

# Precision QCD (jets and $\alpha_s$ ) measurements at HERA

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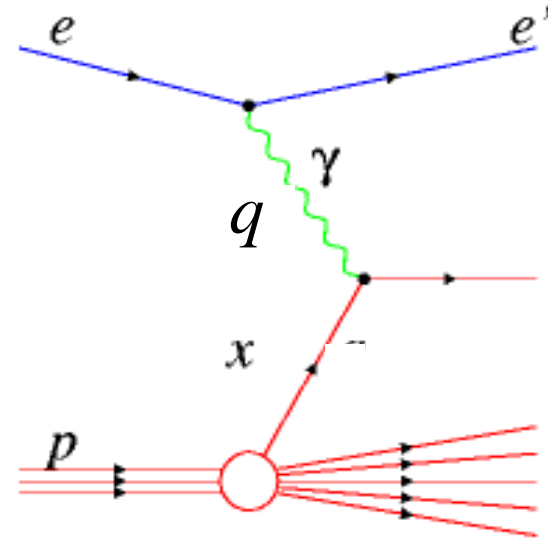
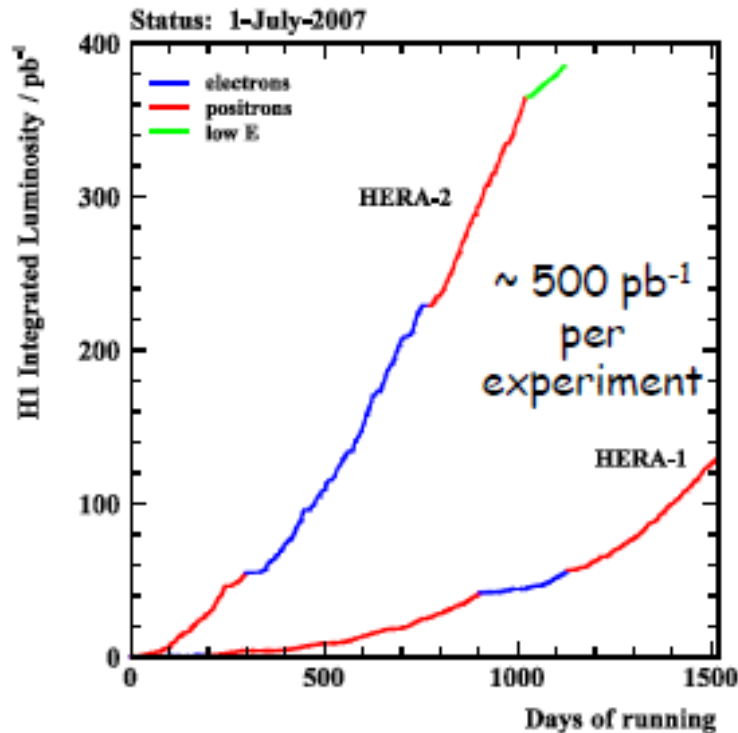
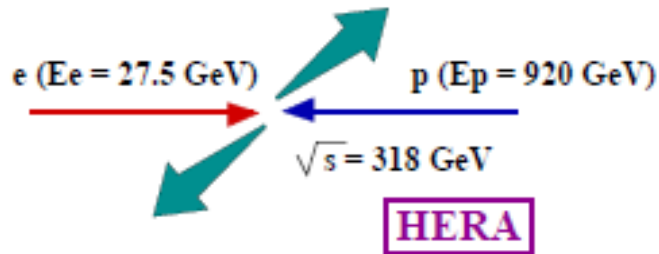


On behalf of H1 and ZEUS Collaborations



- Jet measurements at HERA
- Multijet measurement in DIS – unfolding
- Jet measurement in photoproduction
- Extraction of  $\alpha_s$  : H1 and ZEUS methods
- Comparison of the extracted values of  $\alpha_s$
- Summary

# ep – scattering at HERA



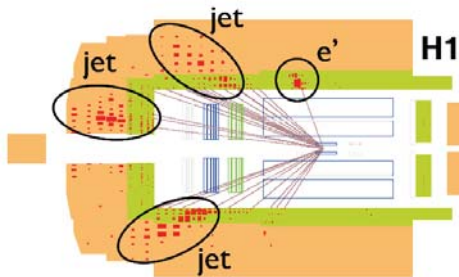
$Q^2 = -q^2$  exchanged boson virtuality  
 $x$  Bjorken scaling variable

## Two kinematic regimes:

- $Q^2 \approx 0 \text{ GeV}^2$  : Photoproduction
- $Q^2 > 1 \text{ GeV}^2$  : DIS

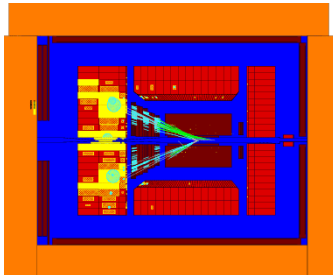
# Precision jet measurements at HERA

□ Data sets 300 – 500 pb<sup>-1</sup> → High statistics → small statistical uncertainties even at high Q<sup>2</sup> and high jet transverse momentum



**H1 DIS multijets:**  
**≈ 104000 events**

$$\begin{aligned} 150 < Q^2 < 15000 \text{ GeV}^2 \\ 0.2 < y < 0.7 \\ -1 < \eta_{\text{lab}} < 2.5 \\ 5(7) < p_T < 50 \text{ GeV} \end{aligned}$$



**ZEUS photoproduction**  
**≈ 450000 events**

$$\begin{aligned} &\bullet Q^2 < 1 \text{ GeV}^2 \\ &\bullet 0.2 < y_{\text{JB}} < 0.85 \\ &\bullet E_T > 17 \text{ GeV} \\ &\bullet -1 < \eta^{\text{jet}} < 2.5 \end{aligned}$$

□ Excellent control of systematic uncertainties

- Electron measurement : 0.5 – 1% scale uncertainty
- **Jet energy scale : 1% !** (effect on jet cross section 3-10 %)

# Jets: key to precise determination of $\alpha_s$

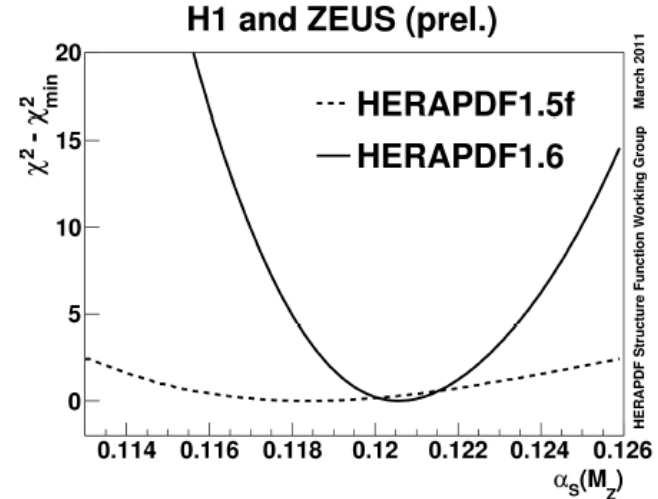
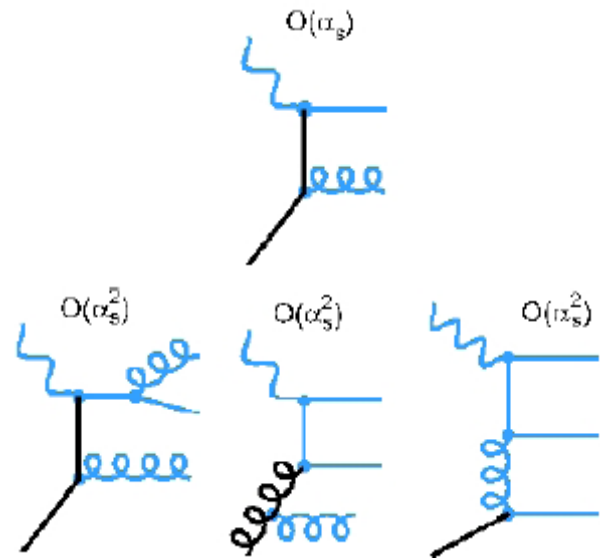
Breit frame inclusive jet cross section proportional to  $\alpha_s$  in LO. Its inclusion to global QCD fit (HERAPDF1.5  $\rightarrow$  1.6) increases immensely sensitivity to  $\alpha_s(M_Z)$

BGF: strong correlation  $\alpha_s$  – gluon density



Due to high statistics of events with  $Q^2 > 1000$  GeV and increased sensitivity to QCDC (valence quark distributions) gluon –  $\alpha_s$  correlation diminished

Trijets:  $\alpha_s^2$  term in LO diminishes experimental uncertainty in extraction of  $\alpha_s(M_Z)$



# Multijet measurements - unfolding

- ❑ Detector resolution introduces migrations between jet samples
- ❑ Correlations between samples ex definitione: inclusive dijet (trijet) is a subsample of inclusive jet (dijet)...

**m** - measured distribution at the detector level

**x** - true particle level

**A** – detector response



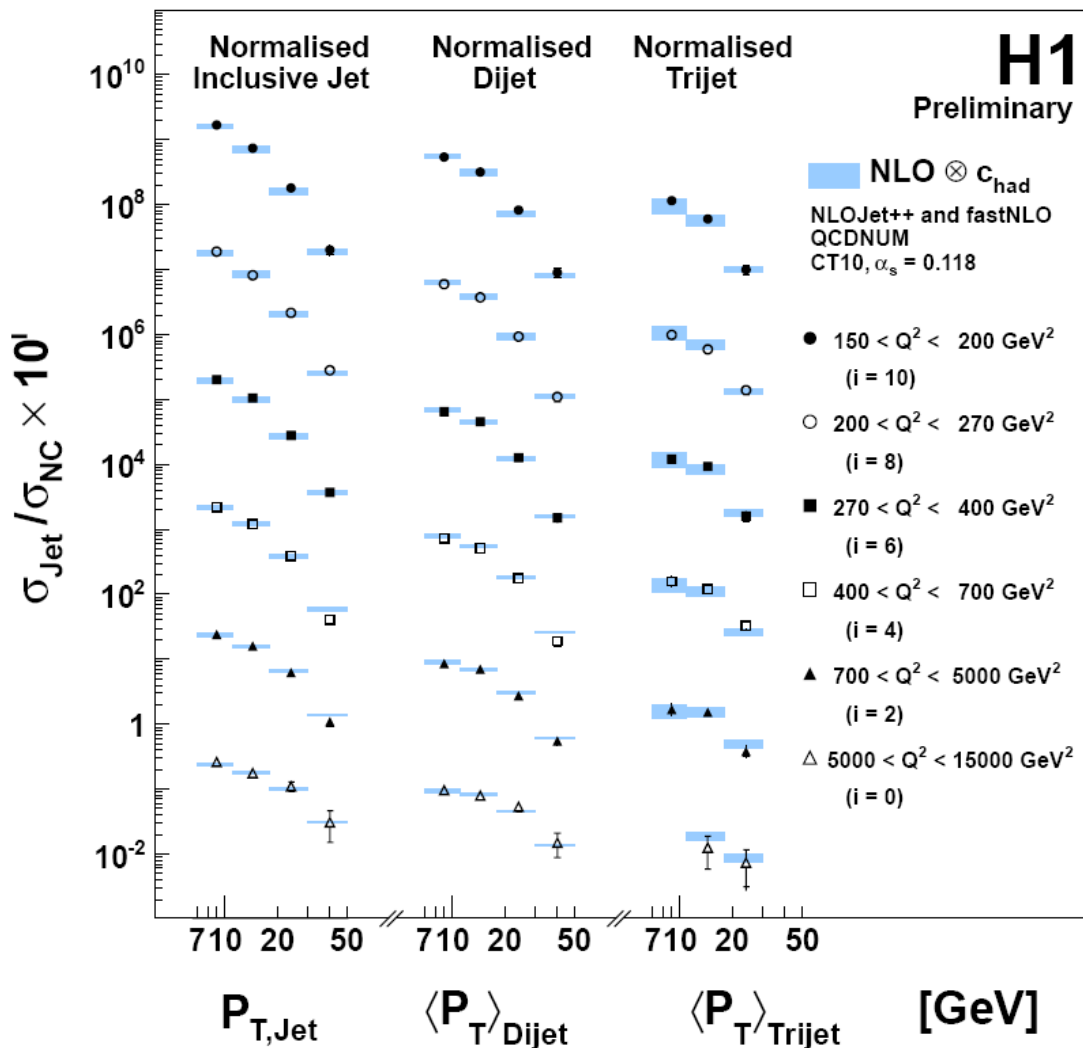
Unfolding solves equation  $\mathbf{m} = \mathbf{A} \cdot \mathbf{x}$

**Method: TUnfold**, regularized unfolding Root application (S. Schmitt, arXiv:1205.6201)

Particle level			<b>Trijet</b> $Q^2, \langle p_T \rangle_3, y,$ Trijet-cuts	$\epsilon_{J3}$
			<b>Dijet</b> $Q^2, \langle p_T \rangle_2, y,$ Dijet-cuts	$\epsilon_{J2}$
		<b>Incl. Jet</b> $p_T, Q^2, y, (\eta)$		$\epsilon_J$
	<b>DIS-Events</b> $(Q^2, y)$	Reconstructed jets without match to generator level	Reconstructed Dijet events which are not generated as Dijet event	Reconstructed Trijet events which are not generated as Trijet event
Detector level				

600 X 2200 bins

# Normalized multijet cross sections



**H1-Prel-12-031**

**NLO Calculation:**

PDF: CT10,  $\alpha_s = 0.118$

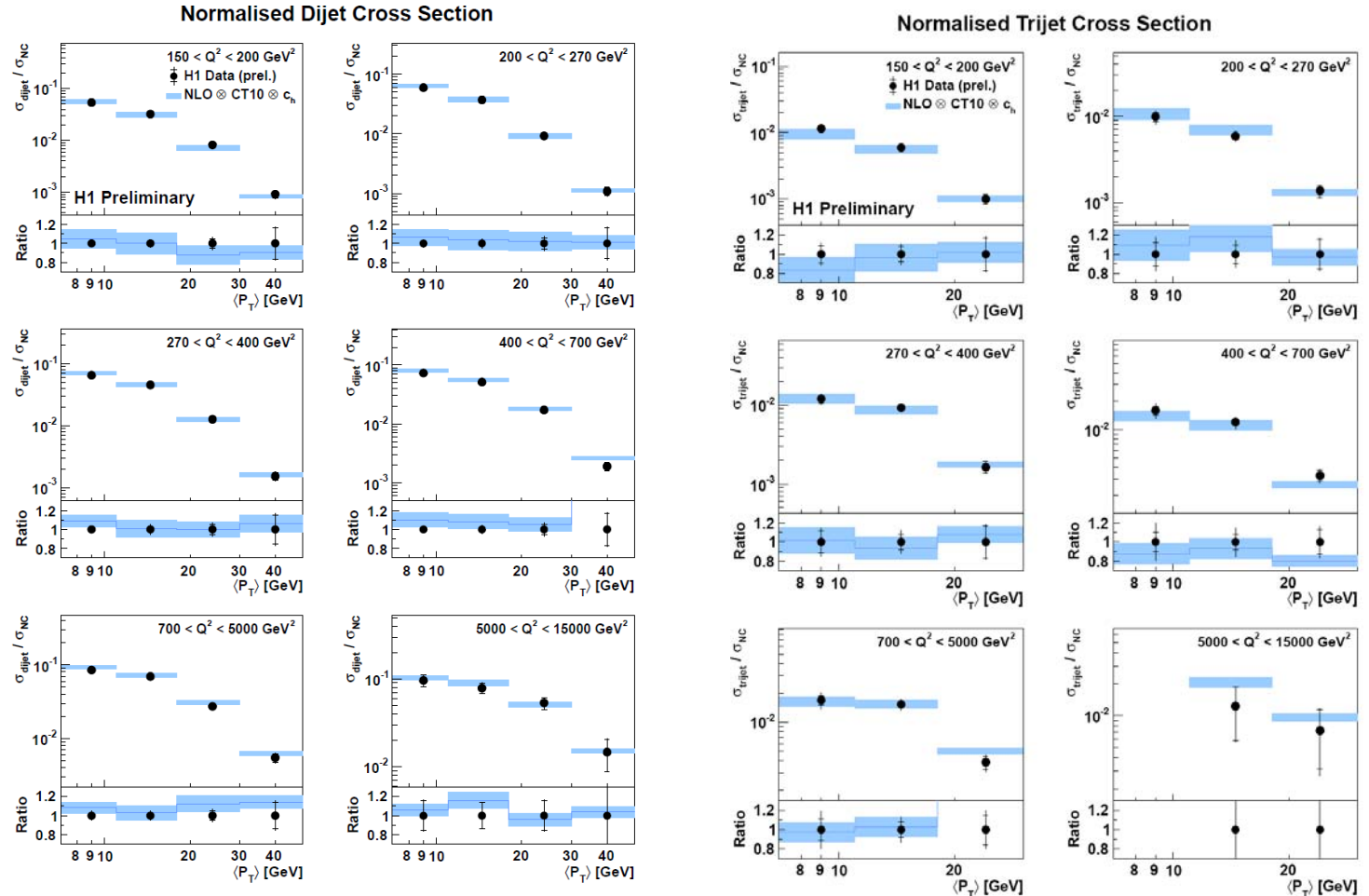
NLOJet++

FastNLO QCDNUM

Corrected for hadronisation

- **Trijets for the first time**
- **Small experimental errors**
- **Very good NLO and LO (trijets) description of the data**

# Normalized dijet and trijet cross sections



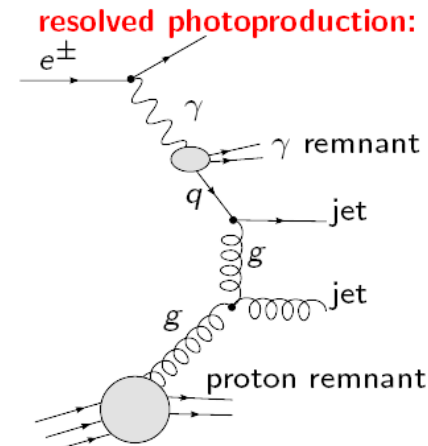
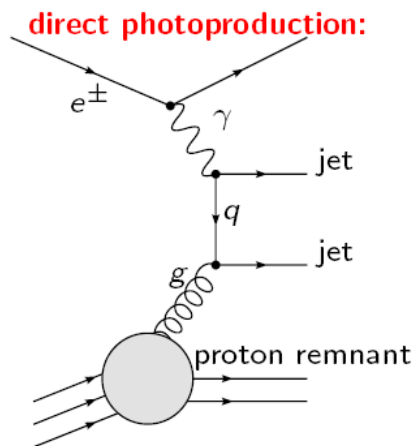
Except for highest  $Q^2$  bins experimental uncertainty much smaller than theoretical

# Jets in photoproduction ( $Q^2 \approx 0$ )

- Large cross section  $\rightarrow$  large statistics of jets with very high transverse momentum
- Single hard scale : jet  $p_T$

**Excellent for extraction of  $\alpha_s$**

**But...**



Multiple parton interactions and significant spread between photon structure functions ( $\gamma PDF$ ) - possible source of ambiguities

# Inclusive jet measurement in photoproduction

DESY-12-045 (March 2012) [Nucl. Phys. B864 \(2012\), pp. 1-37](#)

## Phase space

- $Q^2 < 1 \text{ GeV}^2$
- $0.2 < y_{JB} < 0.85$
- $E_T > 17 \text{ GeV}$
- $-1 < \eta^{\text{jet}} < 2.5$

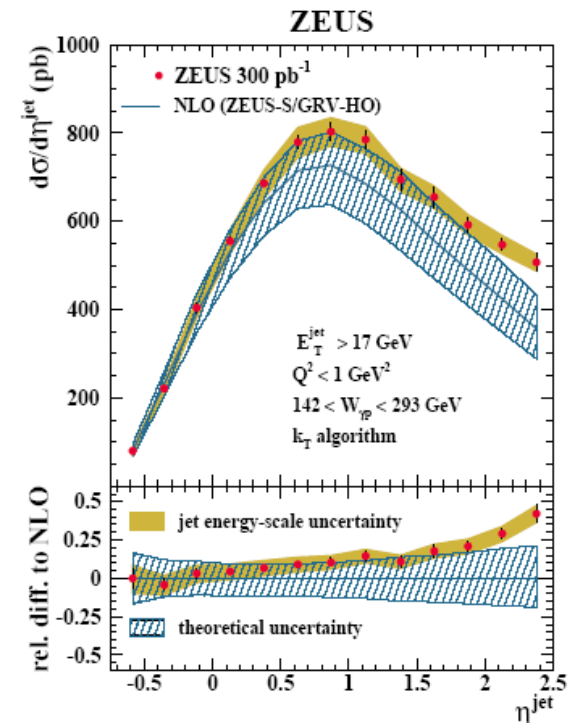
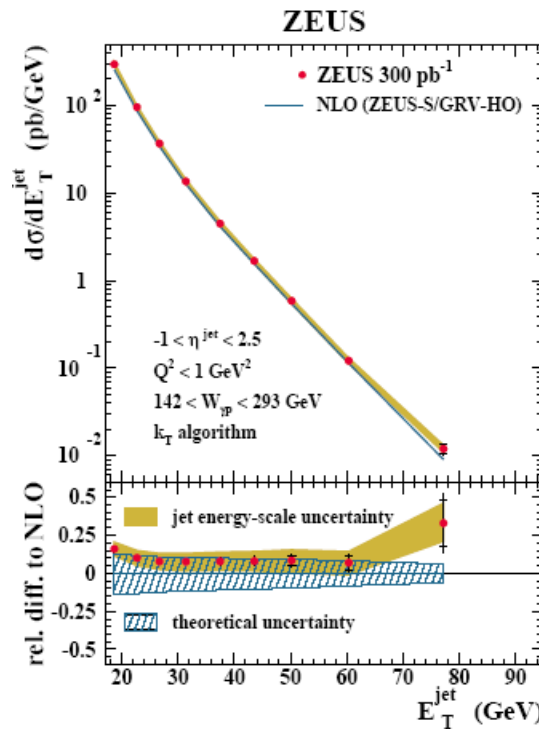
## NLO QCD

Klasen, Kleinwort, Kramer

pPDF: ZEUS-S

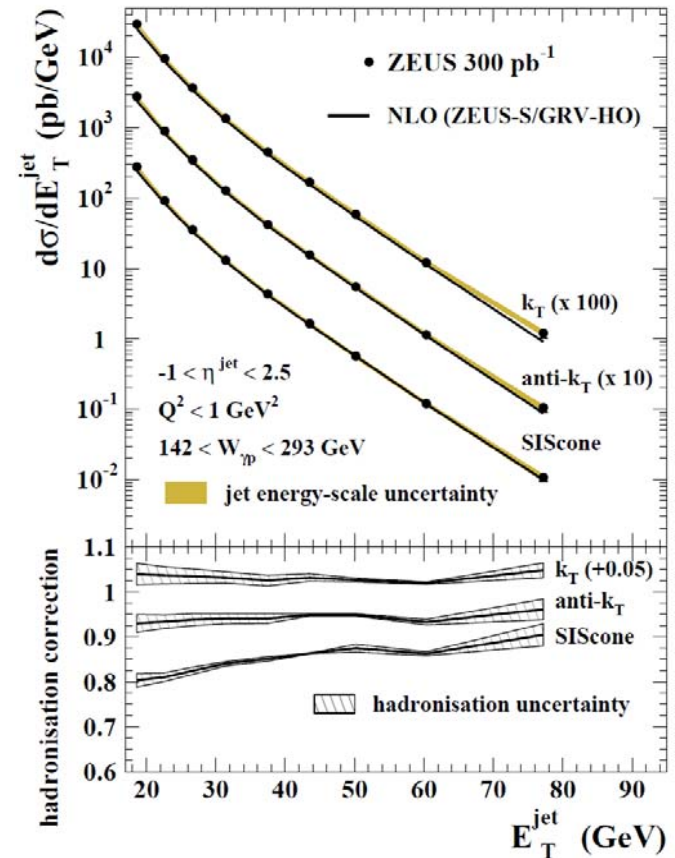
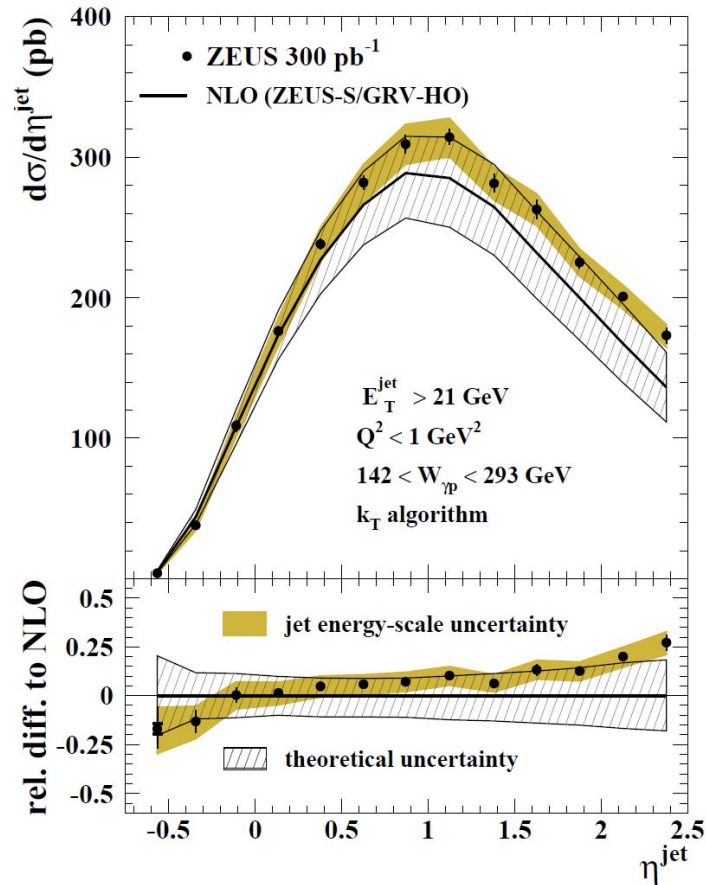
$\gamma$ PDF: GRV-HO

$\mu_r = \mu_f = E_T^{\text{jet}}$



- experimental uncertainty smaller than theoretical
- good description by NLO calculation except for  $\eta^{\text{jet}} > 2.0$
- MI and/or  $\gamma$ PDF possible source of discrepancies

# Inclusive jet measurement in photoproduction



- Good description in the whole  $\eta^{\text{jet}}$  range after raising threshold to  $E_T > 21$  GeV
- Stringent test of jet algorithms

# Determination of $\alpha_s(M_Z)$

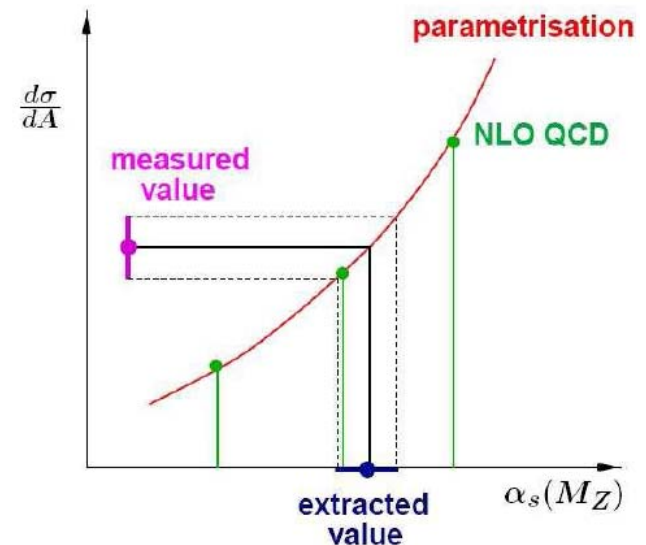
**H1: Hessian method:** Minimise  $\chi^2(\alpha_s)$

$$\chi^2 = \sum_{i=1}^N \frac{[d_i - t_i(1 - \sum_k \epsilon_k \Delta_{ik})]^2}{\sigma_{i,\text{stat}}^2 + \sigma_{i,\text{uncorr}}^2} + \sum_k \epsilon_k^2$$

- Keep PDF (CT10) fixed and fit  $\alpha_s$
- Theoretical uncertainty obtained by offset method : repeat fit with  $\mu_r$  and  $\mu_f$  varied by factor  $\frac{1}{2}$  and 2

## ZEUS:

- Parametrise theory using NLO calculations with PDF sets obtained for different  $\alpha_s$ .
- Measured value and its uncertainty is projected on the parametrization
- Theory uncertainty by band method (more sophisticated version of offset method  $\rightarrow$  30-50% smaller uncertainty)
- ZEUS method unlike H1 takes into account  $\alpha_s$  – PDF (gluon) correlation



# Extracted $\alpha_s(M_Z)$

$$\sigma^{\text{jet}} \rightarrow \sigma^{\text{parton}} \rightarrow \alpha_s(M_Z)$$

## Normalized multijets (k-factor < 1.3)

$\alpha_s = 0.1163 \pm 0.0011$	(exp)	Measurement of jet cross section	} theory
$\pm 0.0014$	(PDF)	Dependence on proton PDF	
$\pm 0.0008$	(had)	Hadron $\rightarrow$ parton level	
$\pm 0.0045$	(scale)	$\mu_r$ and $\mu_f$ dependence	

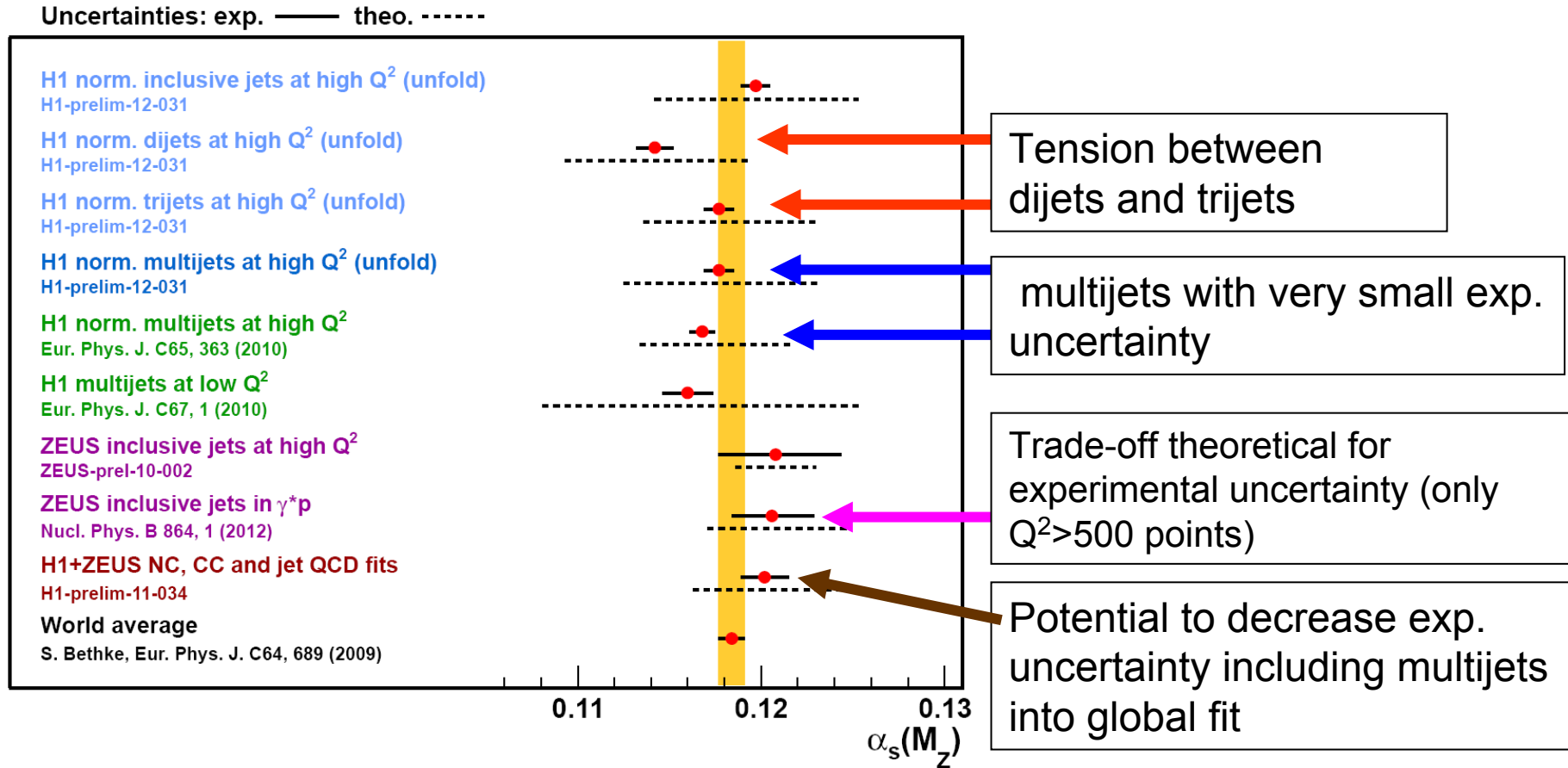
**Theory uncertainty dominated by scale and  $\gg$  experimental uncertainty**

## Photoproduction inclusive jets $E_T > 21$ GeV

$$\alpha_s = 0.1206 \pm 0.002 \text{ (exp)}$$
$$\pm 0.004 \text{ (theory)}$$

**$\gamma$ PDF and scale contribute equally to theory uncertainty**

# Comparison of extracted $\alpha_s(M_Z)$ values



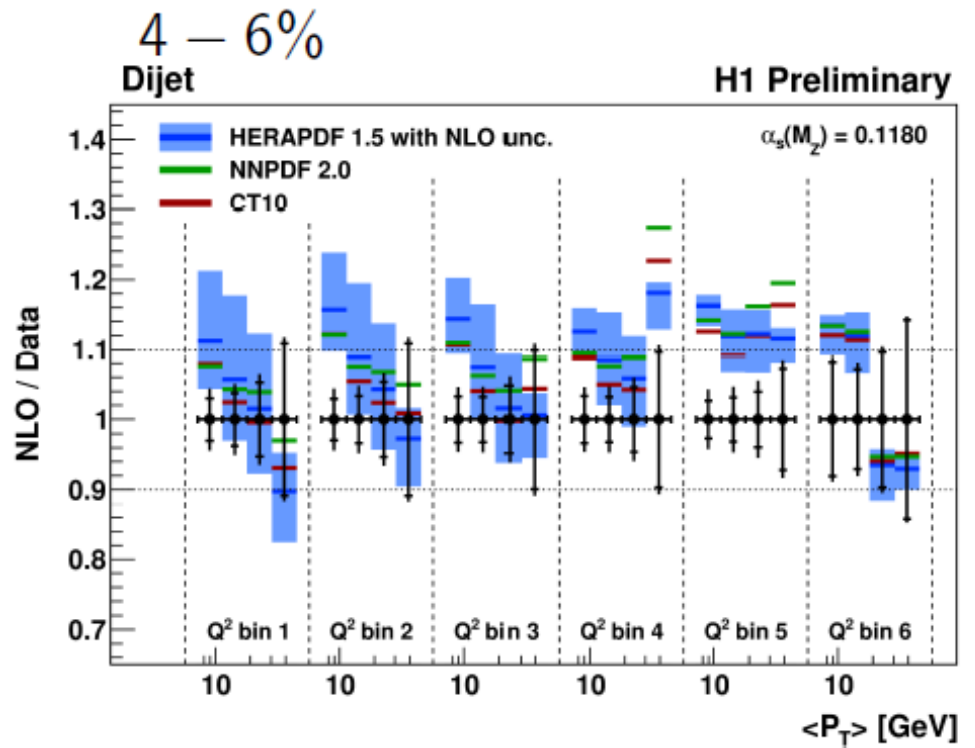
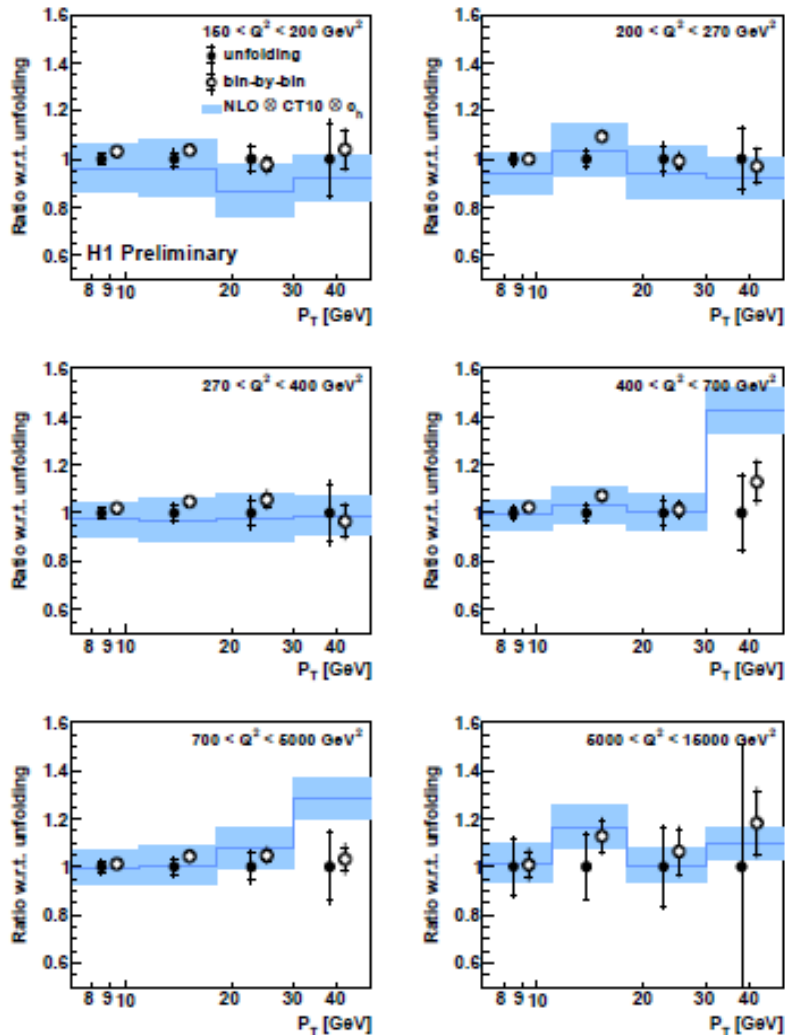
Experimental uncertainty much smaller than theoretical, dominated by missing NNLO  
 All results compatible with world average within uncertainties

# Summary

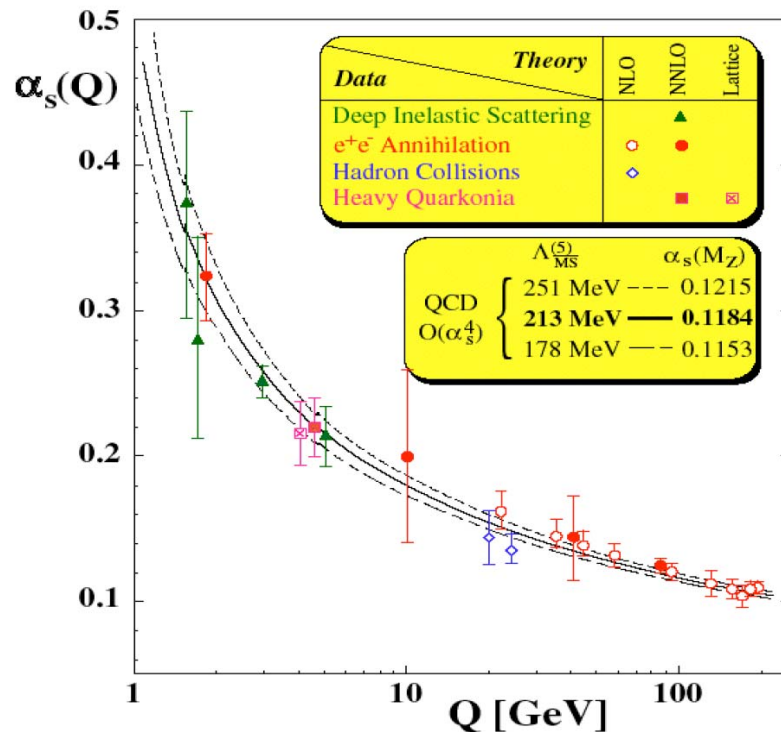
- ❑ Recent precision jet measurements at high  $Q^2$  (H1) and in photoproduction (ZEUS)
- ❑ Inclusive jet, dijet and trijet measurements at high  $Q^2$  using multidimensional unfolding, very small experimental uncertainties, good description of the data by NLO (jet, dijet) and LO (trijet) calculation
- ❑ Inclusive jet measurement in photoproduction, good description of the data by NLO calculation for  $E_T > 21$  GeV
- ❑ **In general, the data are more precise than QCD predictions**
- ❑ **Extracted values of  $\alpha_s$  are consistent with world average and their experimental uncertainties are much smaller than theoretical**
- ❑ In the inclusive multijet measurement, theoretical  $\alpha_s$  uncertainty is dominated by missing NNLO terms of the perturbative expansion
- ❑ In the inclusive photoproduction jet measurement terms beyond NLO and  $\gamma PDF$  contribute similarly to theoretical  $\alpha_s$  uncertainty

# Backup slides

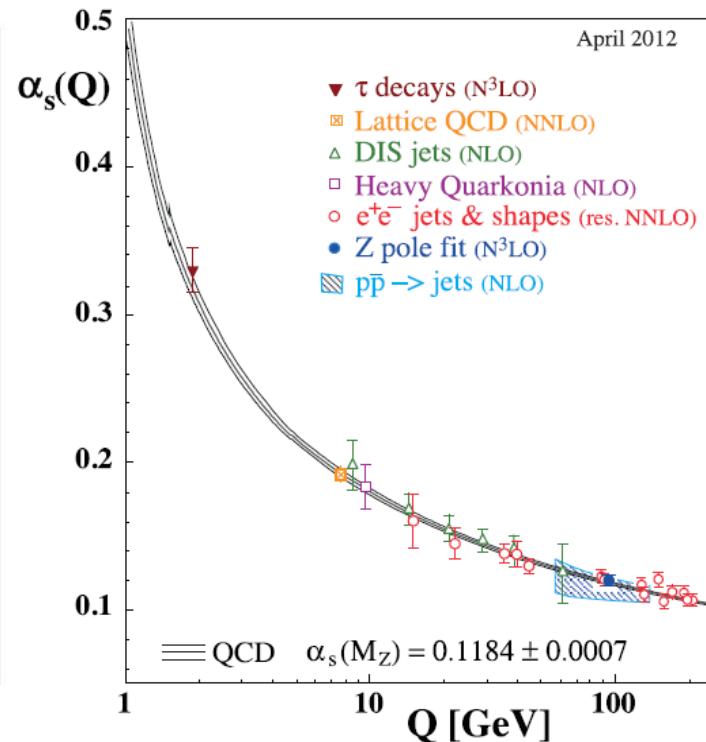
Normalised Inclusive Jet Cross Section



# $\alpha_s(M_Z)$ – fundamental constant



Copied from slide of prof. Frank Wilczek Nobel Lecture **2004**

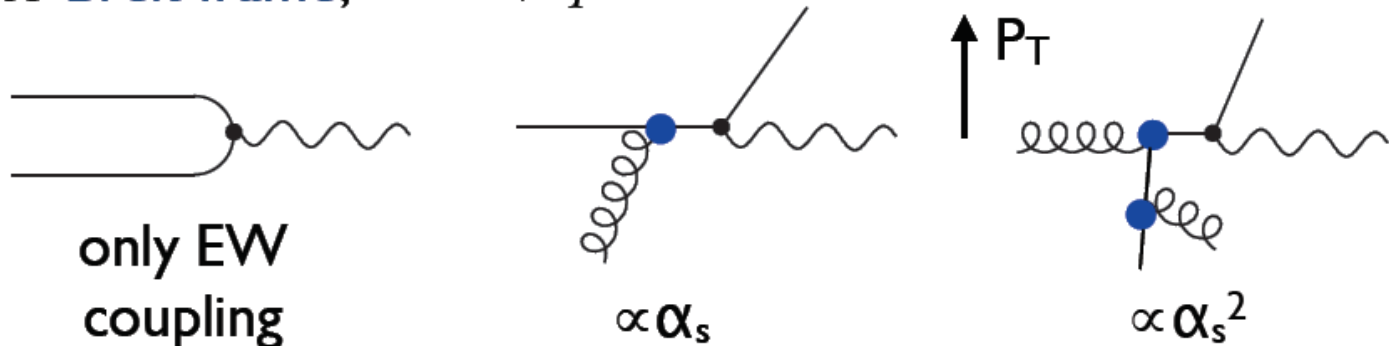


Running  $\alpha_s$  compilation from **2012** PDG QCD review

$\alpha_s(M_Z)$  is a fundamental constant of the nature, it is not possible to exaggerate in efforts to increase the accuracy of the measurements

# Jet production in DIS

Boost to **Breit frame**,  $2xP + q = 0$



- In Breit frame only hard QCD processes generate considerable  $p_T$
- Inclusive jets, dijets, trijets...: at least one, two three.. jet above certain threshold in  $p_T$
- $n$ -jet production in LO proportional to  $\alpha_s^{n-1}$