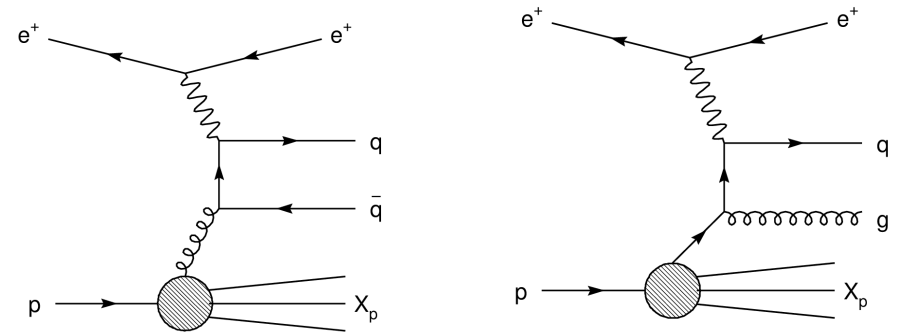
QCD Compton

Jet production at HERA

Two kinematic regions depending on the virtuality of the mediating boson Q^2 :

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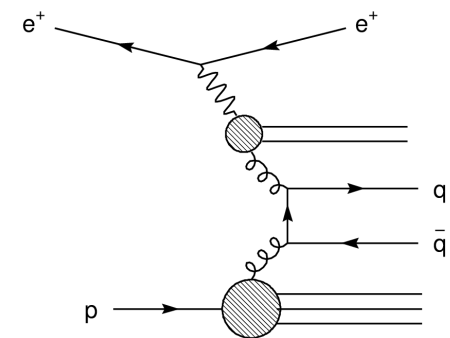


Boson-gluon fusion

QCD Compton

2. Photoproduction (PHP)

- ✓ $Q^2 \approx 0 \text{ GeV}$
- ✓ In addition to B-G fusion and QCD Compton:
Compton: Resolved photoproduction
- ✓ Similarity to hadron-hadron collisions



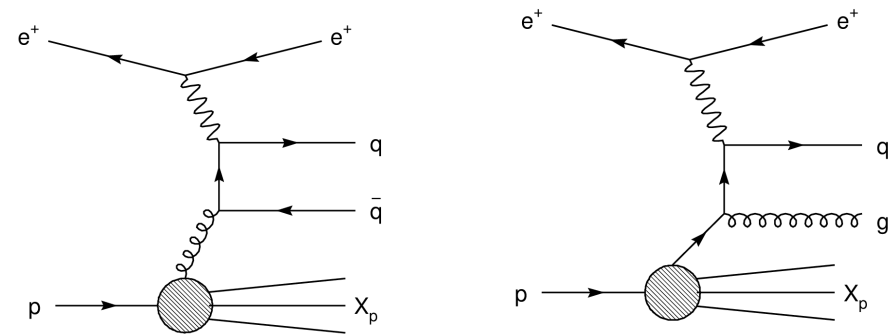
Resolved photoproduction

Jet production at HERA

Two kinematic regions depending on the virtuality of the mediating boson Q^2 :

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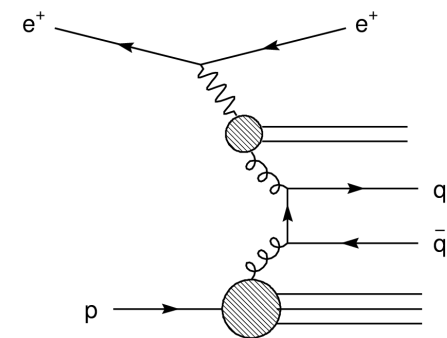


Boson-gluon fusion

QCD Compton

2. Photoproduction (PHP)

- ✓ $Q^2 \approx 0 \text{ GeV}$
- ✓ In addition to B-G fusion and QCD Compton:
Compton: Resolved photoproduction
- ✓ Similarity to hadron-hadron collisions



Resolved photoproduction

Remark: Breit frame = no QPM events

Jet physics at HERA

Jet cross section:

$$d\sigma_{jet} \sim \sum_{j=q,\bar{q},g} \int dx \underbrace{f_{j/p}(x, \mu_F)}_{\text{proton content}} \underbrace{d\hat{\sigma}_j(x, \alpha_s(\mu_R), \mu_R, \mu_F)}_{\text{pQCD matrix element}}$$

x - Bjorken x
 f - PDFs
 μ_R - renormalization scale
 μ_F - factorization scale
 α_s - strong coupling const.

Programs used to compute NLO jet cross sections:

- ✓ **DIS:** DISENT, NLOJET++
- ✓ **PHP:** Frixione-Ridolfi, Klasen-Kleinwort-Kramer

Calculations corrected for hadronization and Z^0 exchange

Theoretical uncertainty estimated by variation of the scale

Jet physics at HERA

Jet cross section:

$$d\sigma_{jet} \sim \sum_{j=q,\bar{q},g} \int dx \underbrace{f_{j/p}(x, \mu_F)}_{\text{proton content}} \underbrace{d\hat{\sigma}_j(x, \alpha_s(\mu_R), \mu_R, \mu_F)}_{\text{pQCD matrix element}}$$

x - Bjorken x
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 α_s - strong coupling const.

In the resolved case:

$$d\sigma_{jet} \sim \sum_{i,j=q,\bar{q},g} \int dx_p \int dx_\gamma \underbrace{f_{j/p}(x_p, \mu_{Fp})}_{\text{proton content}} \underbrace{f_{i/\gamma}(x_\gamma, \mu_{F\gamma})}_{\text{photon content}} \underbrace{d\hat{\sigma}_{ij}(x_p, x_\gamma, \alpha_s, \mu_R, \mu_F)}_{\text{pQCD matrix element}}$$

Jet physics at HERA

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Use of jets:

- ✓ sensitivity to the structure of both proton and photon
- ✓ extensive pQCD tests
- ✓ determination of α_s

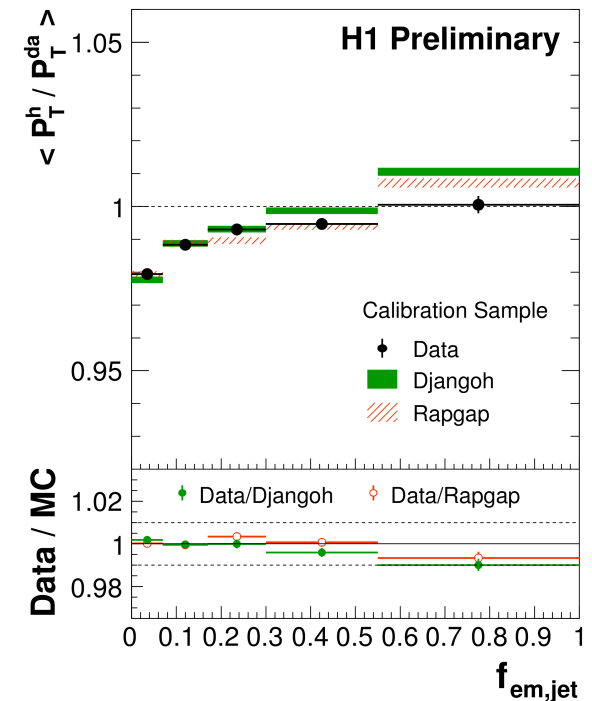
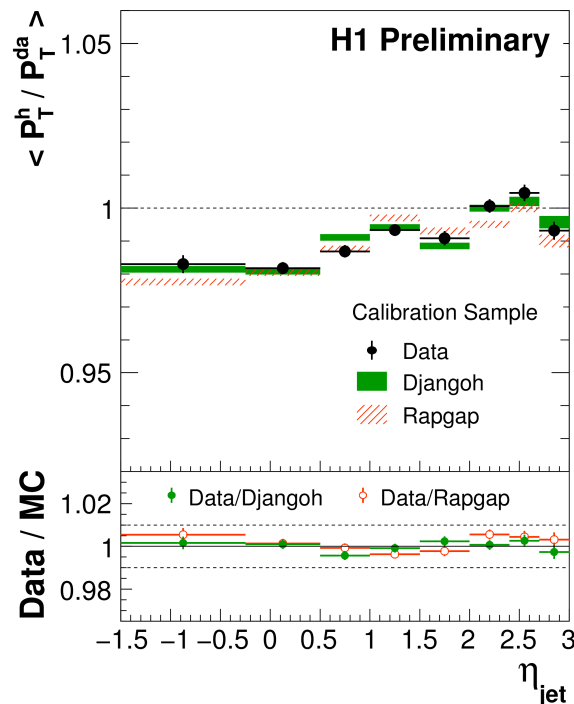
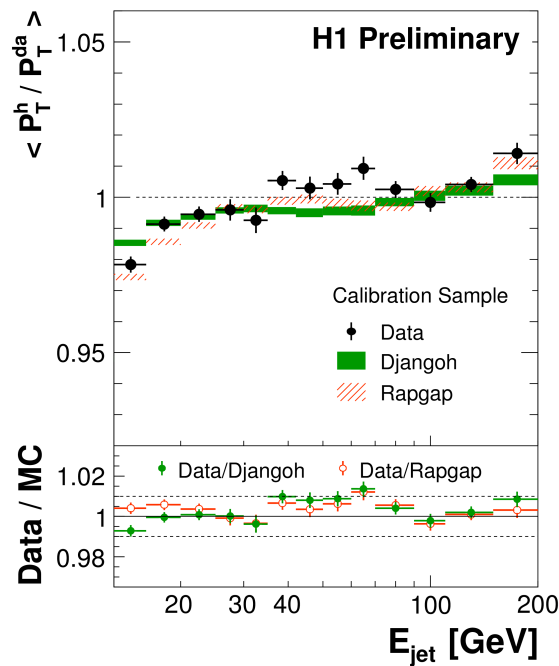


Jet calibration

High control over the jet energy scale at HERA (leading experimental uncertainty source for jet measurements)

Well measured scattered electron used to calibrate jet energy

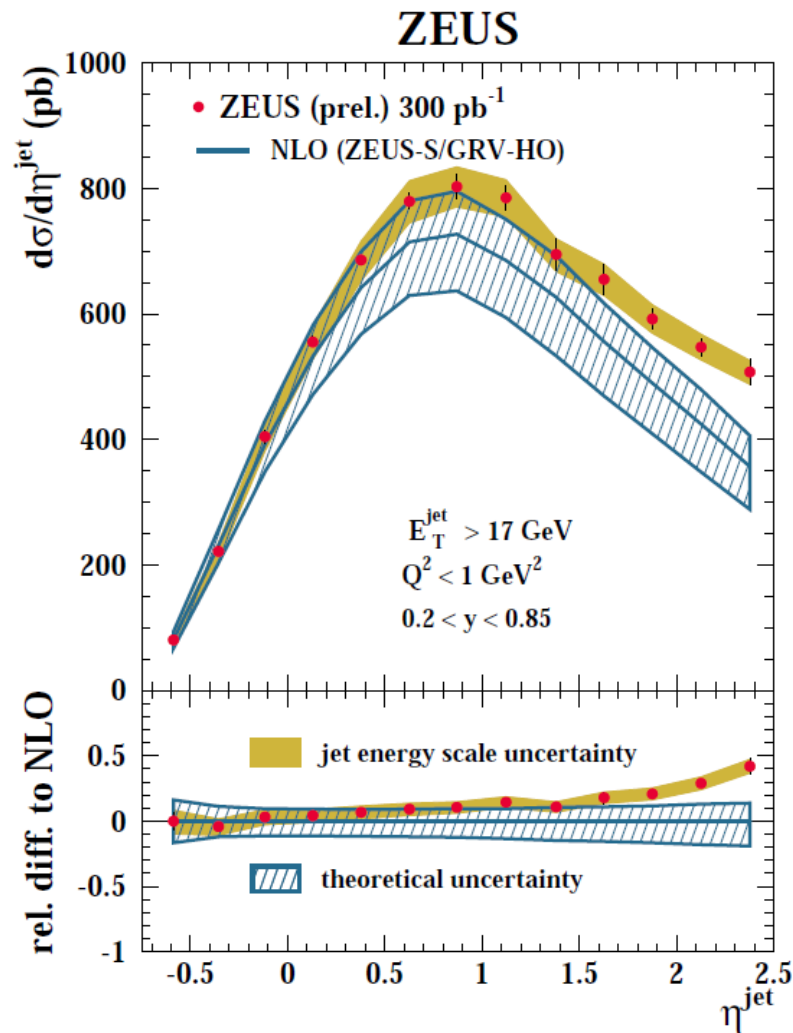
1% precision level on the jet energy scale





Jets in photoproduction

$$\begin{aligned}\mathcal{L} &= 300 \text{ pb}^{-1} \\ Q^2 &< 1 \text{ GeV}^2 \\ 0.2 &< y < 0.85 \\ P_T^{JET} &> 17 \text{ GeV} \\ -1.0 &< \eta_{lab}^{JET} < 2.5\end{aligned}$$



High statistics in photoproduction

More complex analysis (no detected electron, resolved photon, photon PDF uncertainty, etc.)

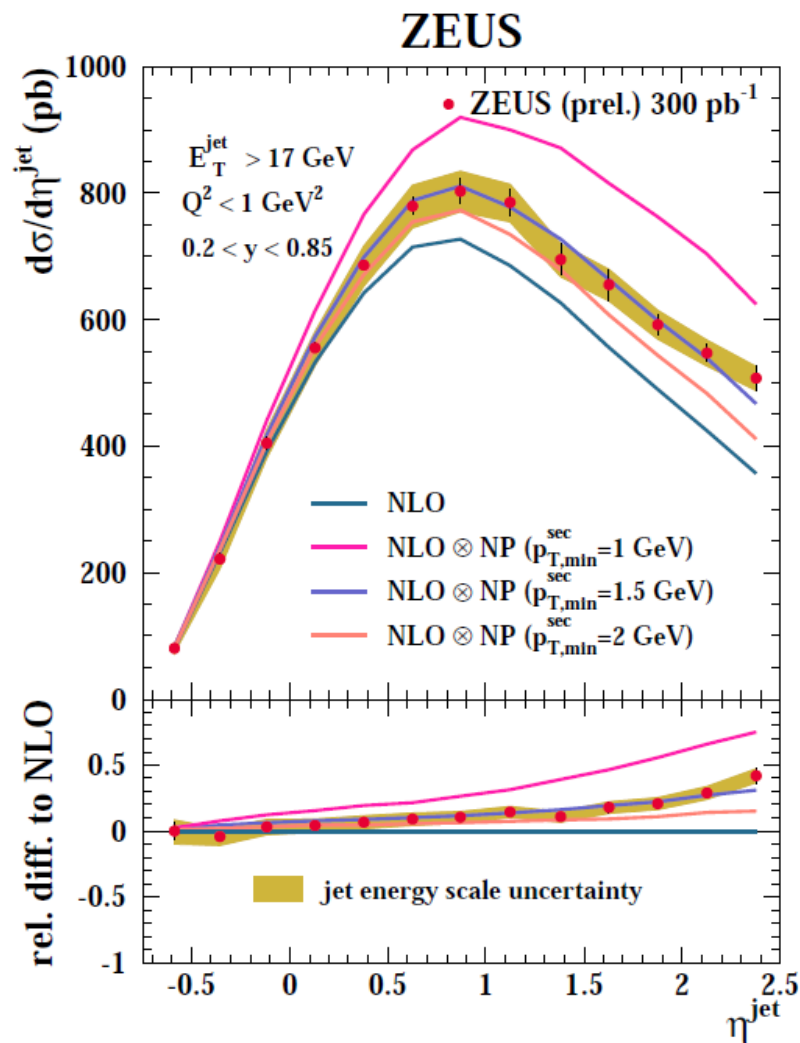
Great potential but understanding of the photon needed

Theory underestimates jet production in forward region (low P_T^{jet})



Jets in photoproduction

$$\begin{aligned} \mathcal{L} &= 300 \text{ pb}^{-1} \\ Q^2 &< 1 \text{ GeV}^2 \\ 0.2 &< y < 0.85 \\ P_T^{JET} &> 17 \text{ GeV} \\ -1.0 &< \eta_{lab}^{JET} < 2.5 \end{aligned}$$



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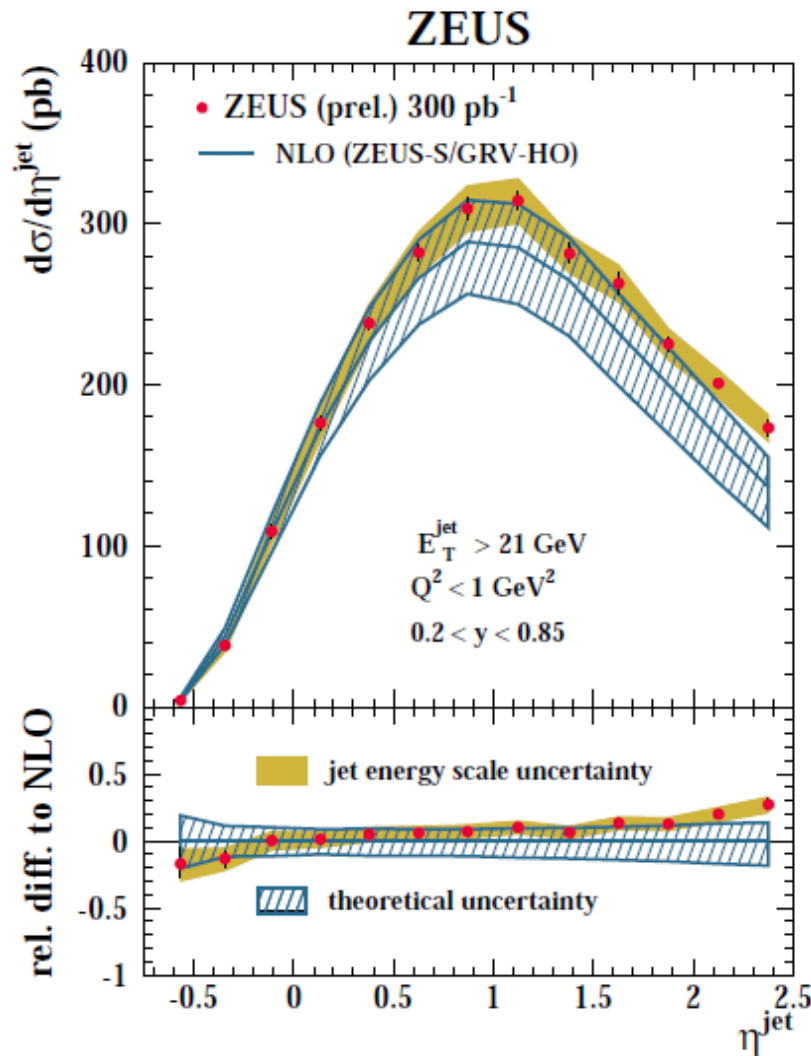
Theory underestimates jet production in forward region

Non-perturbative effects increase the jet rate in the discrepancy region



Jets in photoproduction

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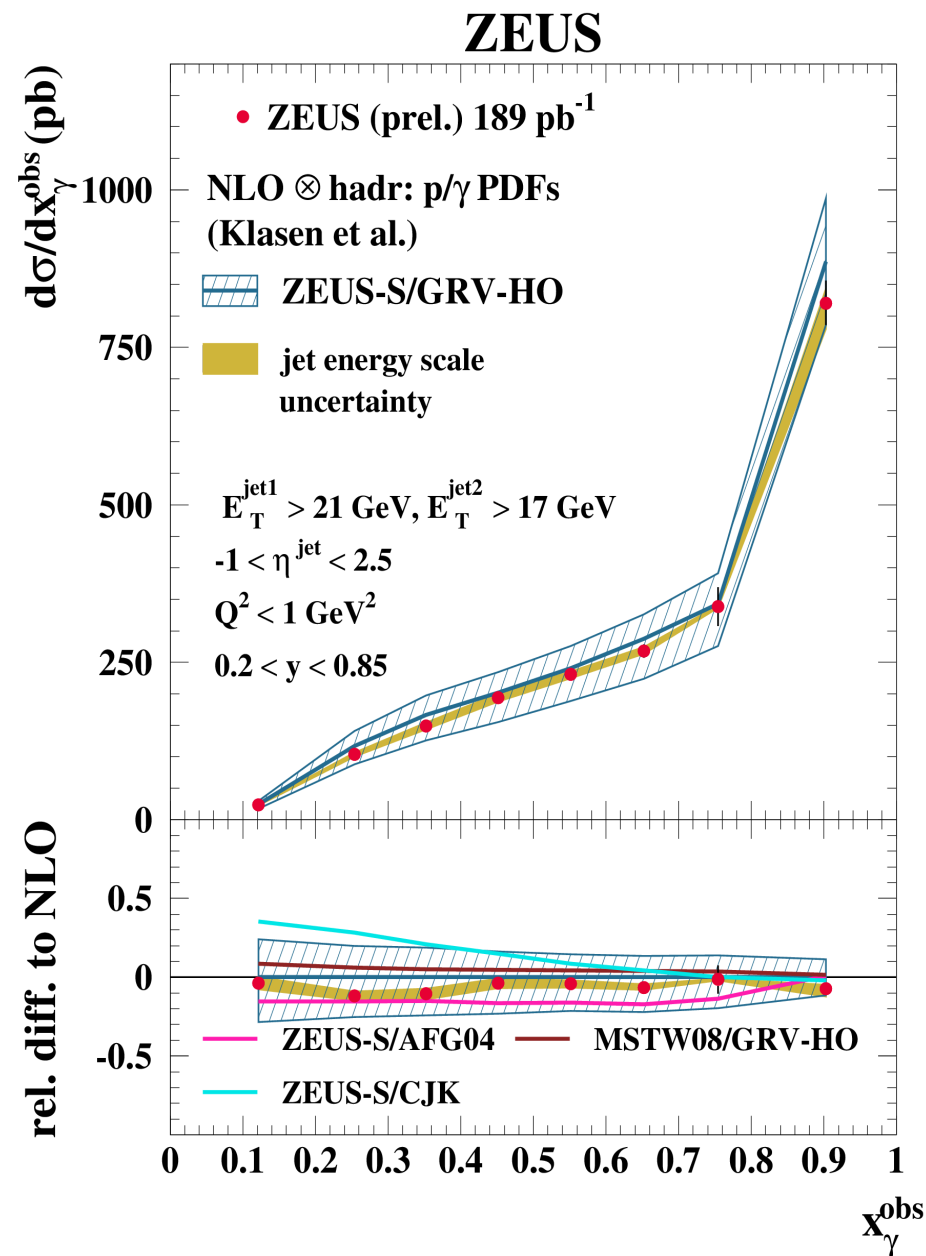
Non-perturbative effects increase the jet rate in the discrepancy region

For α_s fits P_T^{jet} restricted to described region $P_T^{\text{jet}} > 21 \text{ GeV}$



Dijets in photoproduction

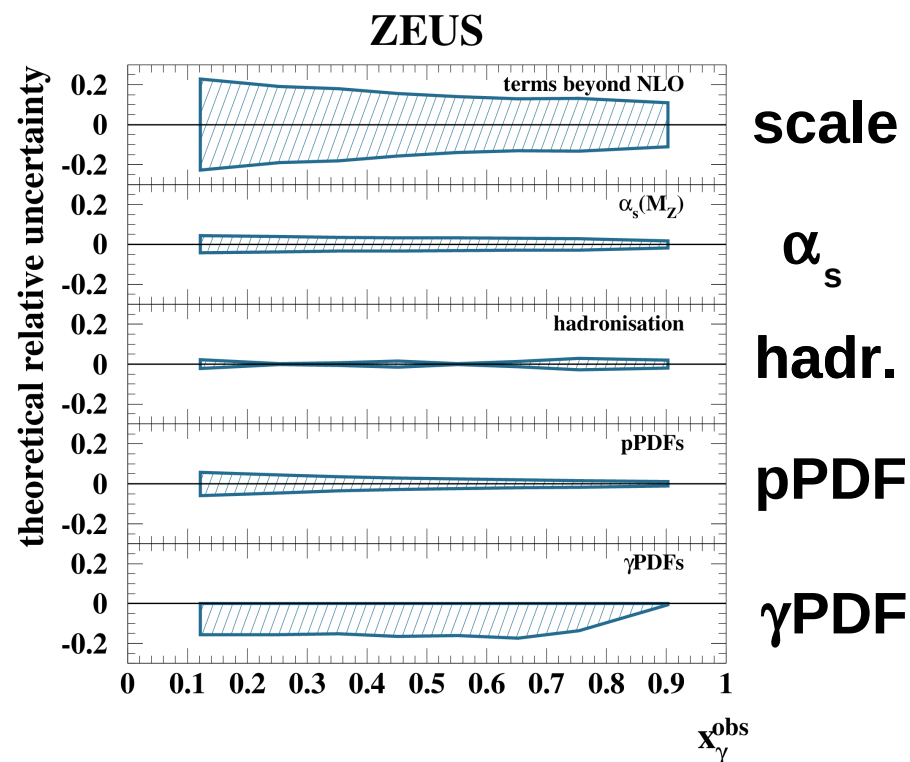
$$\begin{aligned}\mathcal{L} &= 189 \text{ pb}^{-1} \\ Q^2 &< 1 \text{ GeV}^2 \\ 0.2 &< y < 0.85 \\ P_{T,B}^{JET} &> 21 (17) \text{ GeV} \\ -1.0 &< \eta_{lab}^{JET} < 2.5\end{aligned}$$



Sensitivity to photon PDF at low x_γ^{obs}

$$x_\gamma^{\text{LO}} = (E_T^{\text{jet1}} e^{-\eta^{\text{jet1}}} + E_T^{\text{jet2}} e^{-\eta^{\text{jet2}}}) / 2yE_e$$

Large theoretical uncertainty



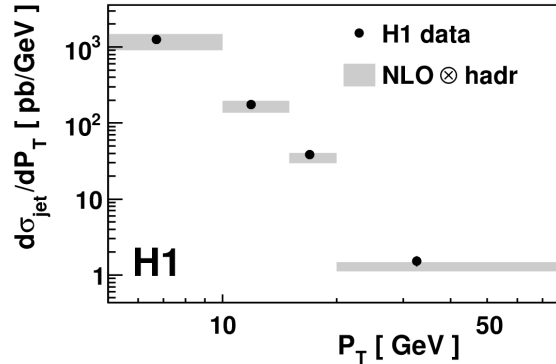
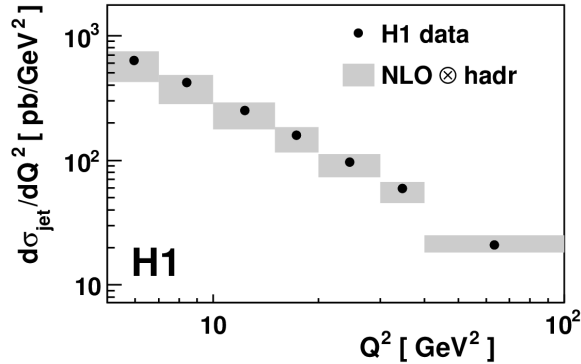


Low Q^2 DIS jets

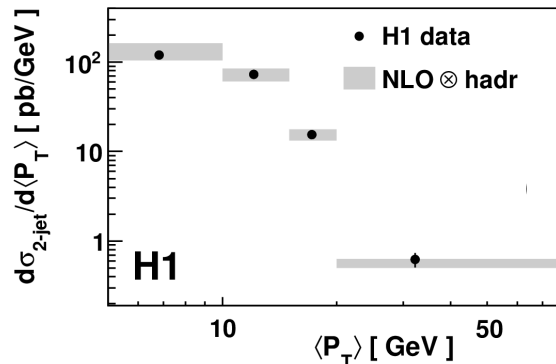
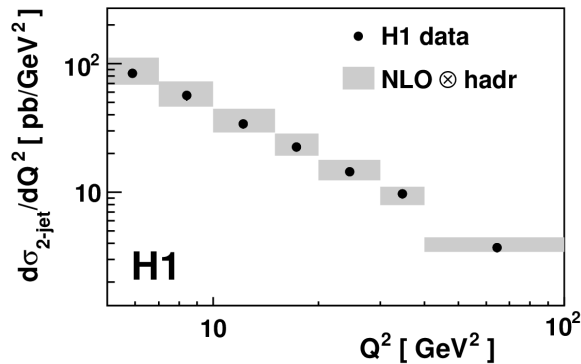
$$\begin{aligned} \mathcal{L} &= 43.5 \text{ pb}^{-1} \\ 5 < Q^2 < 100 \text{ GeV}^2 \\ 0.2 < y < 0.7 \\ P_{T,B}^{JET} &> 5 \text{ GeV} \\ -1.0 < \eta_{lab}^{JET} < 2.5 \end{aligned}$$

Inclusive Jet, 2-Jet and 3-Jet Cross Sections

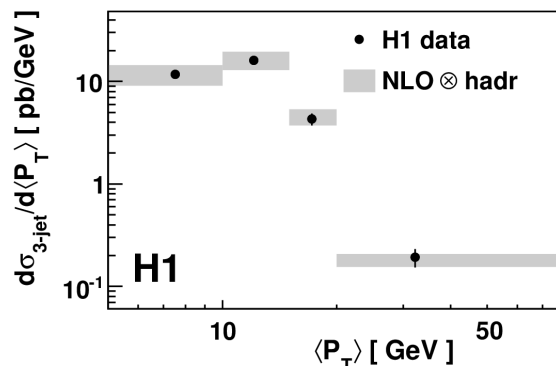
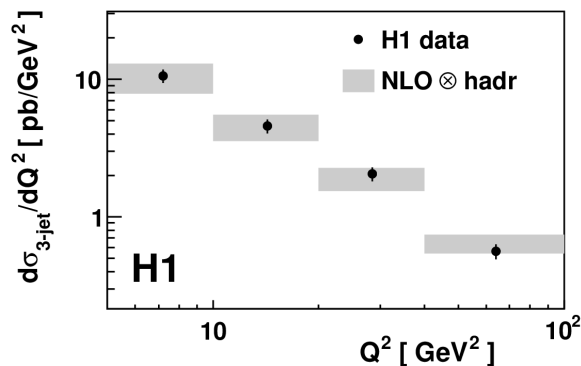
Inclusive



Dijet



Trijet



Inclusive jet and multijet cross section measured

Triggering on scat. electron – measurement lower in P_T

Large theoretical uncertainty (10-30%) especially at lower Q^2

For α_s fit using only points with $k = \sigma_{NLO} / \sigma_{LO} < 2$

$$\alpha_s = 0.1160 \pm 0.0014 (\text{exp})_{-0.079}^{+0.094} (th)$$

Measurement well described by the NLO calculation

NNLO calculation needed to take full advantage of the precise data

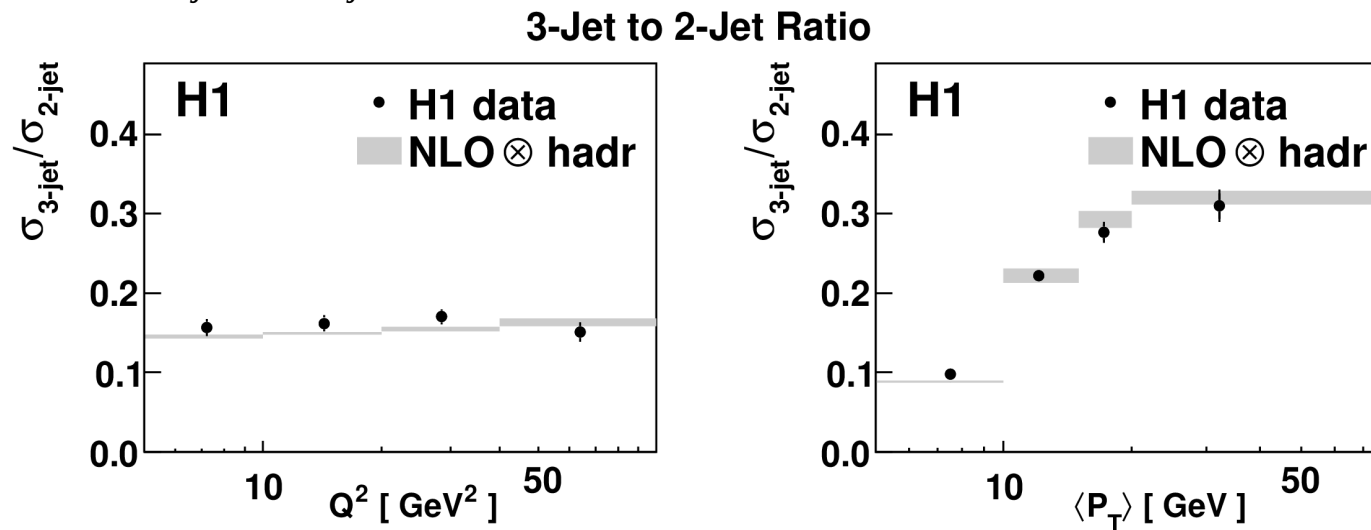


Low Q^2 DIS jets

$$\begin{aligned}\mathcal{L} &= 43.5 \text{ pb}^{-1} \\ 5 < Q^2 < 100 \text{ GeV}^2 \\ 0.2 < y < 0.7 \\ P_{T,B}^{JET} &> 5 \text{ GeV} \\ -1.0 < \eta_{lab}^{JET} < 2.5\end{aligned}$$

Improvement on the uncertainty can be achieved by measuring trijet to dijet ratio:

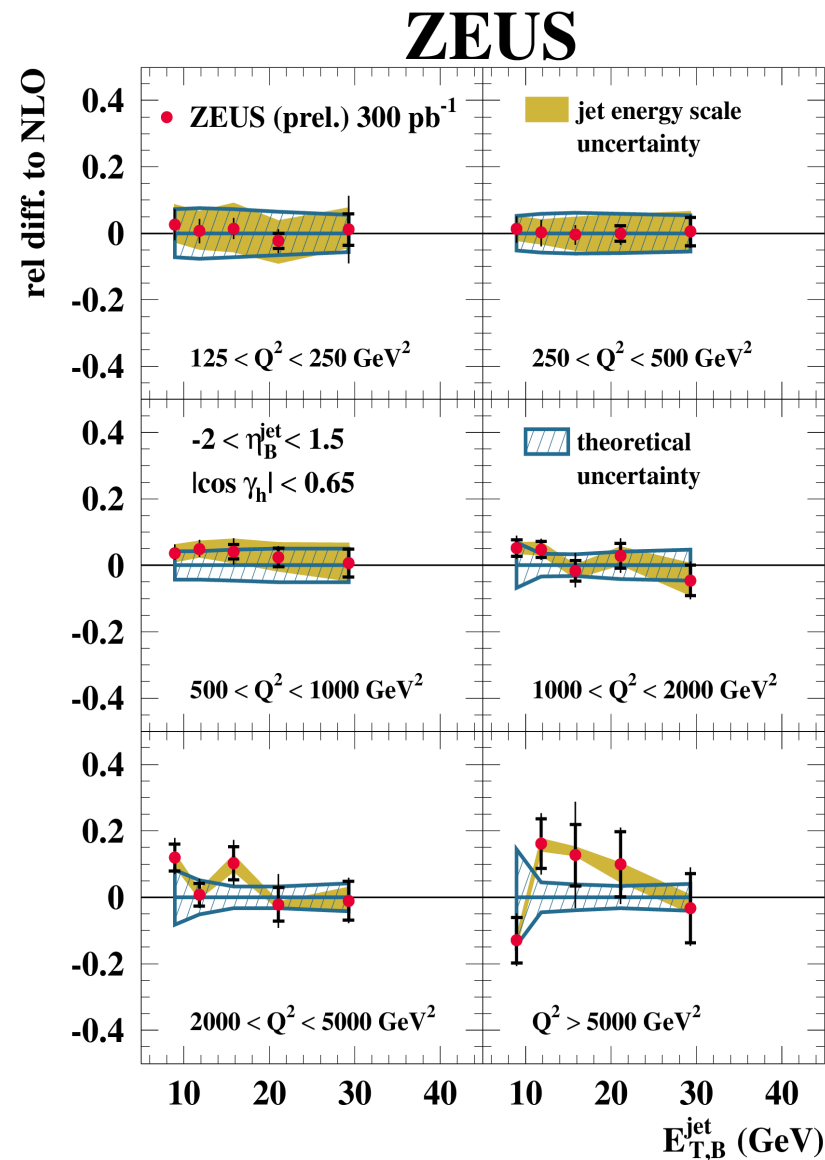
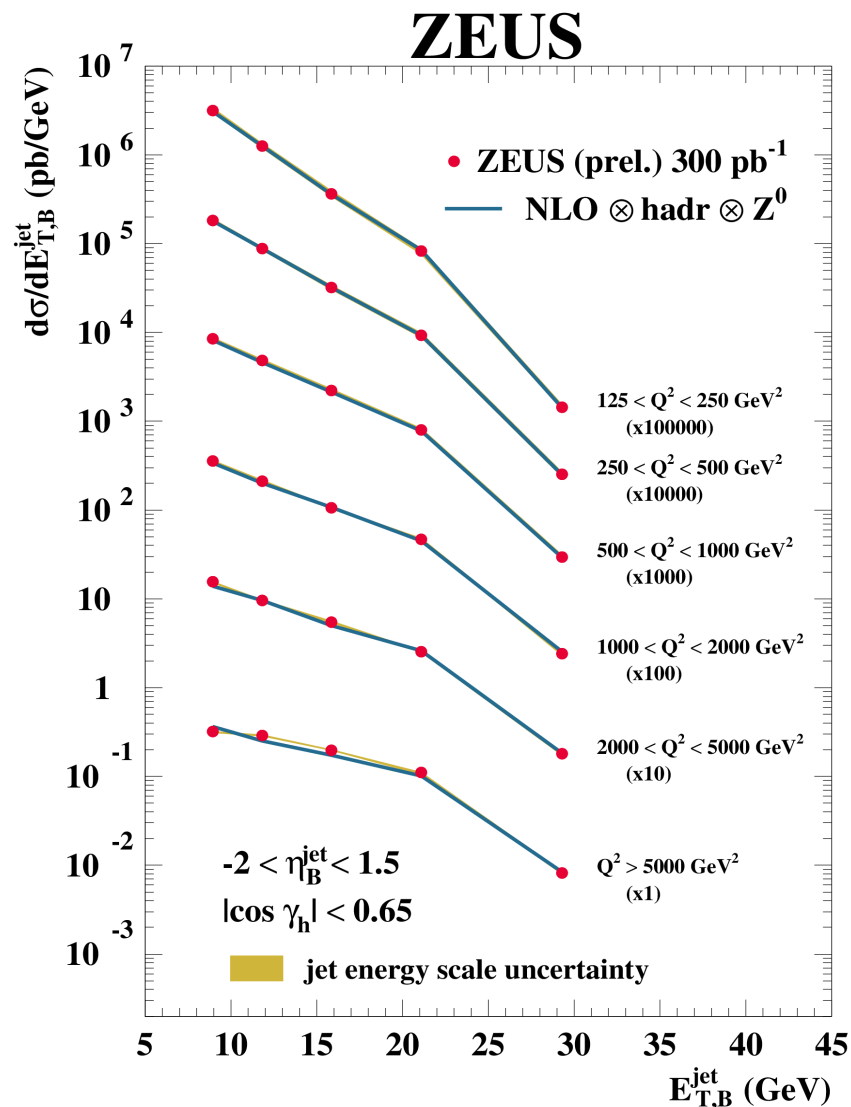
- ✓ Cancellation of some systematic uncertainties
- ✓ Strong reduction of theoretical uncertainty
- ✓ $\alpha_s \sim \sigma_{3\text{-jet}} / \sigma_{2\text{-jet}}$





High Q^2 DIS inclusive jets

$\mathcal{L} = 300 \text{ pb}^{-1}$
 $Q^2 > 125 \text{ GeV}^2$
 $|\cos \gamma_h| < 0.65$
 $P_{T,B}^{JET} > 8 \text{ GeV}$
 $-2.0 < \eta_B^{JET} < 1.5$





High Q^2 DIS inclusive jets

$$\begin{aligned} \mathcal{L} &= 300 \text{ pb}^{-1} \\ Q^2 &> 125 \text{ GeV}^2 \\ |\cos \gamma_h| &< 0.65 \\ P_{T,B}^{JET} &> 8 \text{ GeV} \\ -2.0 < \eta_B^{JET} &< 1.5 \end{aligned}$$

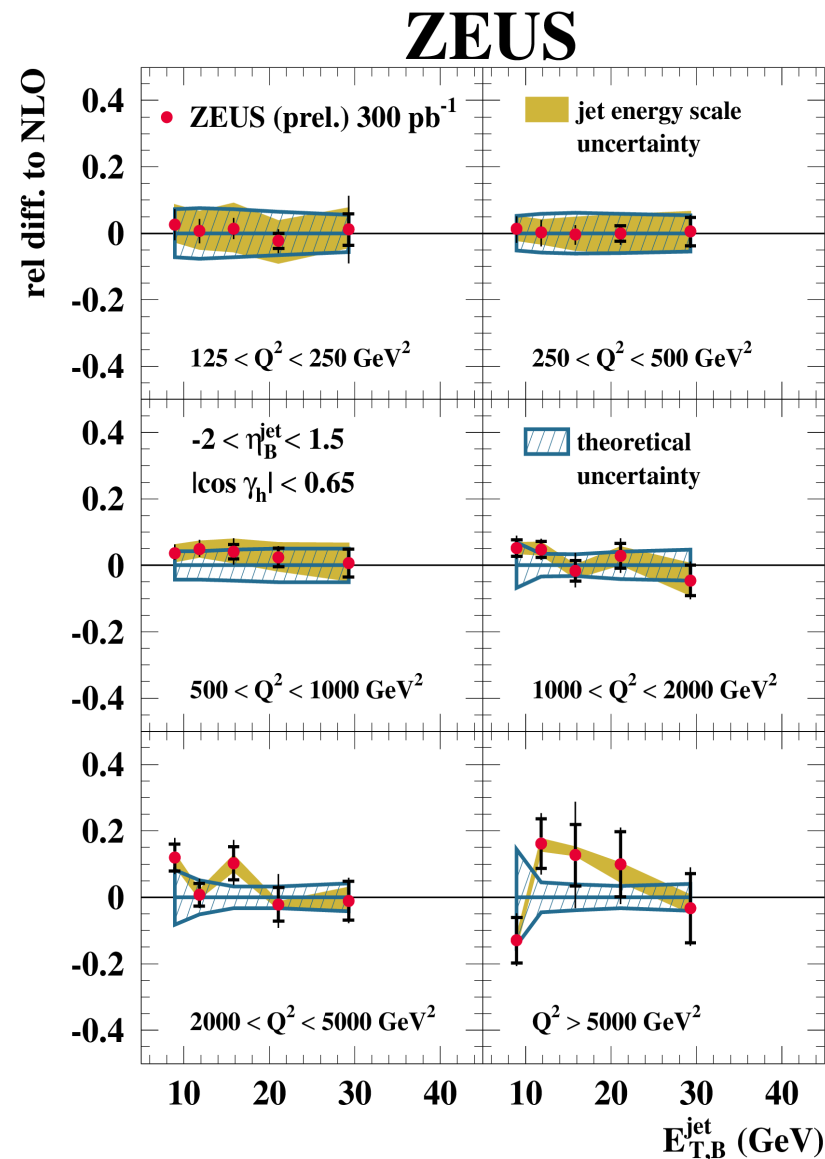
Dominant experimental error – jet energy scale

Comparably high theoretical uncertainty (estimated terms beyond NLO)

Using only points with $Q^2 > 500 \text{ GeV}^2$:

$$\alpha_s = 0.1208_{-0.0037}^{+0.0032} (exp.)_{-0.0022}^{+0.0022} (th.)$$

Measurement well described by NLO prediction

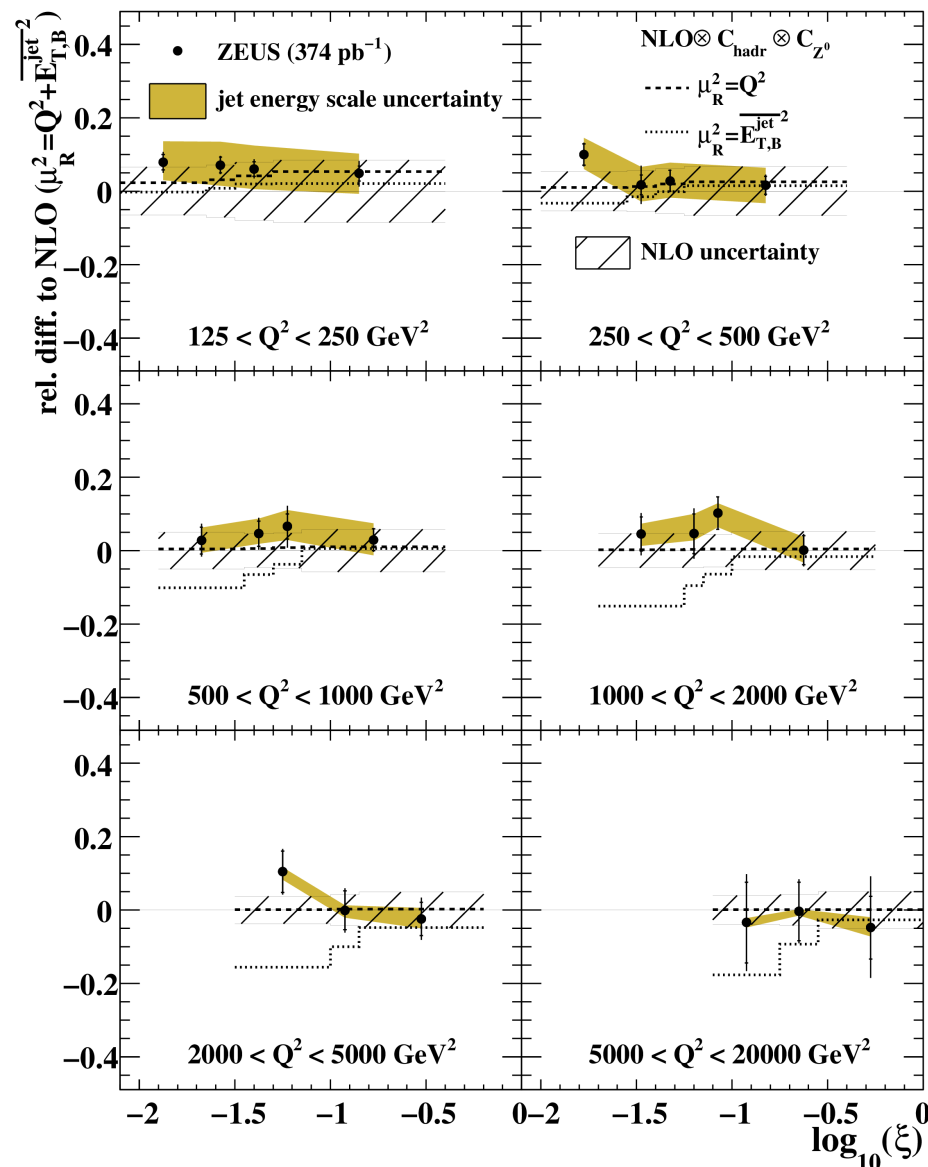




High Q^2 DIS dijets

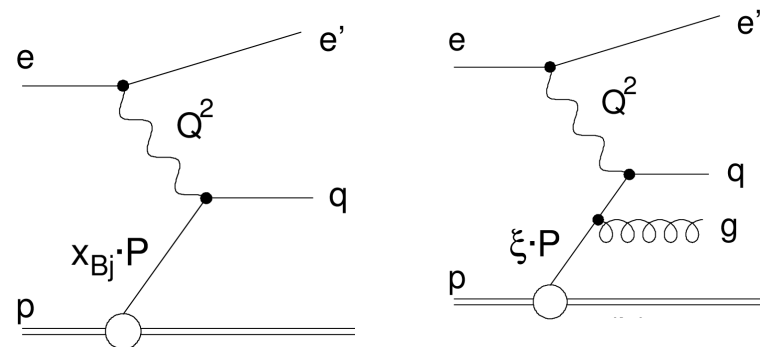
ZEUS

$$\begin{aligned} \mathcal{L} &= 374 \text{ pb}^{-1} \\ 125 < Q^2 < 20000 \text{ GeV}^2 \\ 0.2 < y < 0.6 \\ P_{T,B}^{JET} &> 8 \text{ GeV} \\ -1.0 < \eta_{lab}^{JET} < 2.5 \end{aligned}$$



Estimator of the fraction of the proton momentum taken by the interacting parton (ξ) possible

$$\xi = x_{Bj} (1 + M_{jj}^2 / Q^2)$$



Measurement sensitive to proton PDF

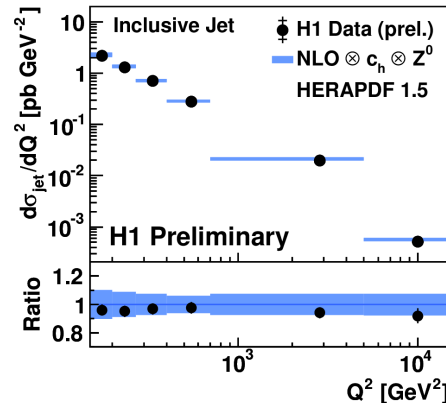
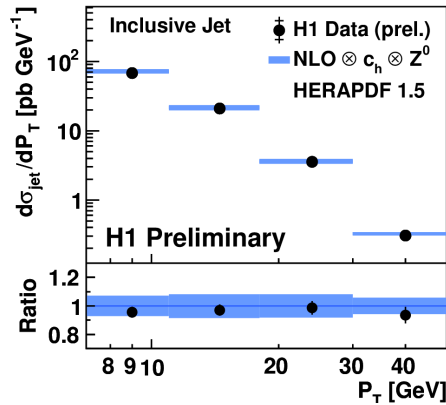
Measurement well described by the NLO calculation



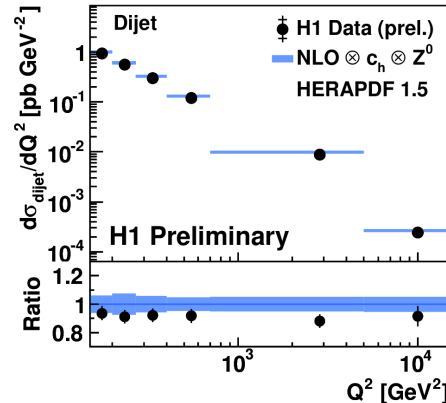
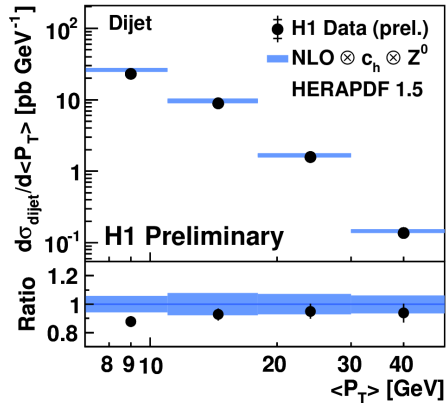
High Q^2 DIS jets

$$\begin{aligned} \mathcal{L} &= 350 \text{ pb}^{-1} \\ 150 < Q^2 < 15000 \text{ GeV}^2 \\ 0.2 < y < 0.7 \\ 7 > P_{T,B}^{JET} > 50 \text{ GeV} \\ -1.0 < \eta_{lab}^{JET} < 2.5 \end{aligned}$$

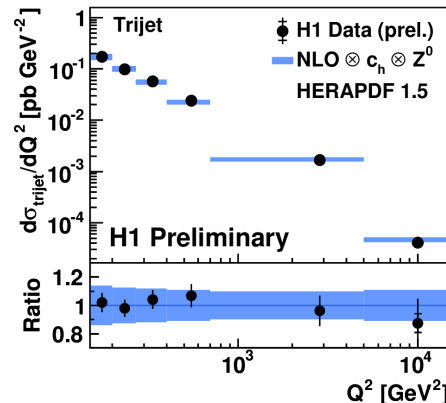
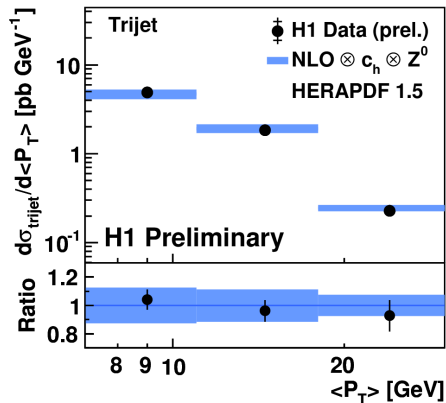
Inclusive



Dijet



Trijet



Inclusive jet, dijet and trijet cross section measured

First ever double differential trijet cross section at HERA

Measurement well described by the NLO calculation



High Q^2 DIS jets

$$\begin{aligned}\mathcal{L} &= 350 \text{pb}^{-1} \\ 150 < Q^2 < 15000 \text{ GeV}^2 \\ 0.2 < y < 0.7 \\ 7 > P_{T,B}^{JET} > 50 \text{ GeV} \\ -1.0 < \eta_{lab}^{JET} < 2.5\end{aligned}$$

Strong coupling constant determined using inclusive jet, dijet and trijet cross sections independently:

Inclusive jets:

$$\alpha_s(M_Z) = 0.1190 \pm 0.0021(\text{exp.}) \pm 0.0020(\text{pdf})_{-0.0056}^{+0.0050}(\text{th.})$$

Dijets:

$$\alpha_s(M_Z) = 0.1146 \pm 0.0022(\text{exp.}) \pm 0.0021(\text{pdf})_{-0.0045}^{+0.0044}(\text{th.})$$

Trijets:

$$\alpha_s(M_Z) = 0.1196 \pm 0.0016(\text{exp.}) \pm 0.0010(\text{pdf})_{-0.0039}^{+0.0055}(\text{th.})$$

Theoretical uncertainty dominates

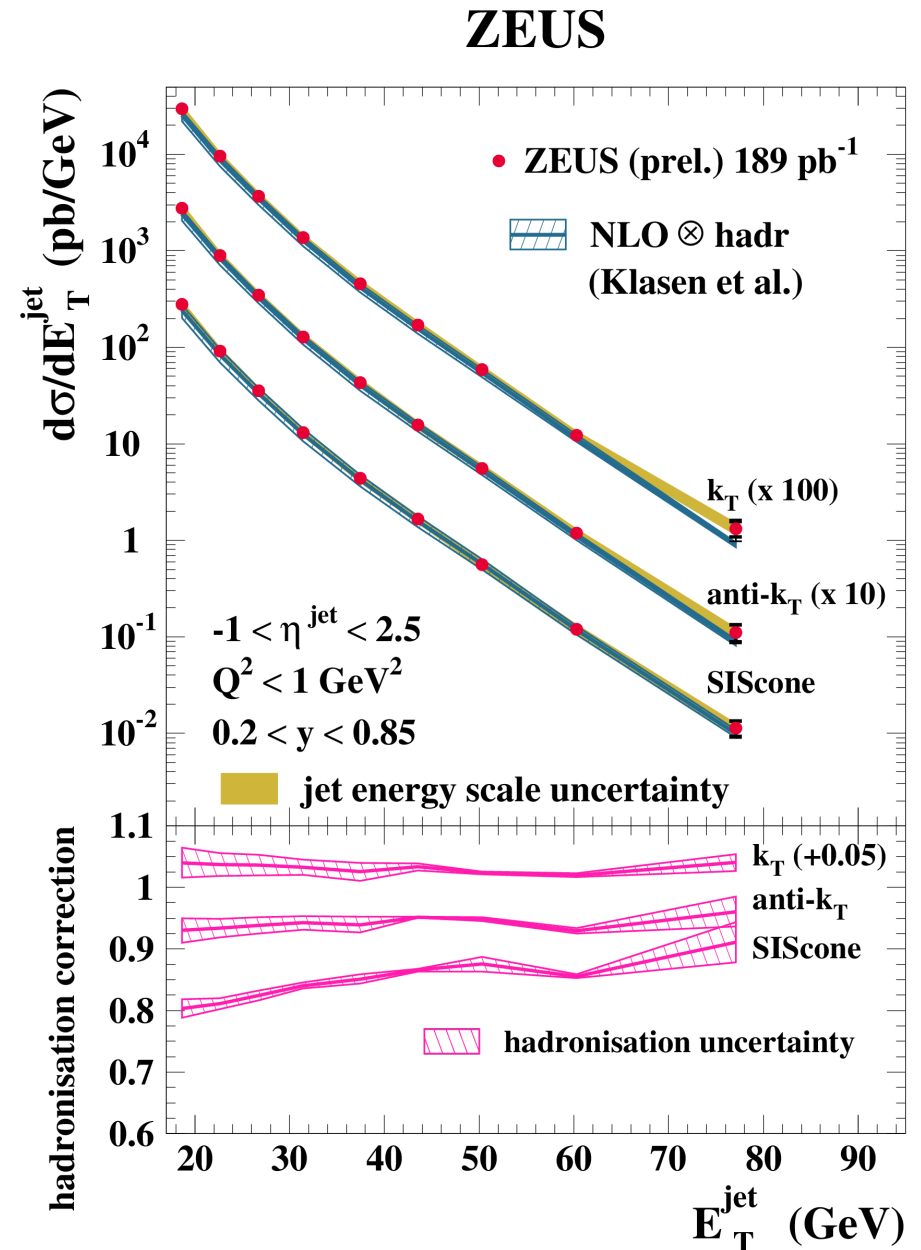
Trijet cross sections give experimentally the most precise result



Jet algorithms comparison

Performance test for new algorithms developed for LHC (anti- k_T , SIScone) using DIS and PHP data (here PHP)

- ✓ k_T and anti- k_T exhibit similar performance
- ✓ SIScone hadronization correction somewhat higher

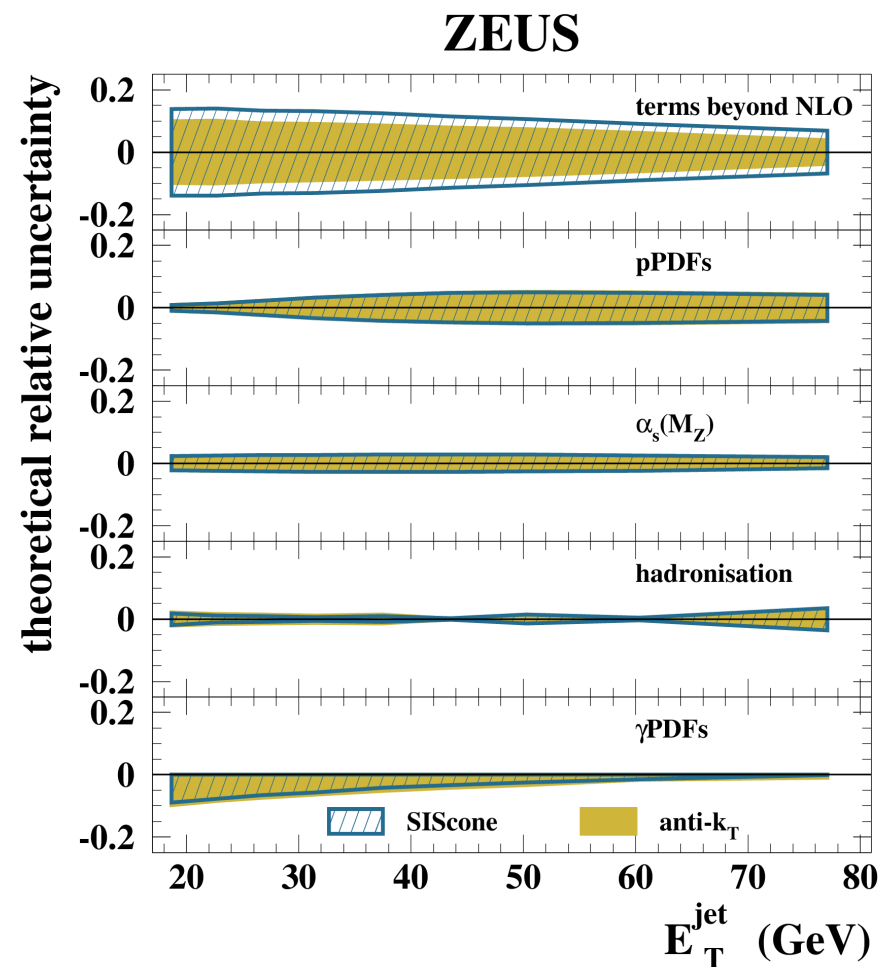




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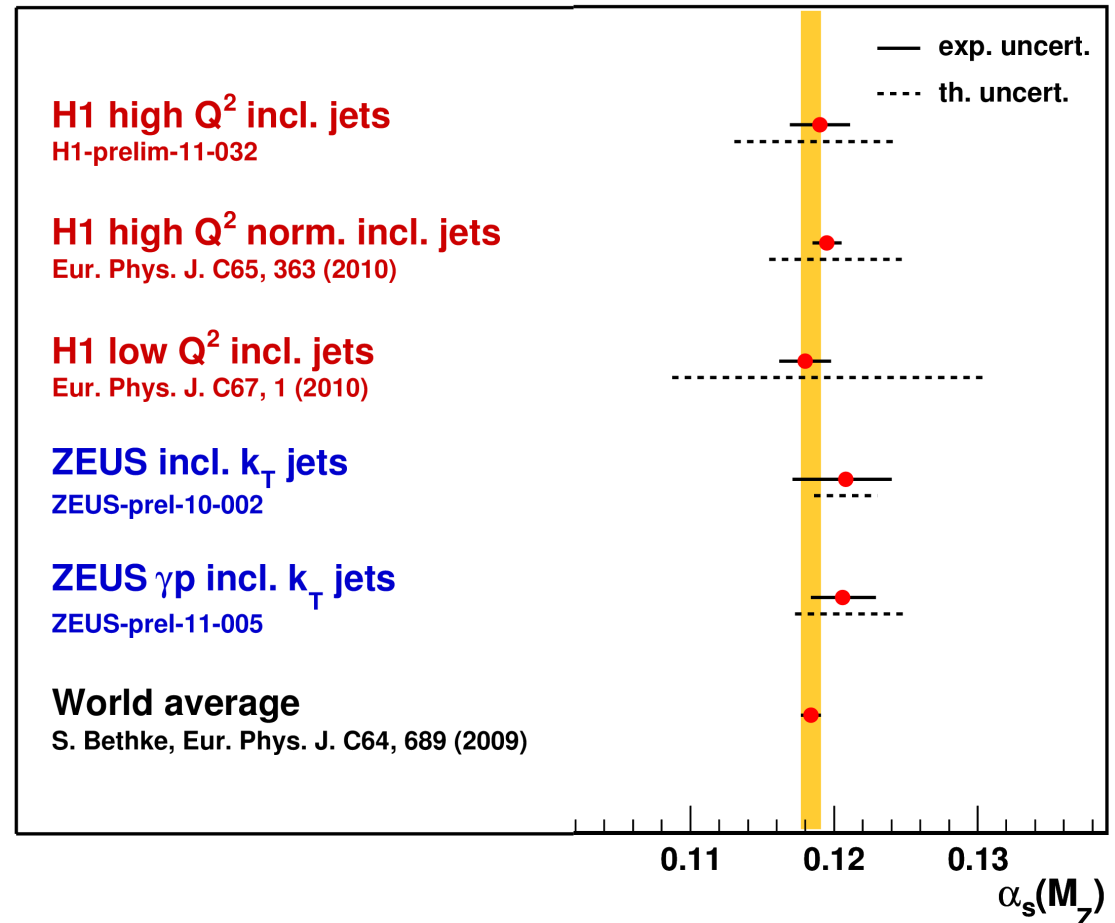
- ✓ k_T and anti- k_T exhibit similar performance
- ✓ SIScone hadronization correction somewhat higher
- ✓ SIScone beyond NLO uncertainty slightly higher



Determination of α_s

Both experiments use their data to determine the strong coupling constant $\alpha_s(M_Z)$

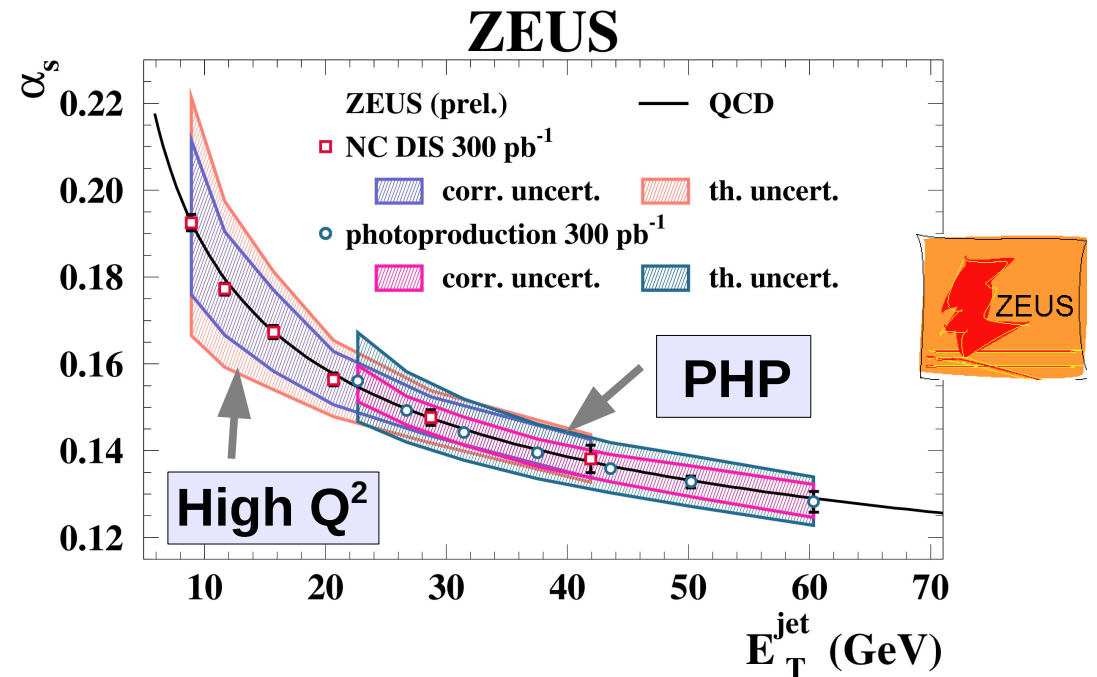
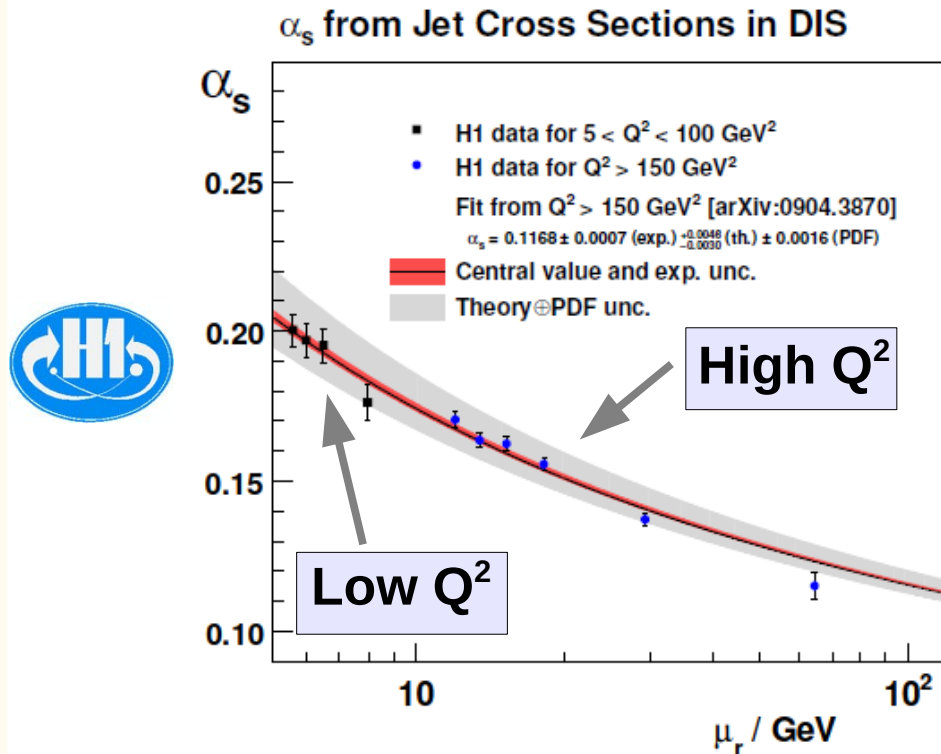
All determined couplings consistent with the world average



NNLO calculations needed to take advantage of the available experimental precision!

Running of α_s test

Both experiments perform tests of the running of the α_s



Tests show high level of consistency in our understanding of QCD

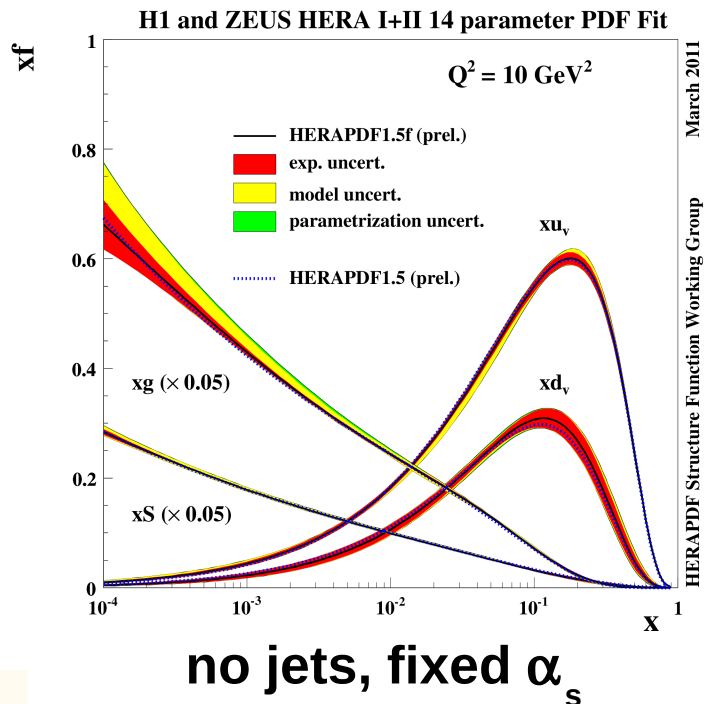


Simultaneous PDF and α_s fit

HERA QCD analysis (talk by E. Rizvi) determine proton PDF using fixed α_s

HERA jet measurements determine α_s using PDF determined elsewhere

Inclusion of inclusive jet data into QCD analysis and simultaneous fit of the $\alpha_s(M_Z)$ and PDFs



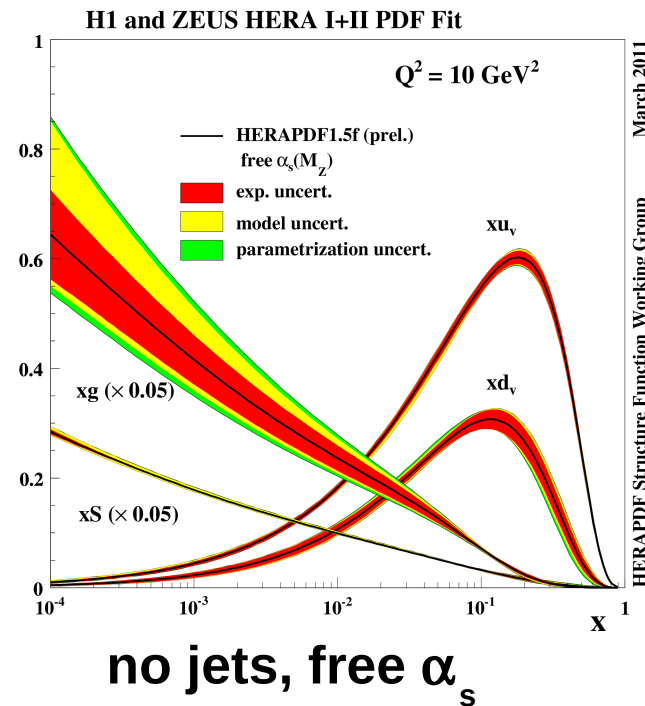
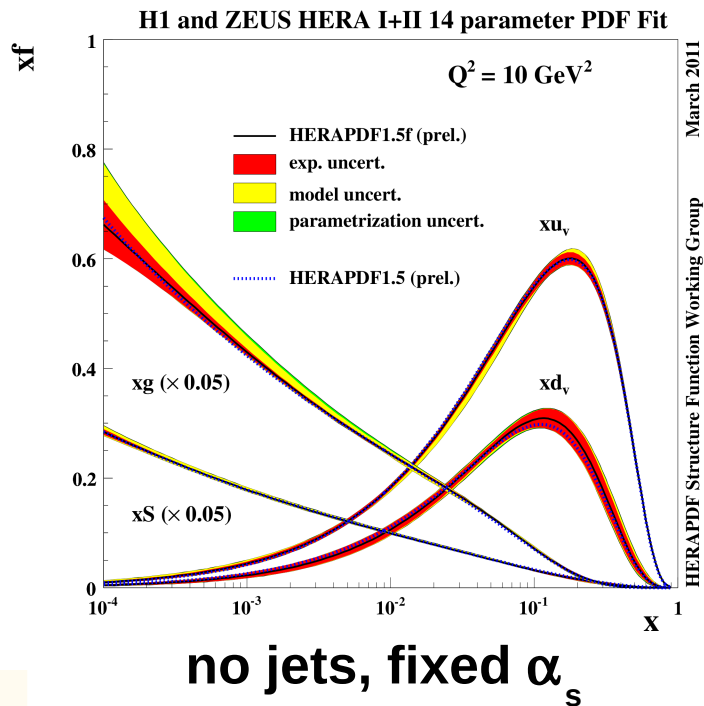


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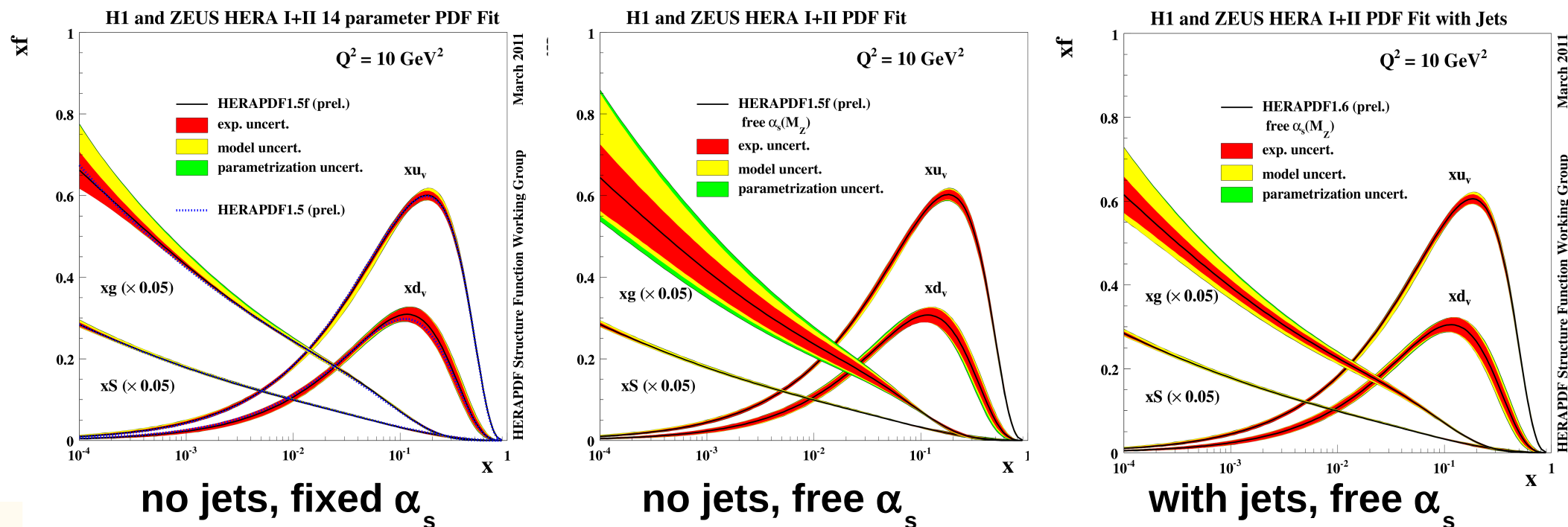


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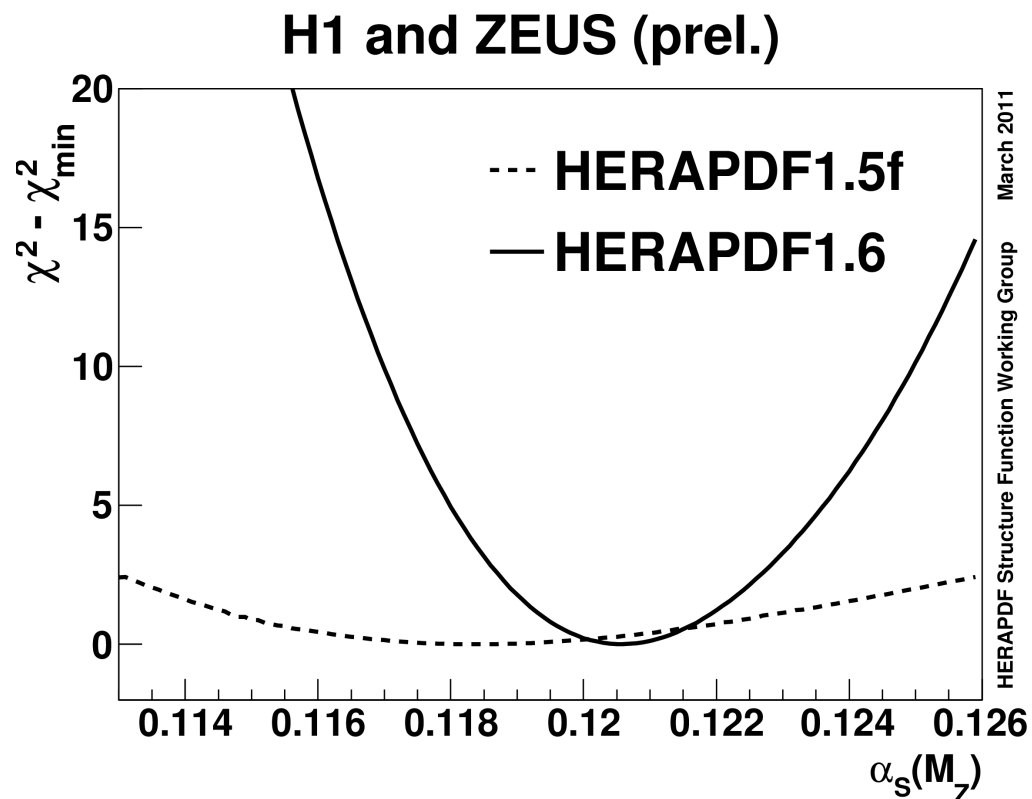
Inclusion of inclusive jet data into QCD analysis and simultaneous fit of the $\alpha_s(M_Z)$ and PDFs



Jet data needed to disentangle gluon and α_s



Simultaneous PDF and α_s fit



*Without jet data (HERAPDF1.5f)
 χ^2 scan exhibits very shallow
minimum*

*With jets (HERAPDF1.6) narrow
minimum of the χ^2 scan*

*HERA jet data sufficient to
determine the strong coupling
constant:*

$$\alpha_s = 0.1202 \pm 0.0013 (exp) \\ \pm 0.0007 (mod/par) \\ \pm 0.0012 (hadr) \\ +0.0045 \\ -0.0036 (scale)$$

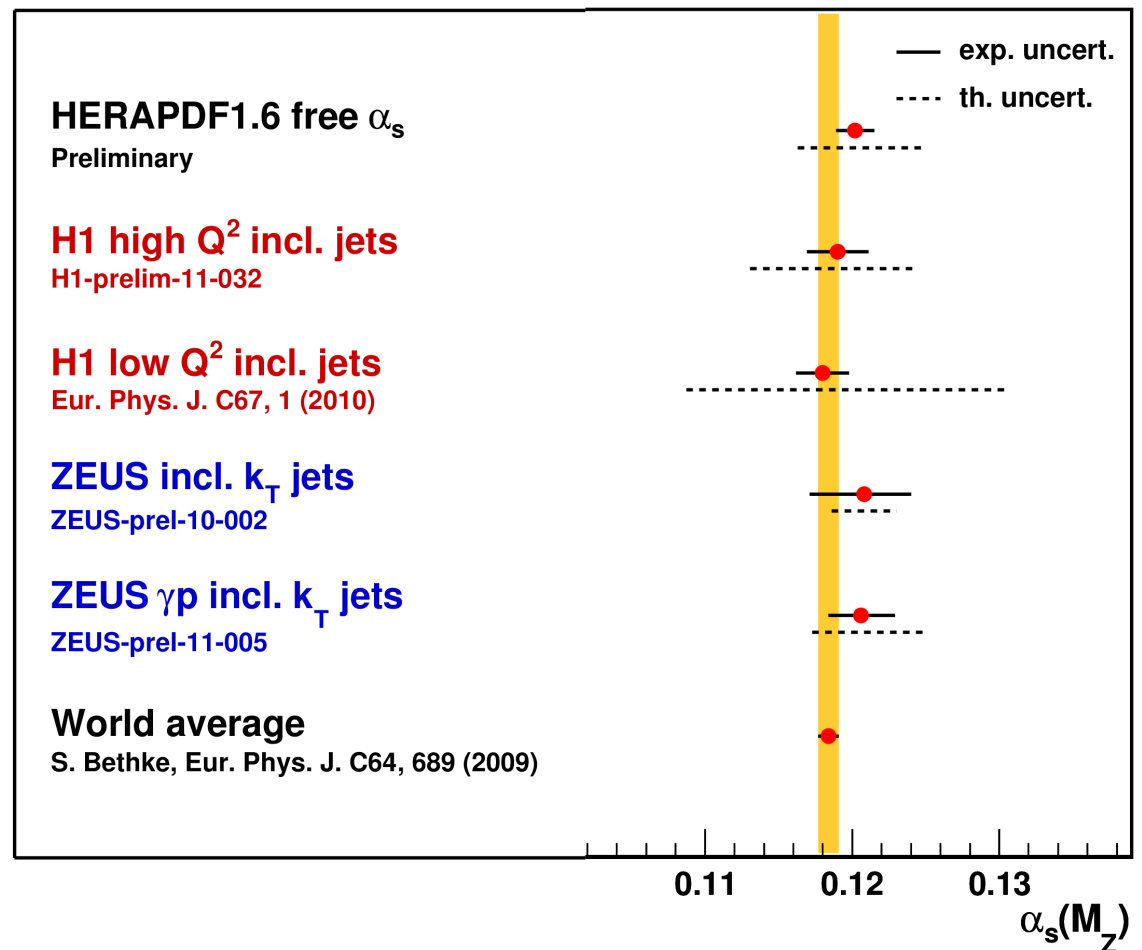
*Similarly to the situation before, the α_s
precision limited by the theoretical
uncertainty*

Determination of α_s

Fit is not using the most recent preliminary jet results

Only inclusive jet data used

Obtained $\alpha_s(M_Z)$ compatible with world average and has already competitive precision



Conclusions

Jet measurements from HERA

- ✓ *important for understanding of QCD*
- ✓ *possibly sensitive to non-perturbative effects*
- ✓ *allowing precise determination of strong coupling constant $\alpha_s(M_Z)$*
- ✓ *test of the running of α_s over wide range of the scale*





High Q^2 DIS normalized jets

$$\mathcal{L} = 395 \text{ pb}^{-1}$$

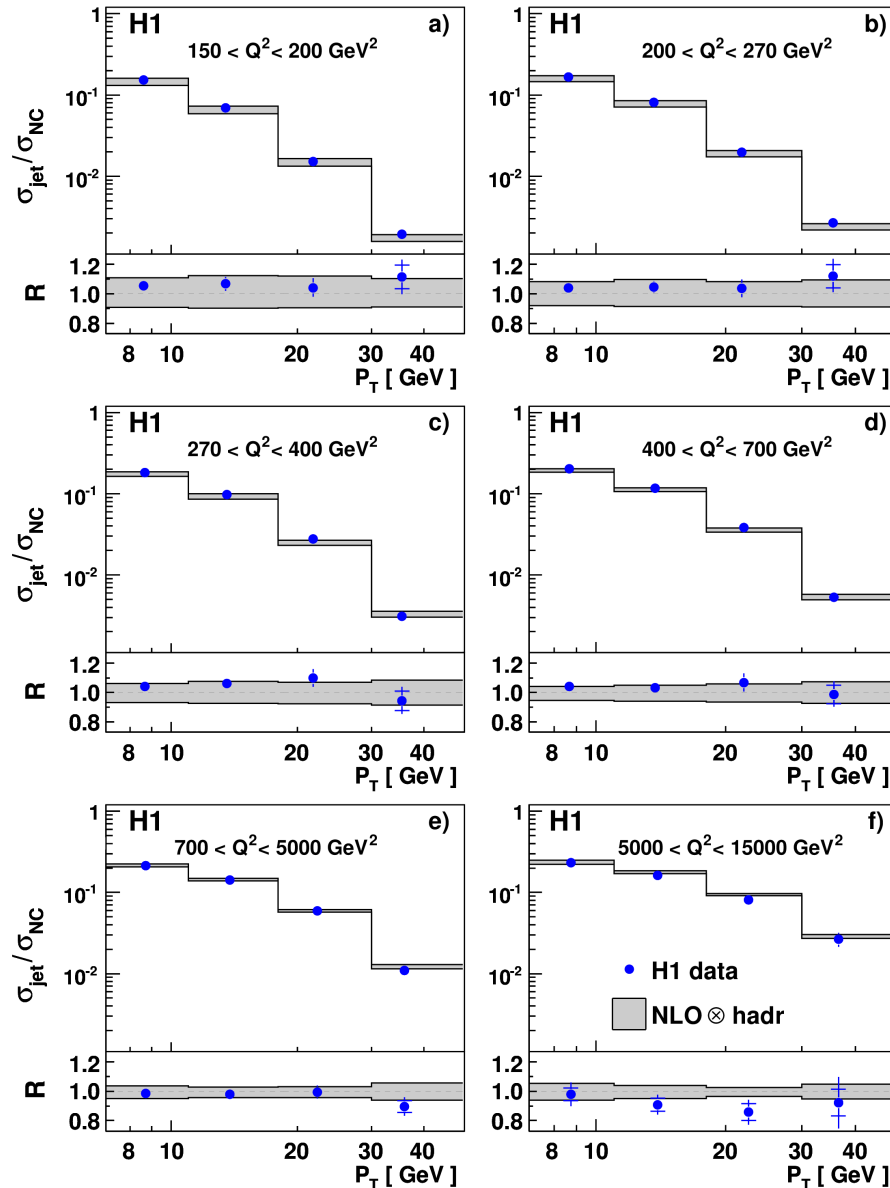
$$150 < Q^2 < 15000 \text{ GeV}^2$$

$$0.2 < y < 0.7$$

$$7(5) < P_T^{JET} < 50 \text{ GeV}$$

$$-0.8 < \eta^{JET} < 2.0$$

Normalised Inclusive Jet Cross Section



Inclusive, dijets and trijets cross sections normalized to inclusive DIS cross sections

Normalization allows to decrease experimental error

Theory error dominating, mostly renormalization scale uncertainty (up to 30%) - NNLO needed

Data well described by NLO calculations (DISENT, NLOJET++, FastNLO)